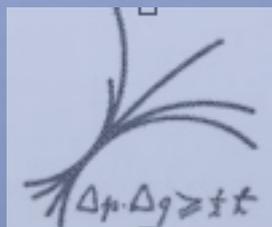


Axion cold dark matter: two birds with the same stone

Javier Redondo (LMU & MPP München)

27 Nov 2012, Invisible seminar



Outline

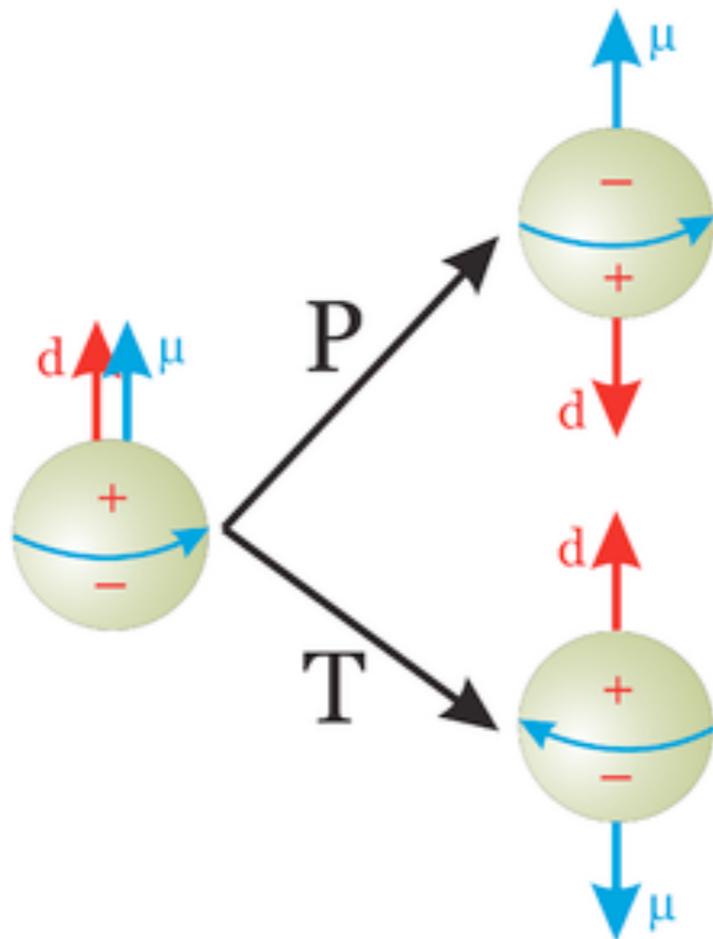
- **Strong CP problem**
- **Strong CP solution: Axions**
- **Axion Dark matter**
- **Experimental searches**

The Strong CP problem

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \theta$$

$$\theta = \theta_{\text{QCD}} + \arg \det \mathcal{M}_q$$

$\theta_{\text{QCD}} \in (-\pi, \pi)$
 $\arg \det \mathcal{M}_q \sim \mathcal{O}(1)?$



Prediction:

$$d_n \sim 10^{-15} \theta \text{ ecm}$$

Non Observation:

$$d_n < 2.6 \times 10^{-26} \text{ ecm}$$

$$\theta \lesssim 10^{-11} \quad \text{Why ??????}$$

The Strong CP problem: a hint

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \theta$$

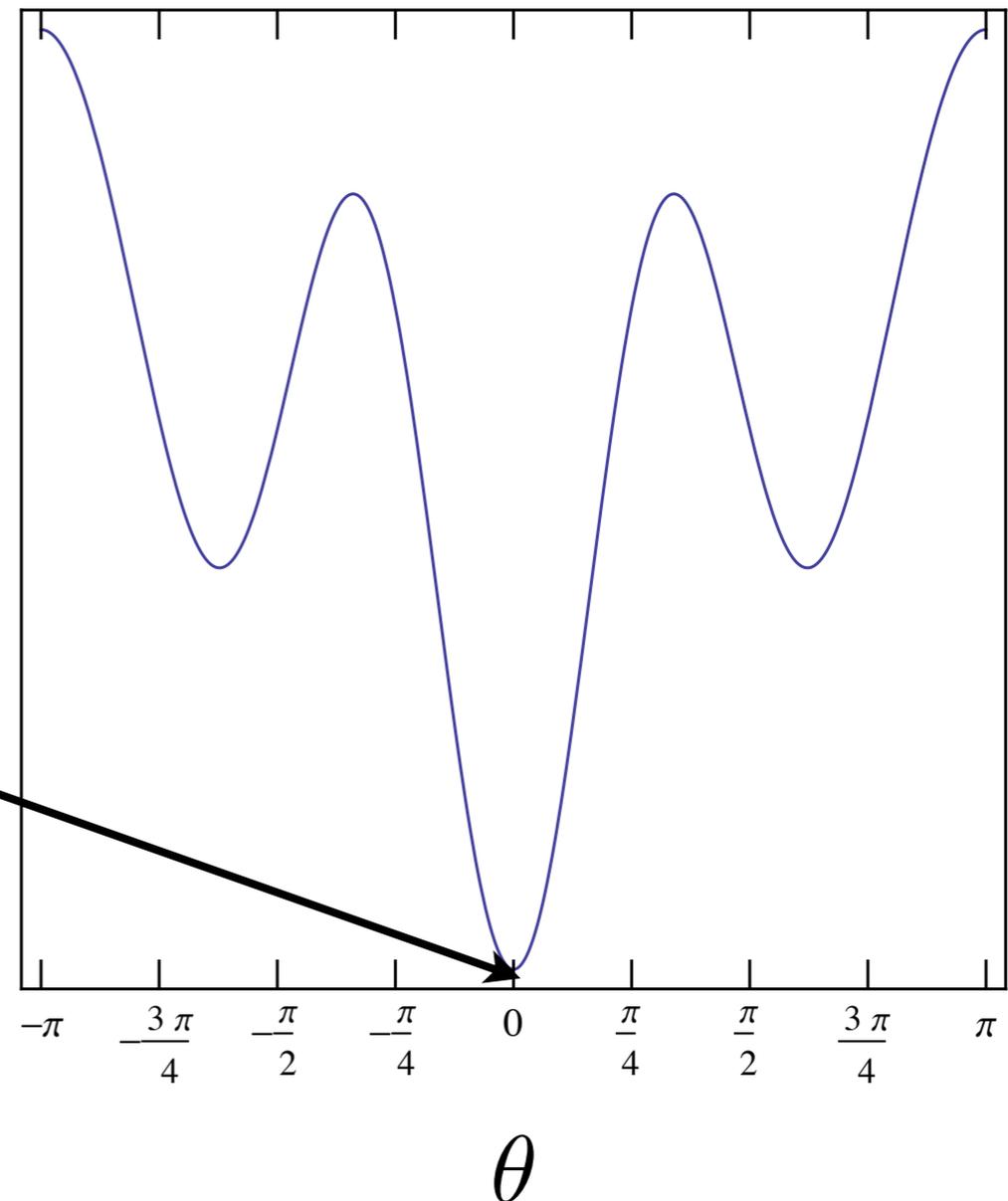
Consider no quarks

If the rest of the theory is P,T invariant

Minimum at $\theta = 0$

but θ is not dynamical

$V_{\text{eff}}(\theta)$



The Strong CP problem: a hint

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \theta$$

$V_{\text{eff}}(\theta)$

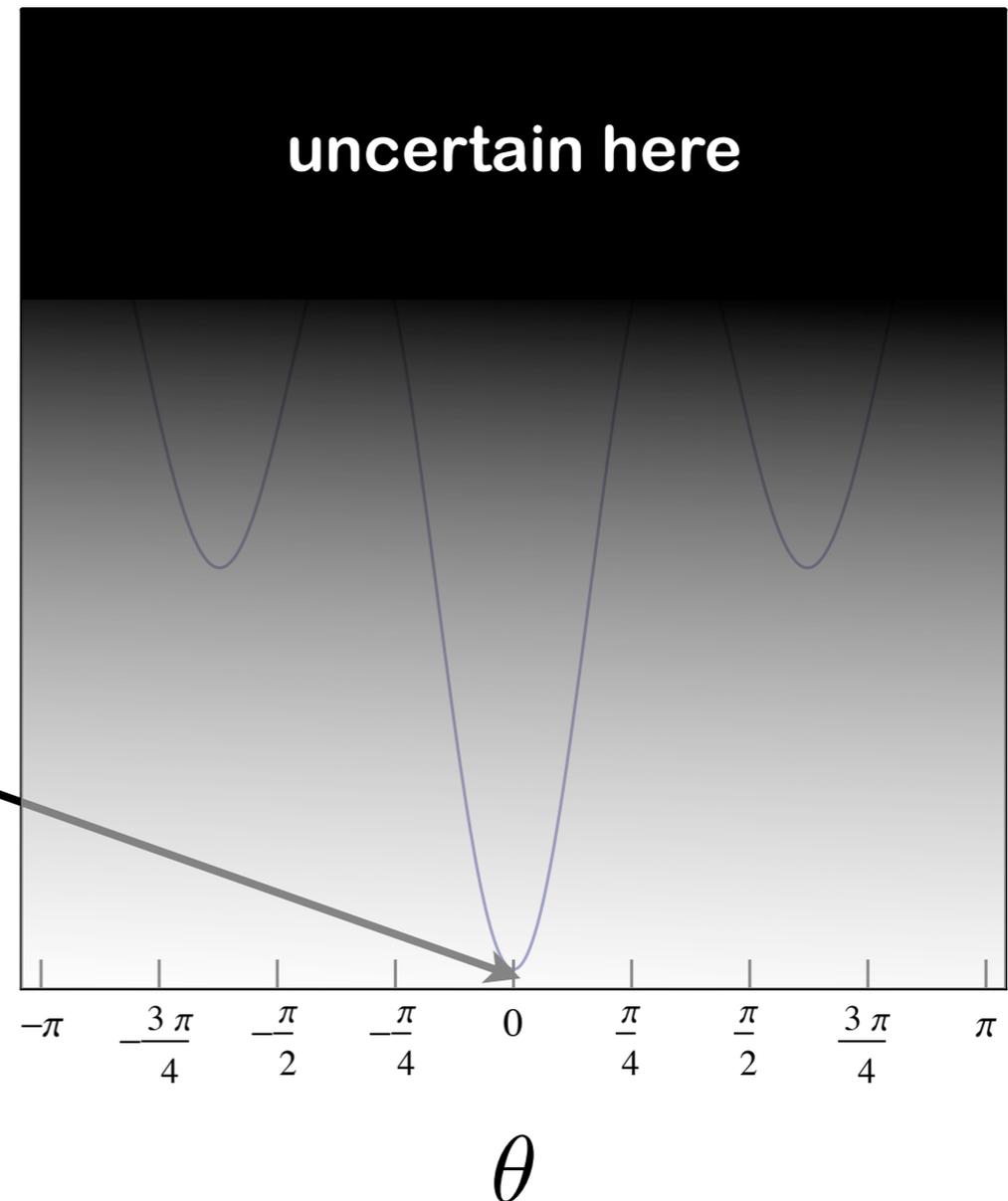
uncertain here

Consider no quarks

If the rest of the theory is P,T invariant

Minimum at $\theta = 0$

but θ is not dynamical



The Strong CP problem: a hint

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \left(\theta + \frac{\eta'}{f_\eta} \right)$$

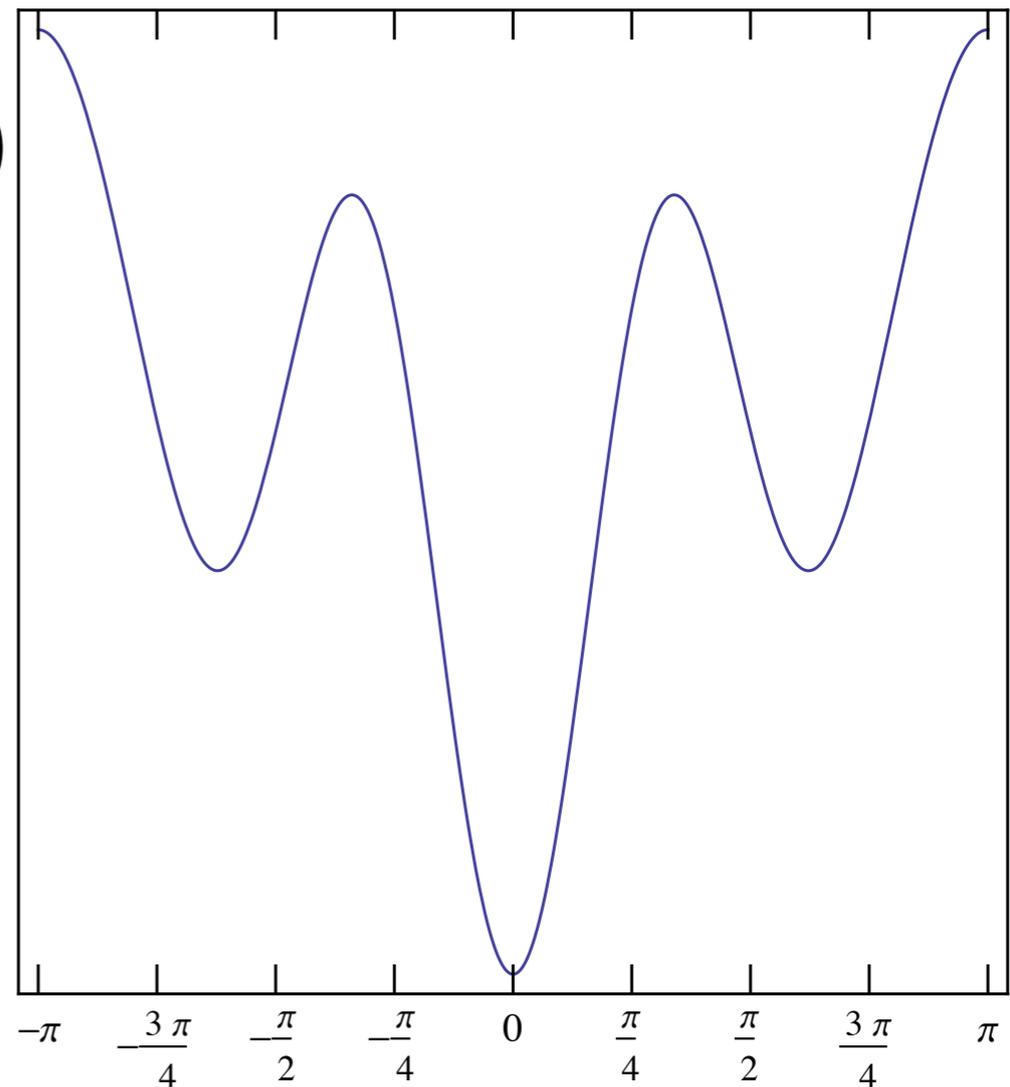
With quarks, low-energy QCD

$U(1)_A$ is color anomalous

η' has anomalous gg coupling

can roll down the potential and restore
P, T symmetries!!

$V_{\text{eff}}(\theta_{\text{eff}})$



$$\theta_{\text{eff}} = \theta + \langle \eta' \rangle / f_\eta$$

The Strong CP problem: a hint

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \left(\theta + \frac{\eta'}{f_\eta} \right) - \frac{1}{2} m_\pi^2 \eta'^2$$

With quarks, low-energy QCD

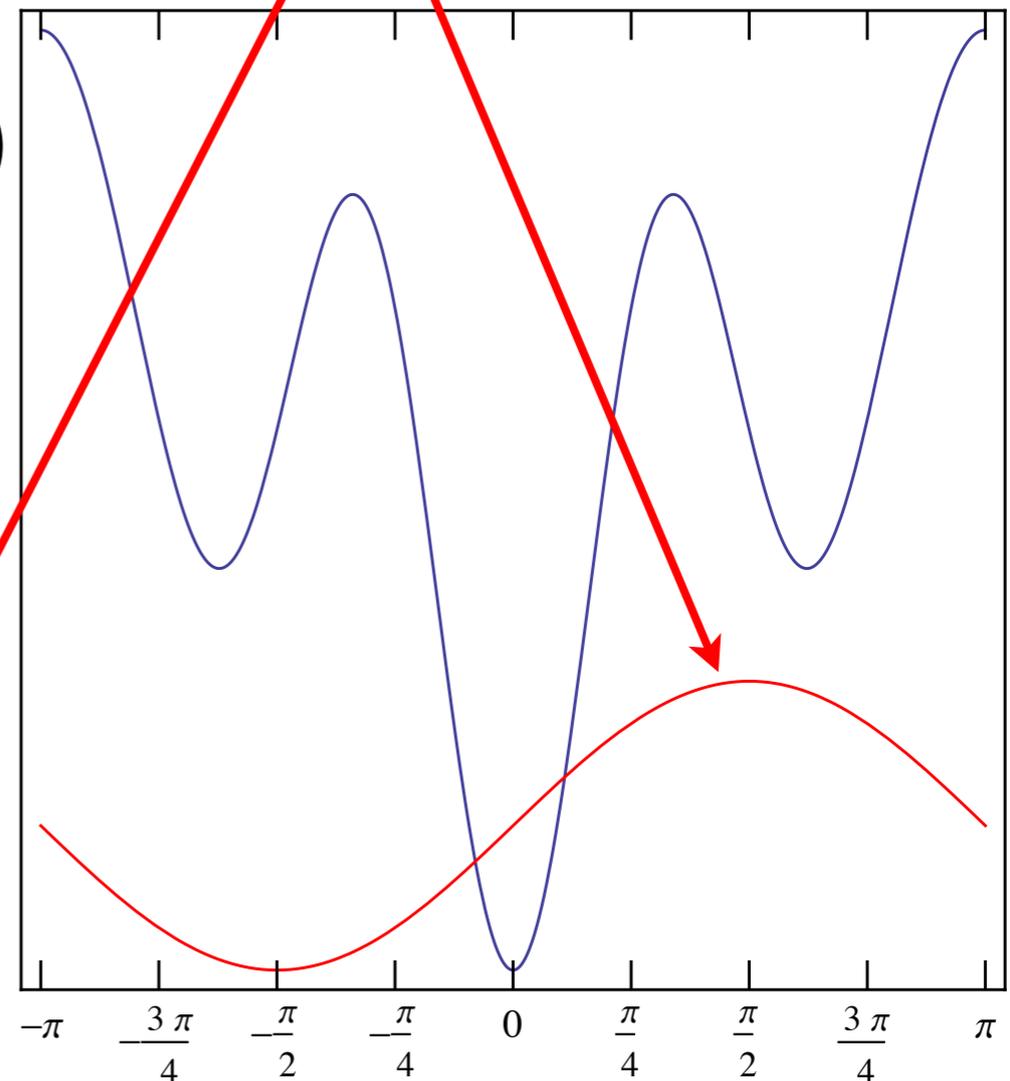
$U(1)_A$ is color anomalous

η' has anomalous gg coupling

~~can roll down the potential and restore P, T symmetries!!~~

Actually cannot because EW SB makes $m_u, m_d \neq 0$ and breaks explicitly $U(1)_A$ giving η' mass of the order of the π^0 mass.

$V_{\text{eff}}(\theta_{\text{eff}})$



$$\theta_{\text{eff}} = \theta + \langle \eta' \rangle / f_\eta$$

The Strong CP problem: a hint

$$\mathcal{L}_\theta = V(\eta') = \frac{1}{2} m_{\eta'}^2 (\eta' + \theta f_\eta)^2 + \frac{1}{2} m_\pi^2 \eta'^2$$

$V_{\text{eff}}(\theta_{\text{eff}})$

With quarks, low-energy $U(1)_A$ is color anomalous. η' has anomalous

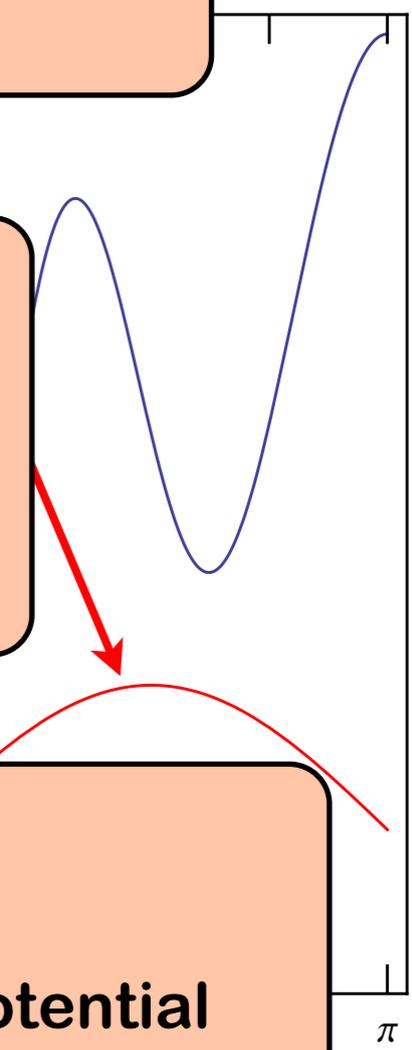
$$\theta_{\text{eff}} = \theta \frac{m_\pi^2}{m_{\eta'}^2 + m_\pi^2} \simeq 0.02\theta$$

~~can roll down the potential and restore P, T sym~~

The effective value of θ decreases and in the limit $m_\pi \rightarrow 0$ vanishes since η' can freely roll down the instantonic potential

Actually makes m_π explicit $U(1)_A$ giving η a mass of the order of the π^0 mass.

$$\theta_{\text{eff}} = \theta + \langle \eta' \rangle / f_\eta$$



Axion as a solution to the strong CP problem

$$\mathcal{L}_\theta = \frac{\alpha_s}{8\pi} \text{tr} \left\{ G_a^{\mu\nu} \tilde{G}_{a\mu\nu} \right\} \left(\theta + \frac{\eta'}{f_\eta} + \frac{\phi}{f_a} \right) - \frac{1}{2} m_\pi^2 \eta'^2$$

$$V_{\text{eff}}(\theta_{\text{eff}})$$

Add a new field coupling to gg

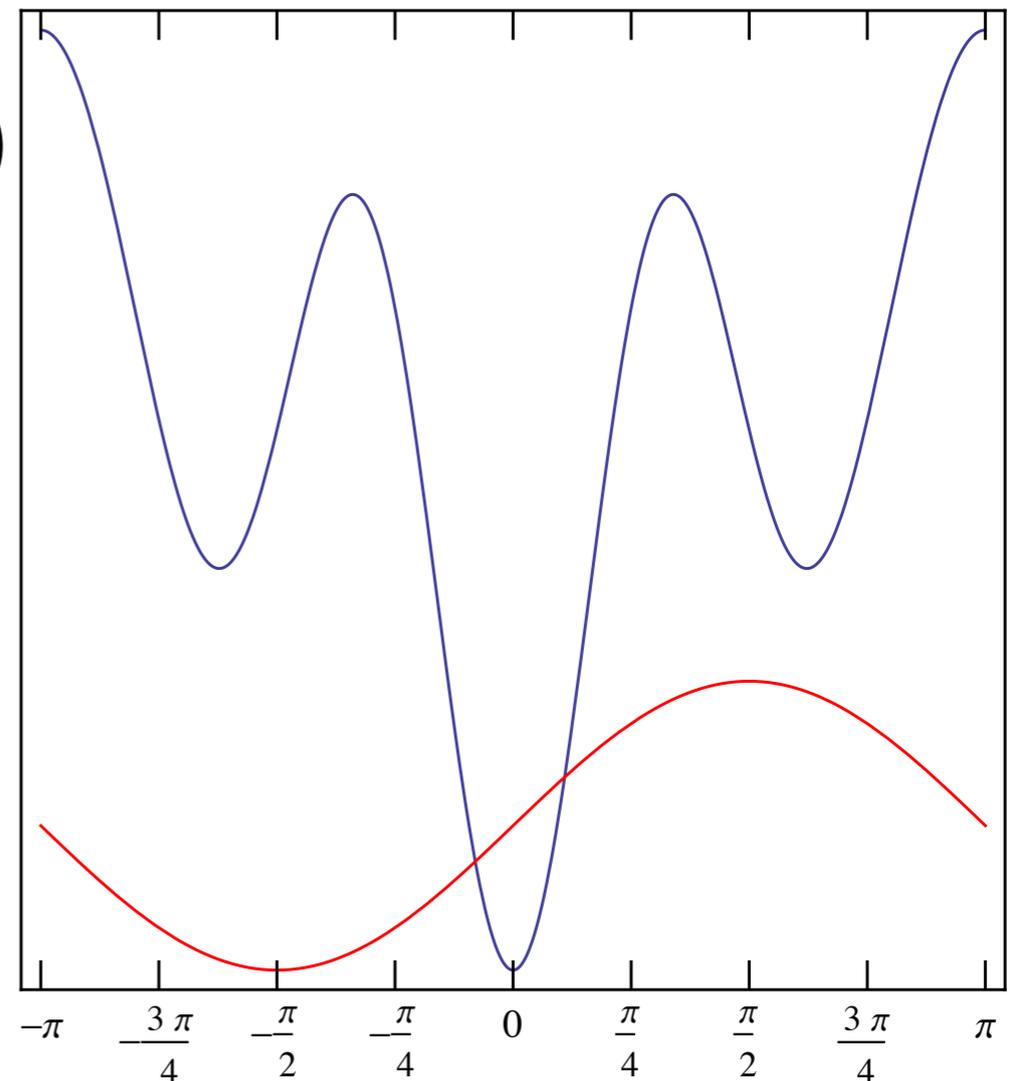
Goldstone of ANOTHER $U(1)_A$

usually called Peccei-Quinn symmetry

$$\langle \eta' \rangle = 0$$

$$\langle \phi \rangle / f_a = -\theta$$

$$\theta_{\text{eff}} = 0!!!!$$



$$\theta_{\text{eff}} = \theta + \langle \eta' \rangle / f_\eta + \langle \phi \rangle / f_a$$

Axion couplings/mass

(minimal, hadronic model)

$$V(\eta') = \frac{1}{2} m_{\eta'}^2 \left(\eta' + \phi \frac{f_\eta}{f_a} \right)^2 + \frac{1}{2} m_\pi^2 \frac{f_\pi^2}{f_\eta^2} \eta'^2$$

$$a = \phi - \eta' \frac{f_\eta}{f_a}$$

$$m_a^2 \simeq m_\pi^2 \left(\frac{f_\pi}{f_a} \right)^2$$

axion = orthogonal to physical η'

the axion gets a calculable mass

$$m_a \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$

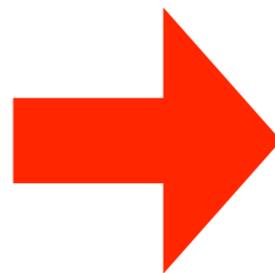
And calculable mixings
with the neut. ps. mesons

couplings to hadrons

$$\varphi_{a\eta'} \sim f_\eta / f_a$$

$$\varphi_{a\eta} \sim f_\eta / f_a$$

$$\varphi_{a\pi^0} \sim f_{\pi^0} / f_a$$



$$\sim \bar{N} \gamma_\mu \gamma_5 N \frac{\partial^\mu a}{f_a}$$

Axion couplings/mass

In a general model it depends how $U(1)_{PQ}$ is implemented

- Only axion term is in the anomaly \rightarrow hadronic axions (KSVZ)
- In the original Peccei-Quinn Model & variants, and DFSZ the axion is a combination of EW Higgs phases and therefore axions couple at tree level to leptons as well

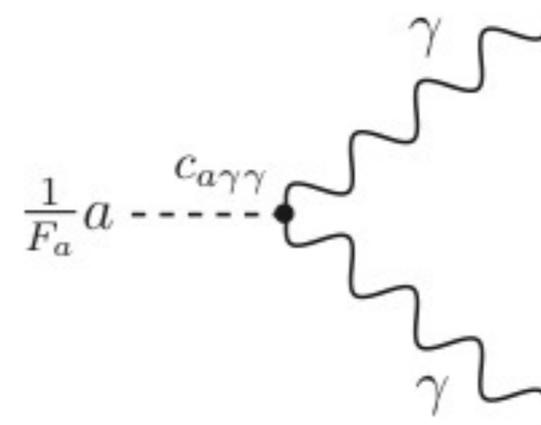
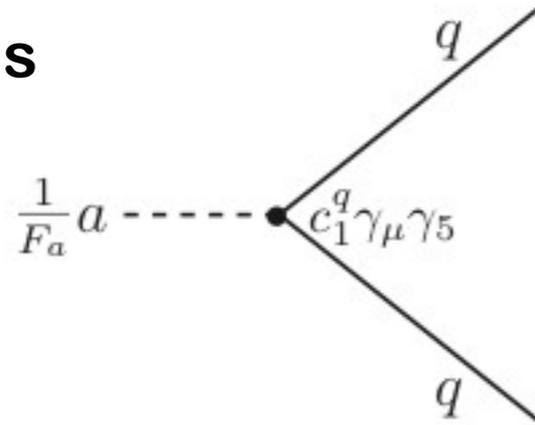
$$L_{\text{Yukawa}} = \Gamma_{ij}^u \bar{Q}_{Li} \Phi_1 u_{Rj} + \Gamma_{ij}^d \bar{Q}_{Li} \Phi_2 d_{Rj} + \Gamma_{ij}^\ell \bar{L}_{Li} \Phi_2 \ell_{Rj} + h.c.$$

$$\Phi_1 = \frac{v_1}{\sqrt{2}} e^{iax/v_F} \begin{bmatrix} 1 \\ 0 \end{bmatrix} ; \quad \Phi_2 = \frac{v_2}{\sqrt{2}} e^{ia/xv_F} \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \quad x = v_2/v_1$$

However $f_a \sim v_F$ was very soon ruled out,
the only plausible option becoming $f_a \gg v_F$ (INVISIBLE axions)

Axion couplings

Hadronic axions



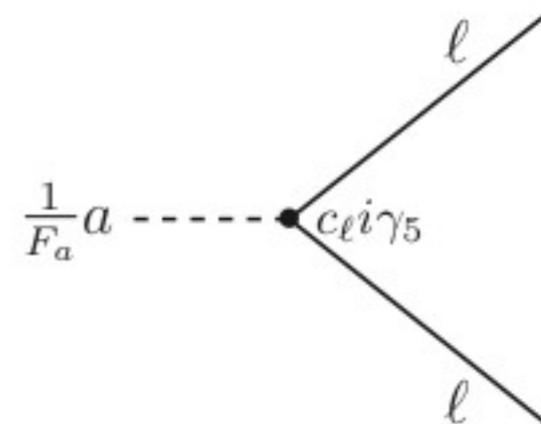
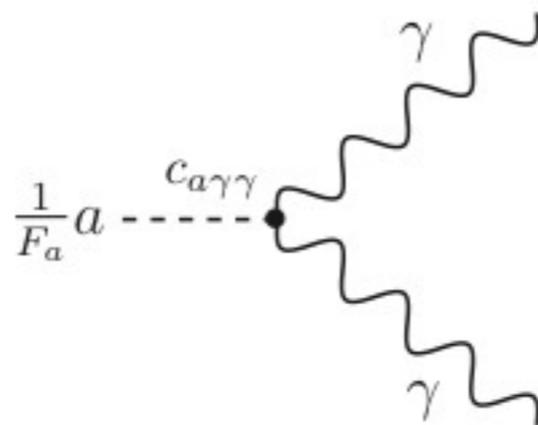
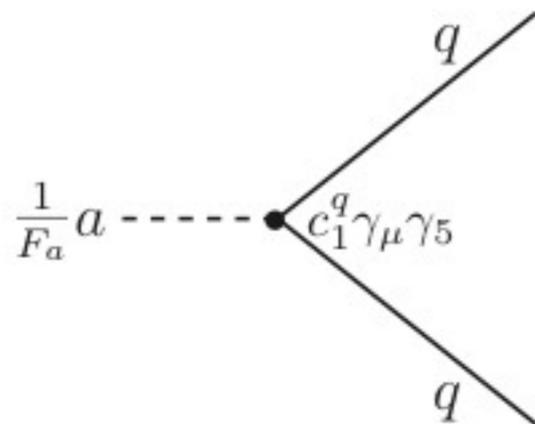
$$c_N (\bar{N} \gamma_\mu \gamma_5 N) \frac{\partial^\mu a}{2f_a} \equiv \frac{c_N m_N}{f_a} \bar{N} \gamma_5 N$$

$$g_{aN} = \frac{c_N m_N}{f_a}$$

$$\frac{\alpha}{8\pi} (F_{\mu\nu} \tilde{F}^{\mu\nu}) c_{a\gamma\gamma} \frac{a}{f_a}$$

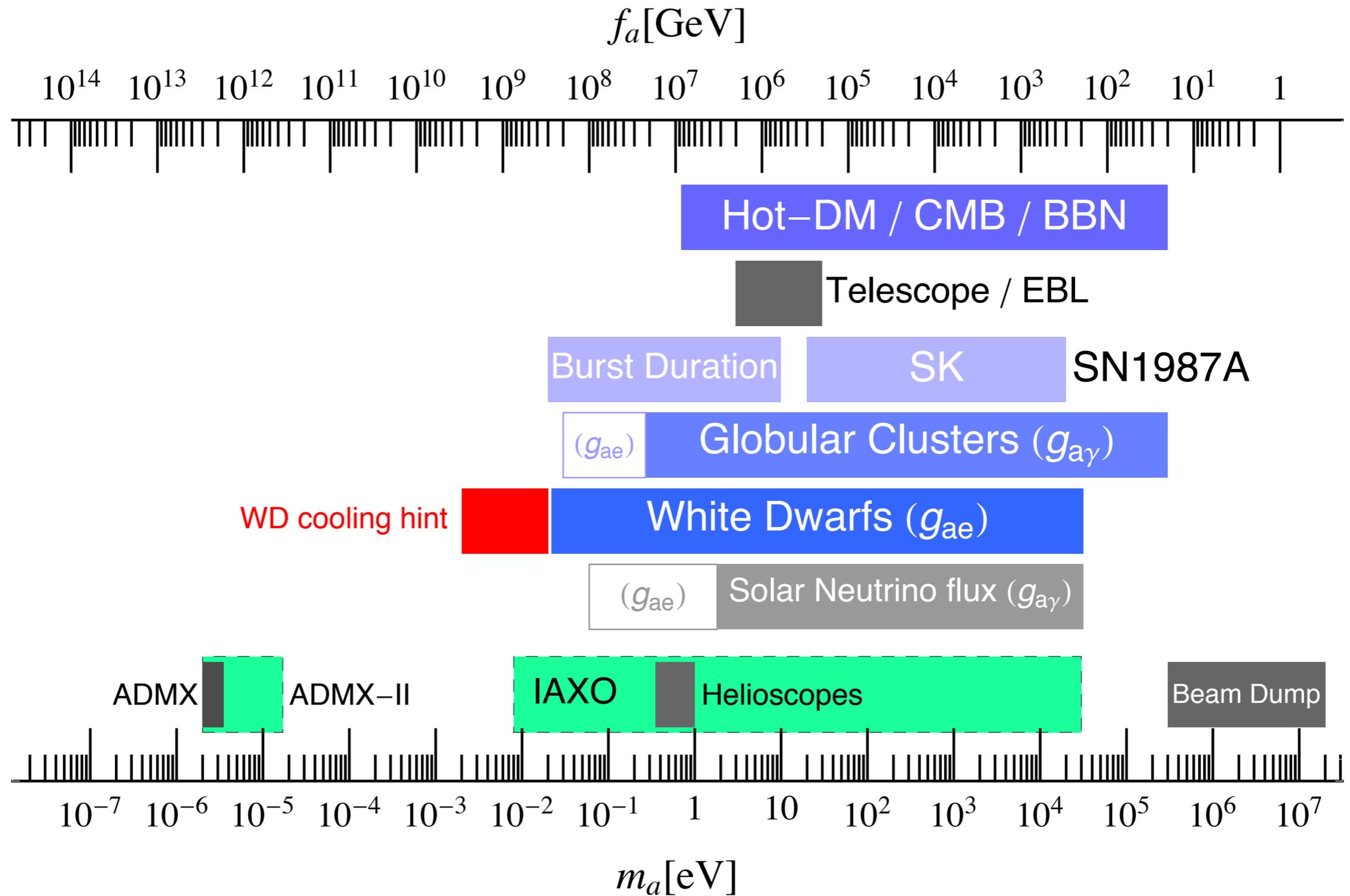
$$g_{a\gamma} = c_{a\gamma\gamma} \frac{\alpha}{2\pi f_a}$$

Non Hadronic



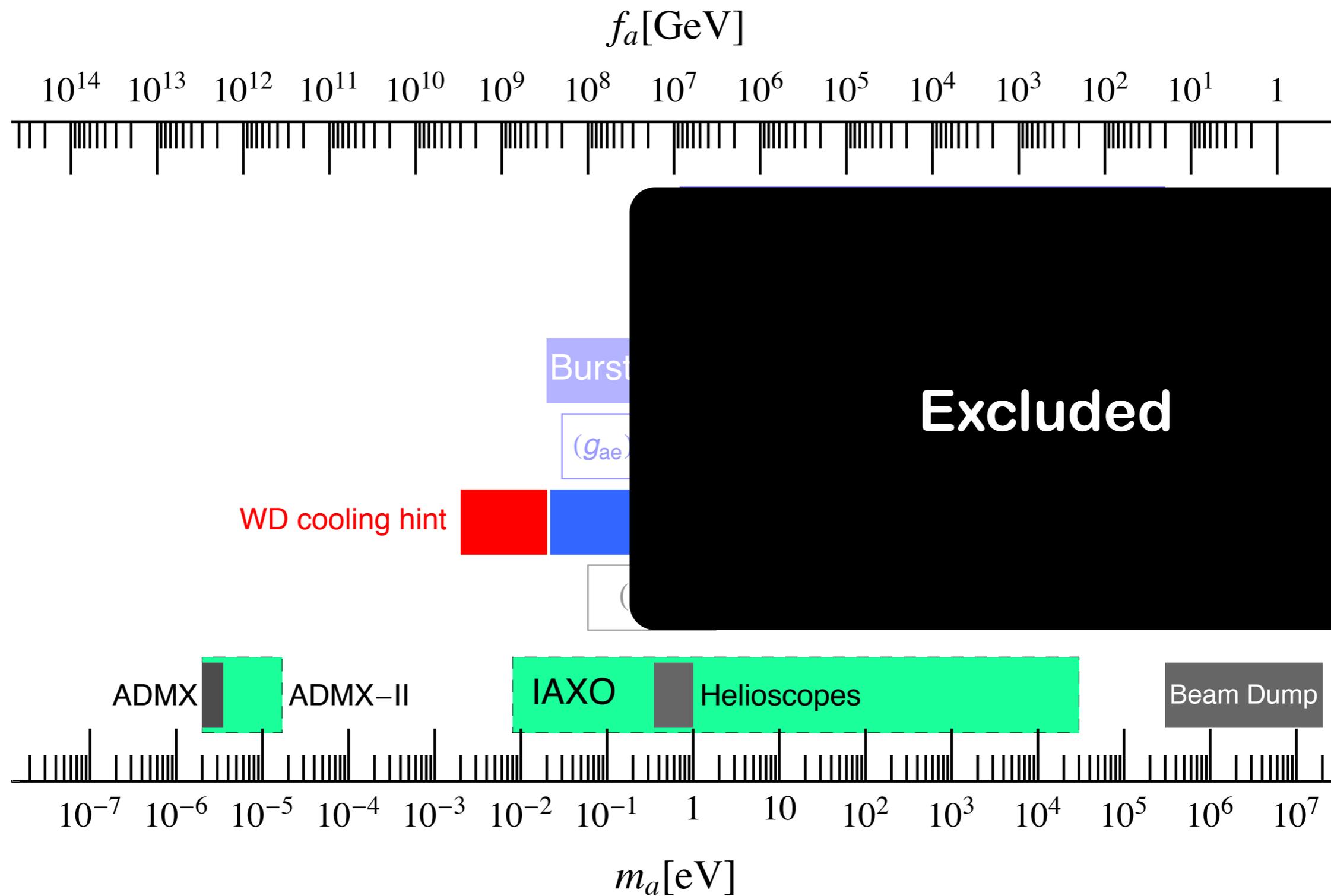
Where we are

Hewett et al. arXiv:1205.2671



Where we are

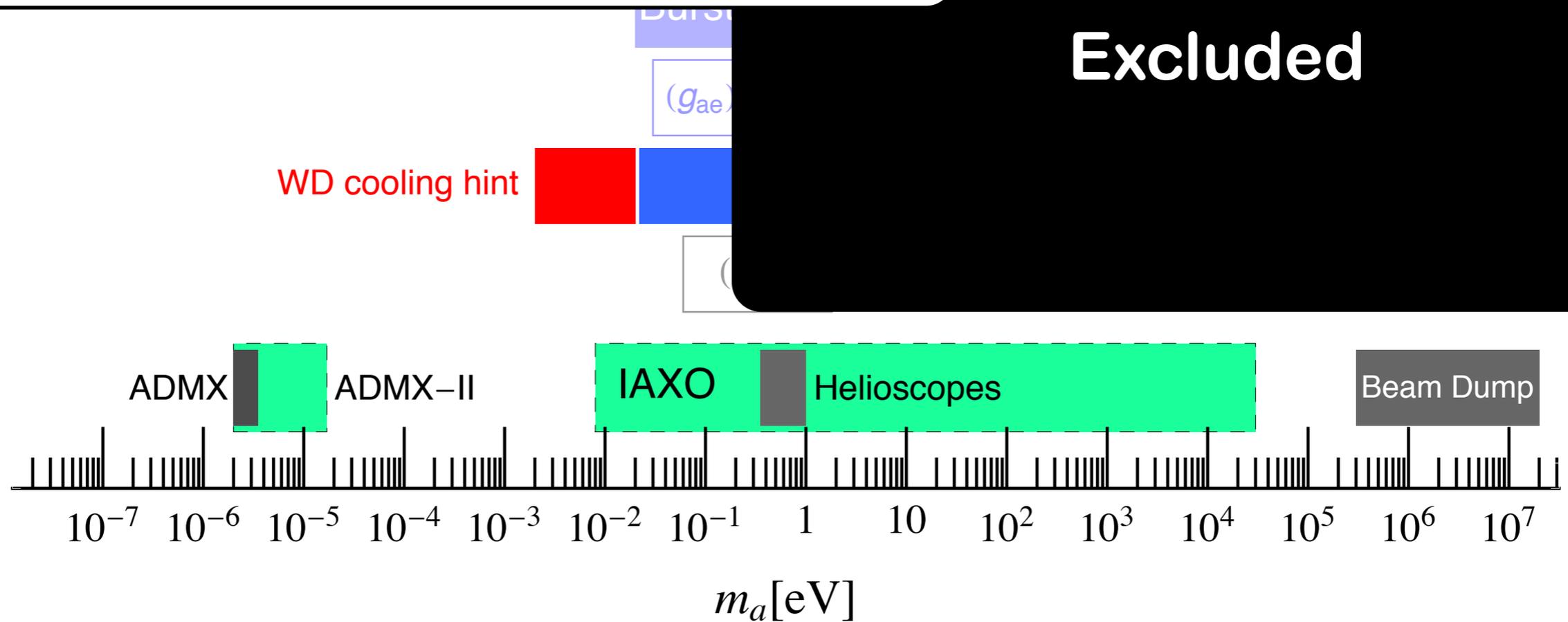
Hewett et al. arXiv:1205.2671





THIS TALK

Excluded

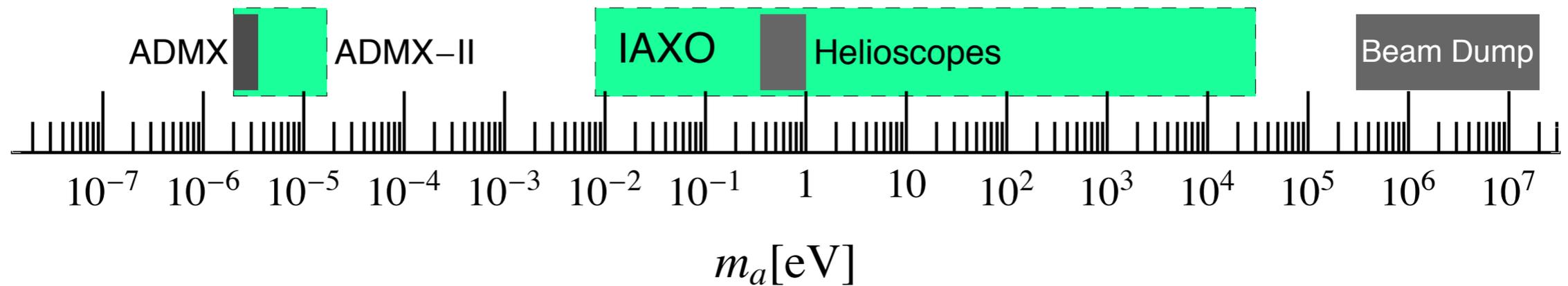




THIS TALK

Cold Dark Matter

Excluded



Where we are

Hewett et al. arXiv:1205.2671

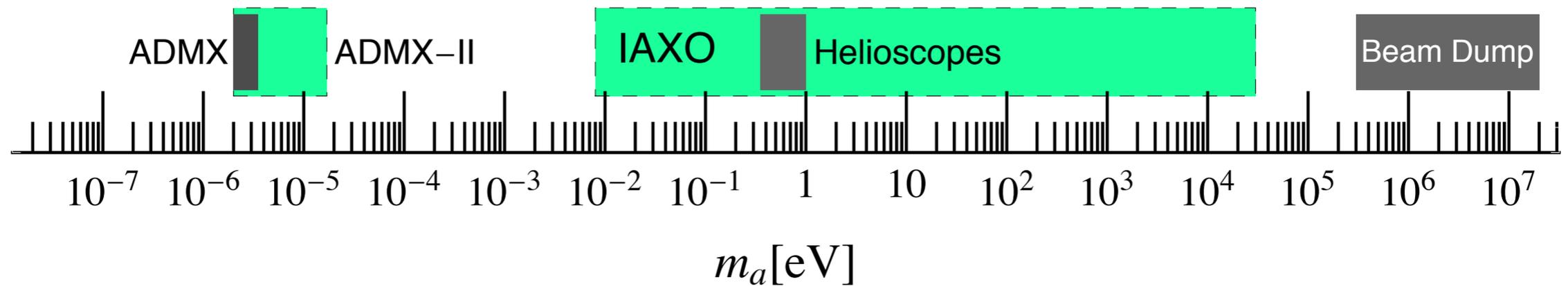


THIS TALK

Cold Dark Matter

Hot!

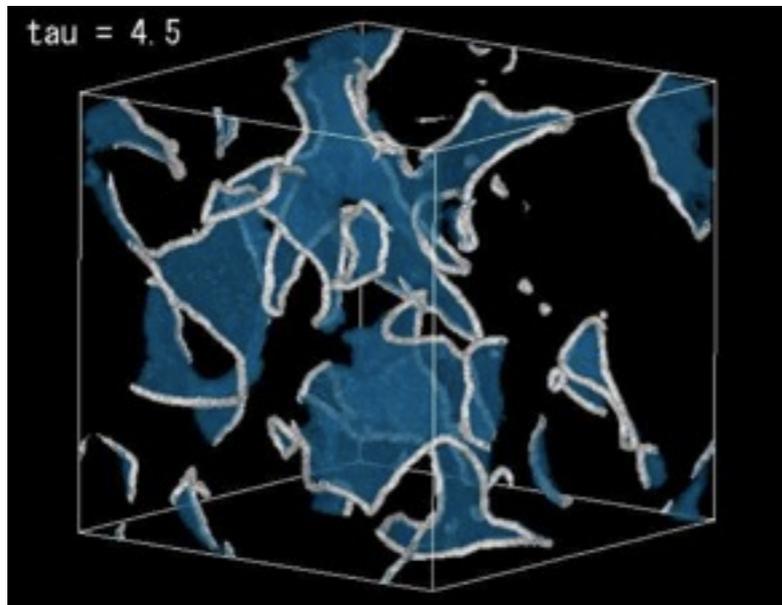
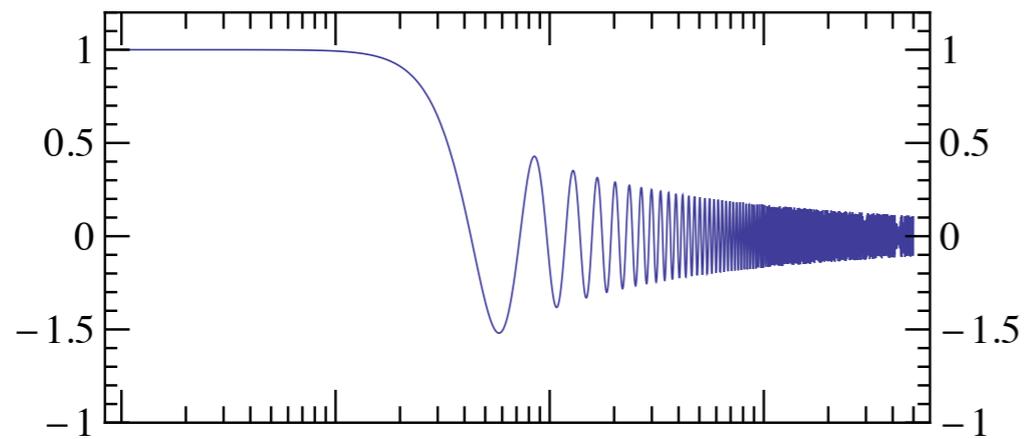
Excluded



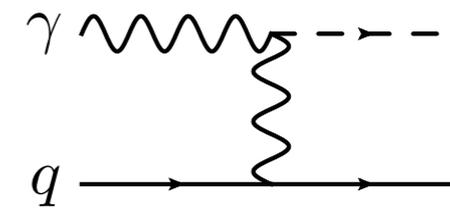
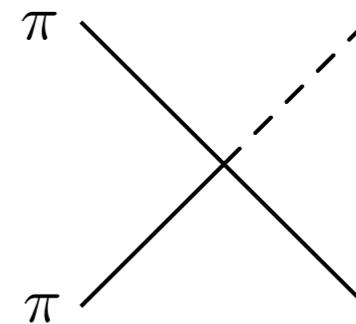
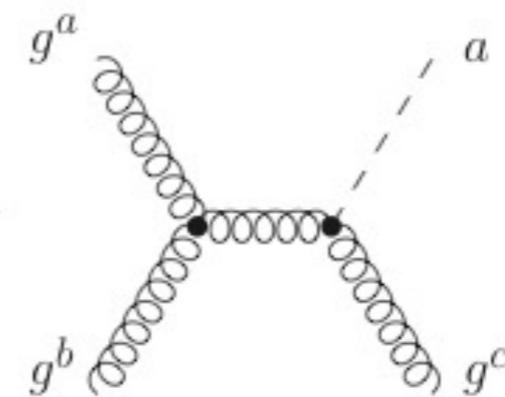
Axion dark matter: production mechanisms

Non thermally (cold)

$$\ddot{a} - 3H\dot{a} + m_a^2(T)a = 0$$

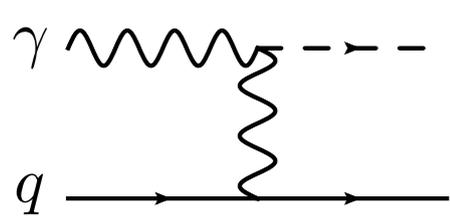


Thermally (hot)

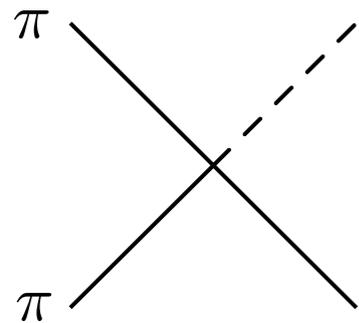


Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes

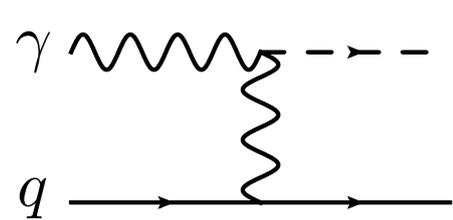


$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

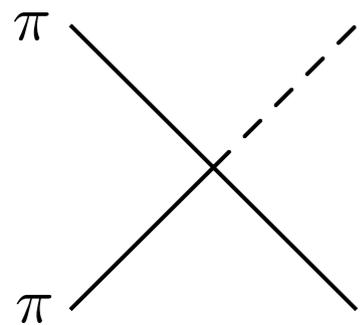


Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes



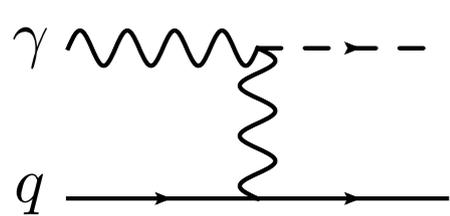
$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$



$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$

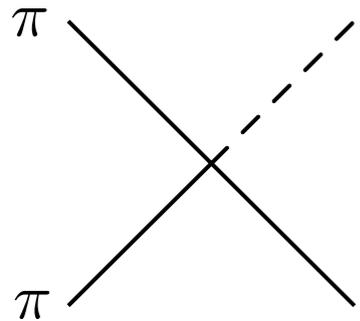
Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes



$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

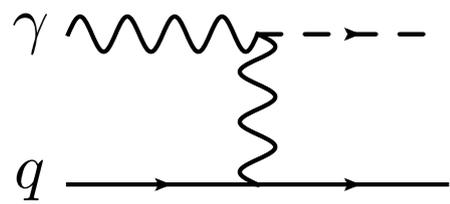
Such small mass axions behave as hot DM, which is not favored by observations.



$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$

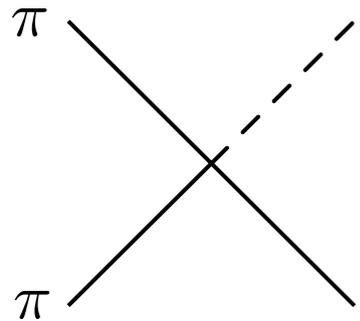
Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes

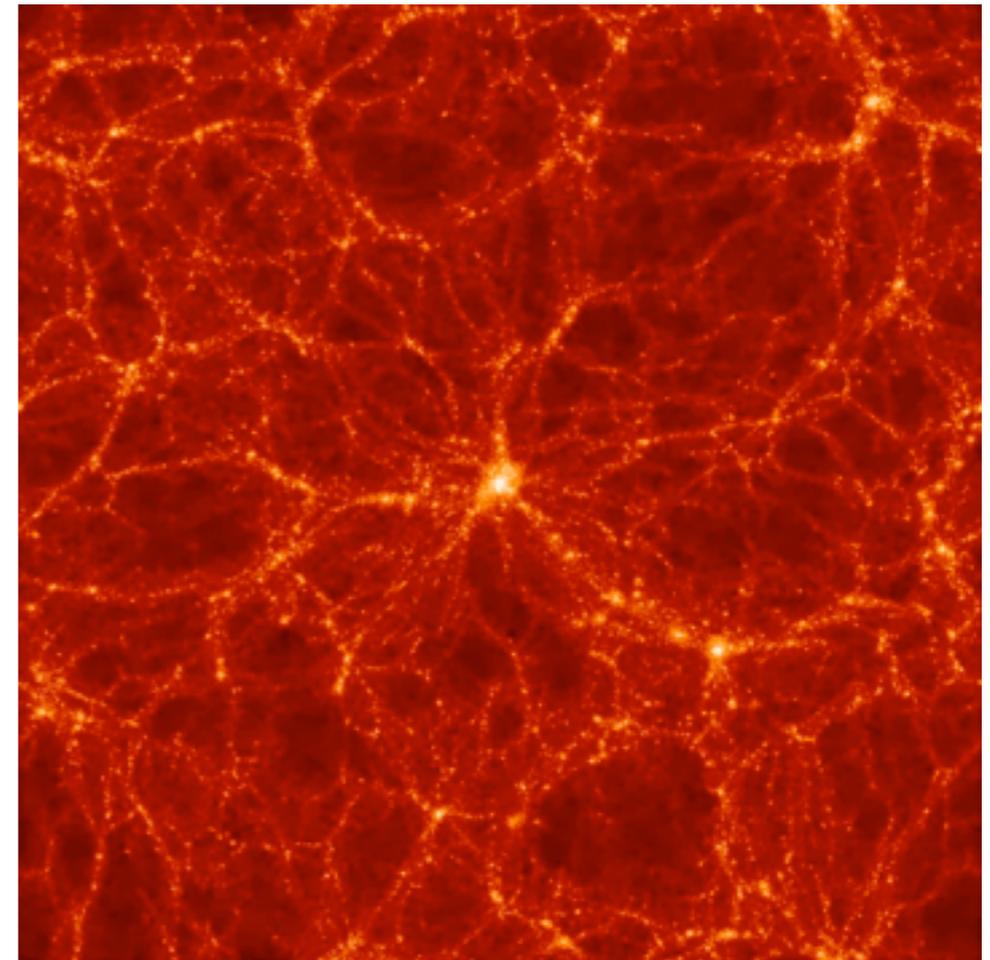


$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

Such small mass axions behave as hot DM, which is not favored by observations.

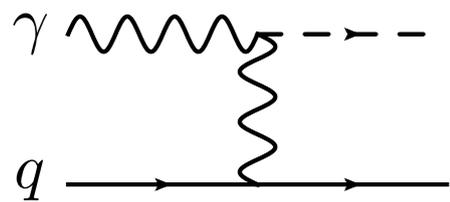


$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$



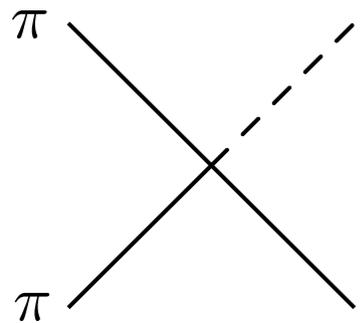
Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes

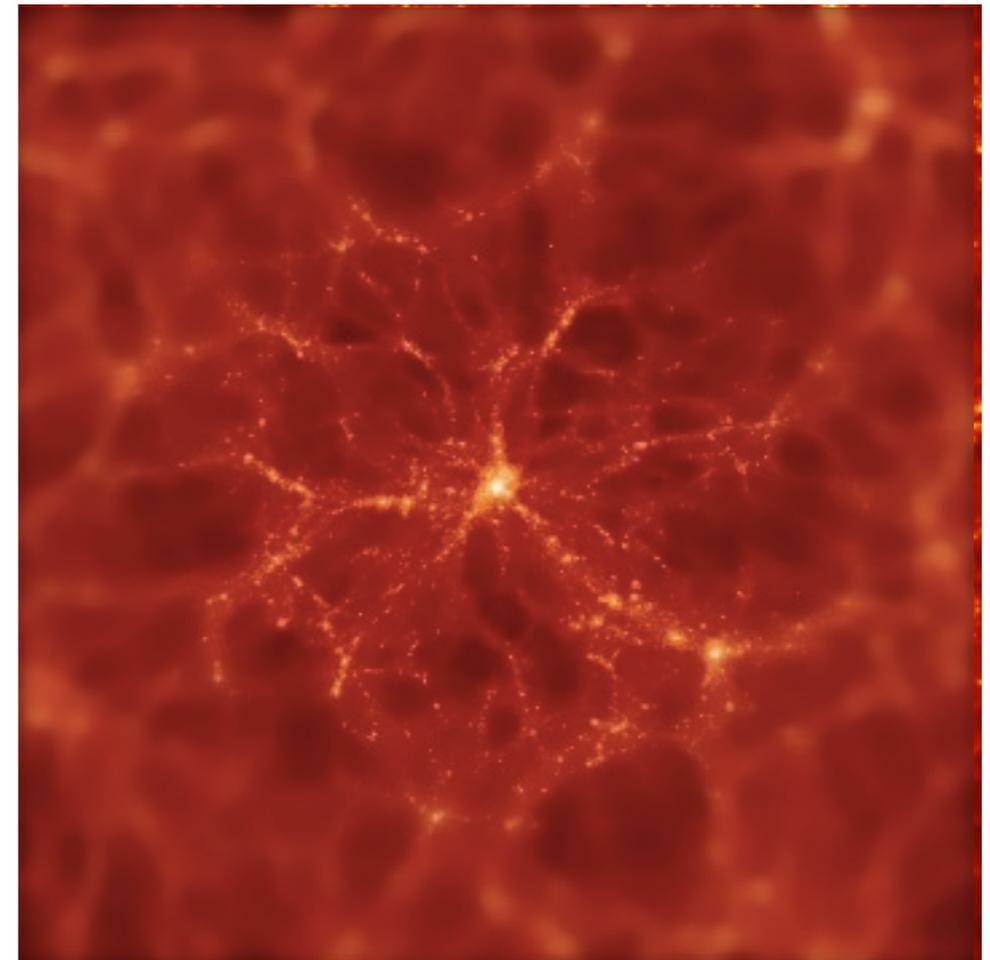


$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

Such small mass axions behave as hot DM, which is not favored by observations.

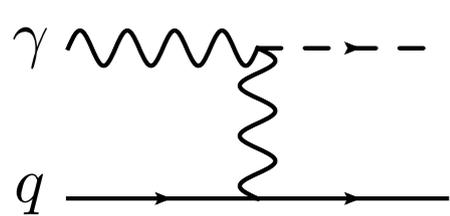


$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$



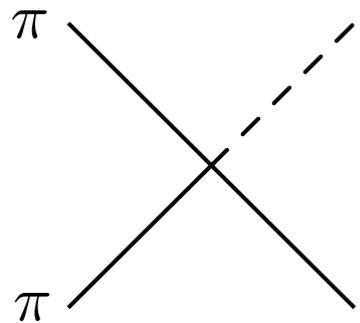
Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes



$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

Such small mass axions behave as hot DM, which is not favored by observations.

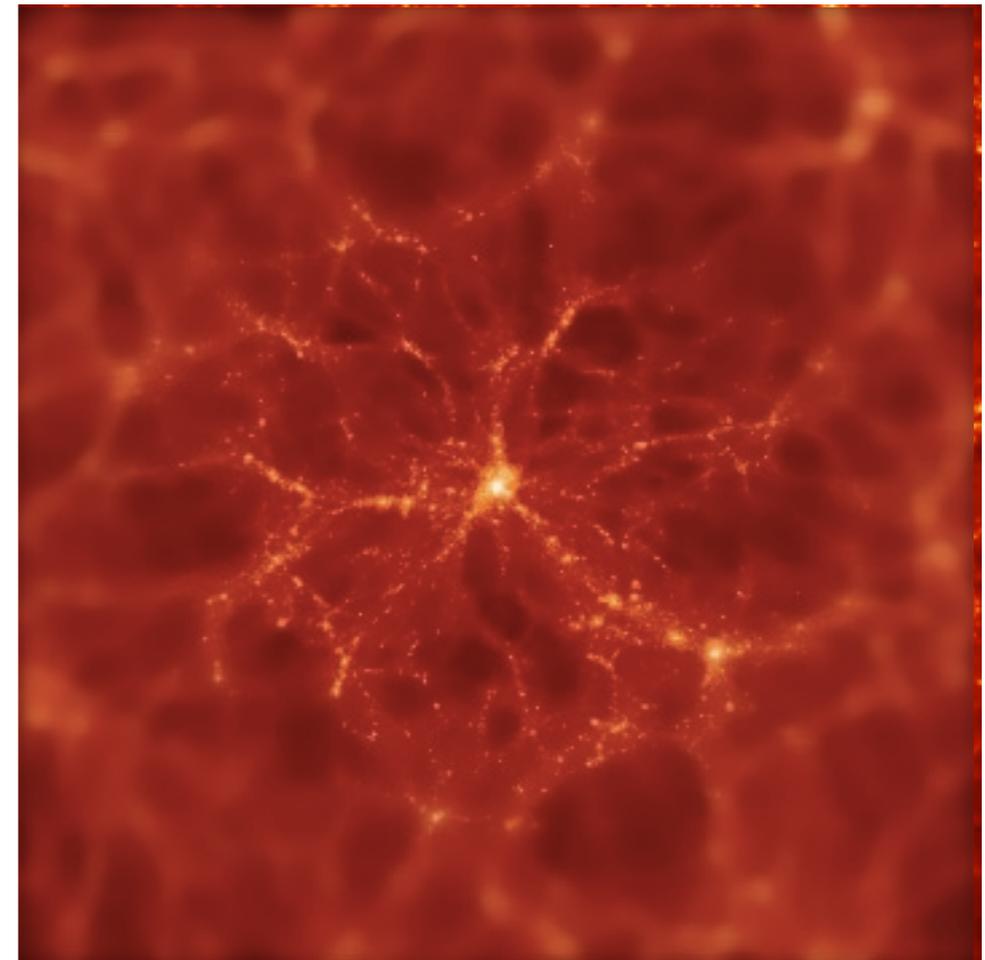


$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$

They should be a subdominant component of DM

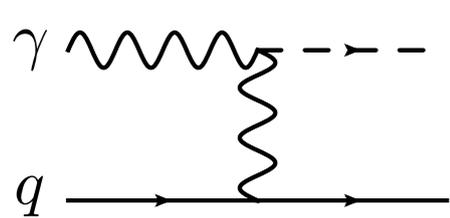
Hannestad et al. JCAP 1008

$$\frac{\Omega_{\text{hDM},a}}{\Omega_{\text{DM,obs}}} < 0.03 \quad (m_a < 0.72 \text{ eV})$$



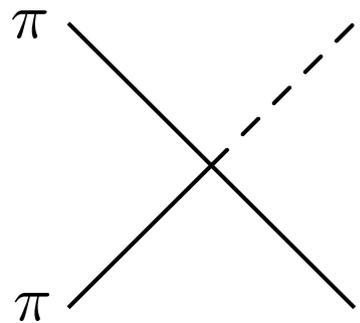
Axion hot Dark Matter (or Dark Radiation)

Axions are thermally produced in the early universe by a number of processes



$$\frac{\Gamma}{H} \propto \frac{T m_{\text{Pl}}}{f_a^2}$$

Such small mass axions behave as hot DM, which is not favored by observations.

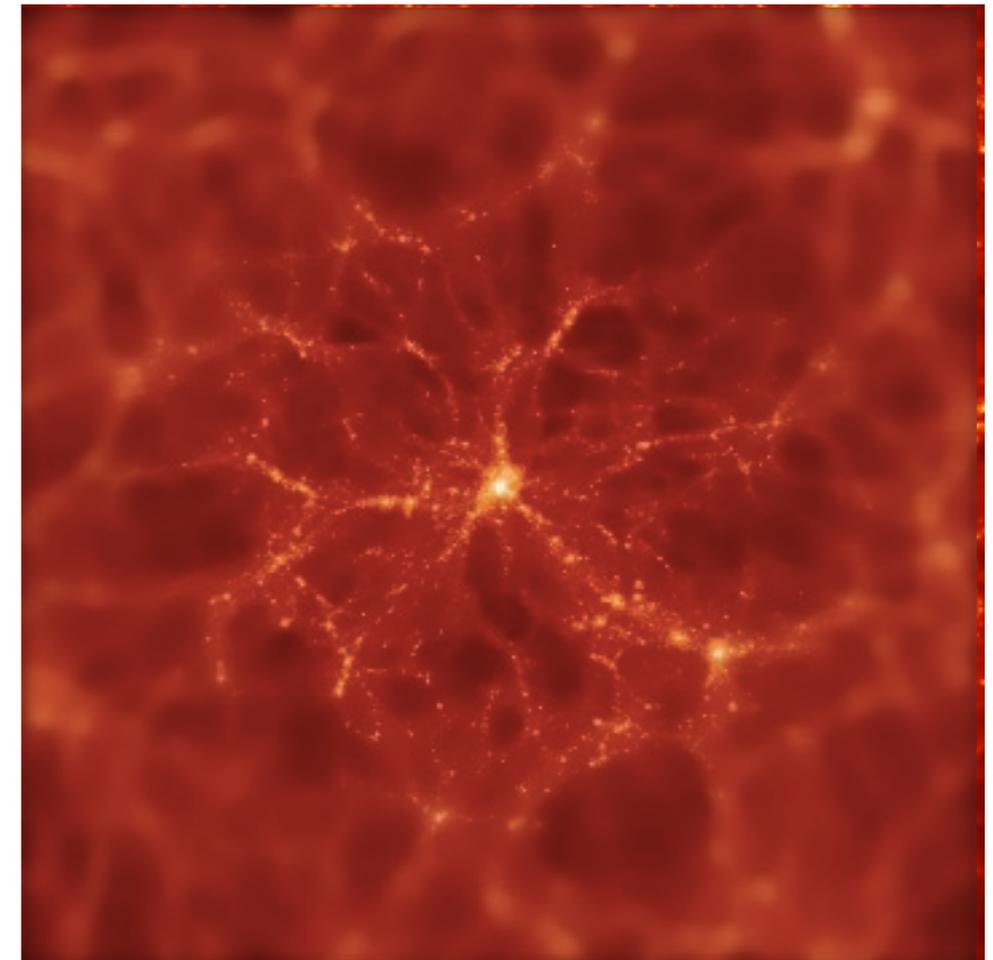


$$\frac{\Omega_{a,\text{hDM}}}{\Omega_{\text{obs}}} \sim \frac{m_a}{154 \text{ eV}} \mathcal{C}(g's)$$

They should be a subdominant component of DM

Hannestad et al. JCAP 1008

$$\frac{\Omega_{\text{hDM},a}}{\Omega_{\text{DM,obs}}} < 0.03 \quad (m_a < 0.72 \text{ eV})$$



Sub eV axions or ALPs behave as Dark Radiation but $N_{\text{eff}} < 3.9$
(There are however other DR production mechanisms)

Graf and Steffen arXiv:1208.2951,
 Takahashi arXiv:1201.4816, Sikivie PRL 108,

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)

Cosmic Strings

(Position space)

Domain Walls

$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

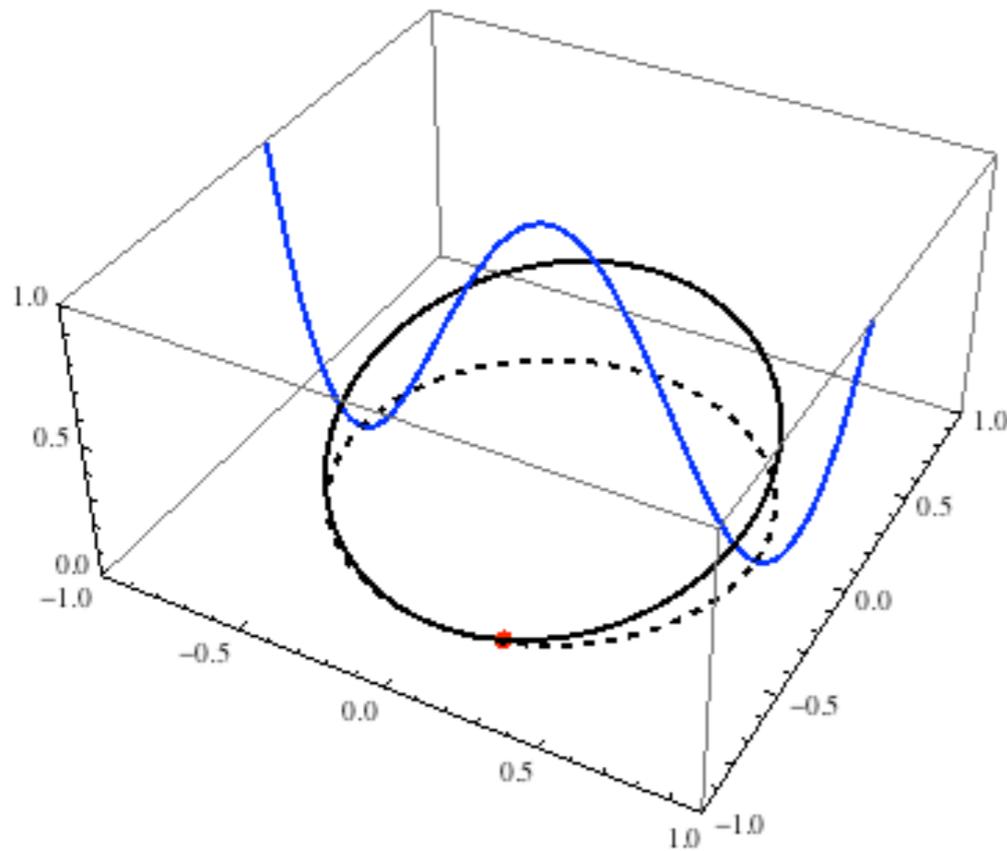
Realignment mechanism

(Field space)

Cosmic Strings

(Position space)

Domain Walls



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

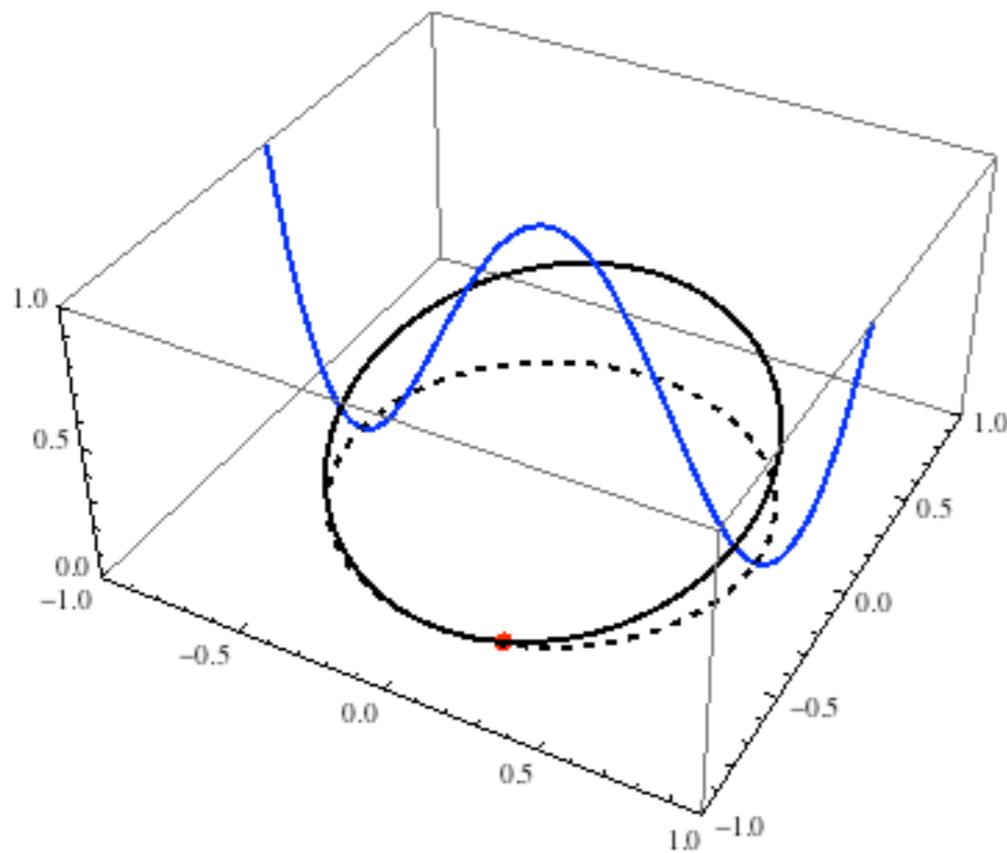
Realignment mechanism

(Field space)

Cosmic Strings

(Position space)

Domain Walls



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

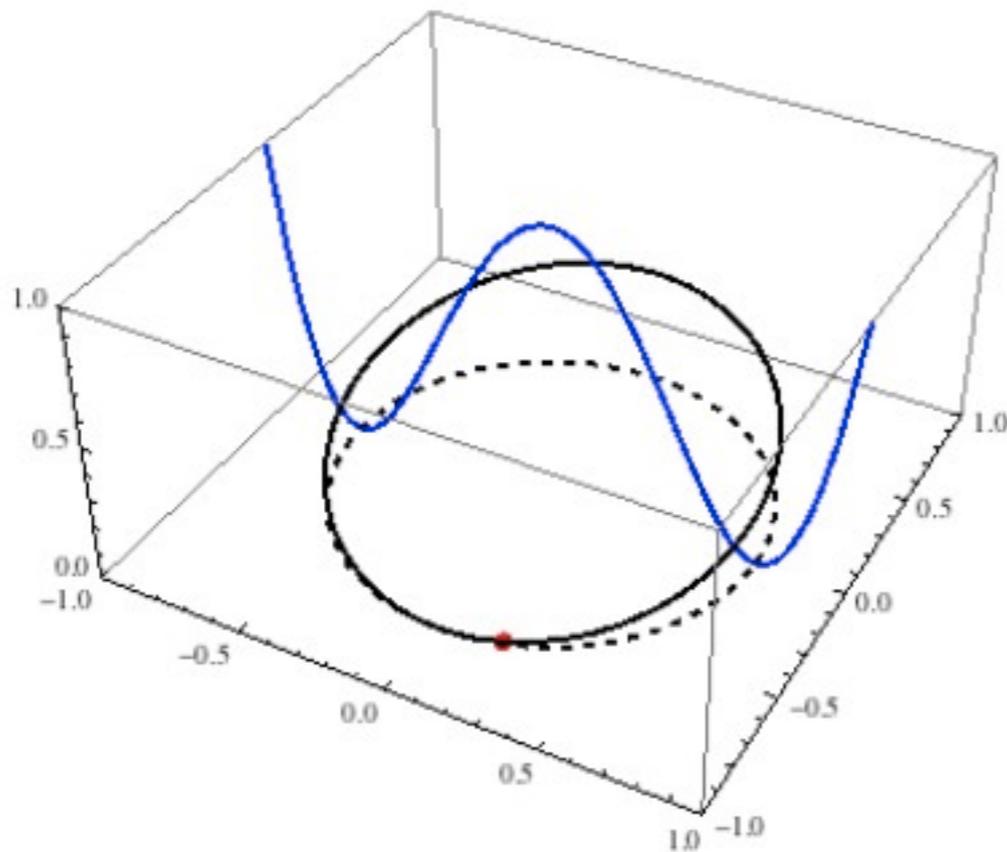
$$\frac{\Omega_{a,VR}}{\Omega_{\text{obs}}} \sim \left(\frac{40 \mu\text{eV}}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

(Position space)

($T > QCD$)

Domain Walls

($T < QCD$)

$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

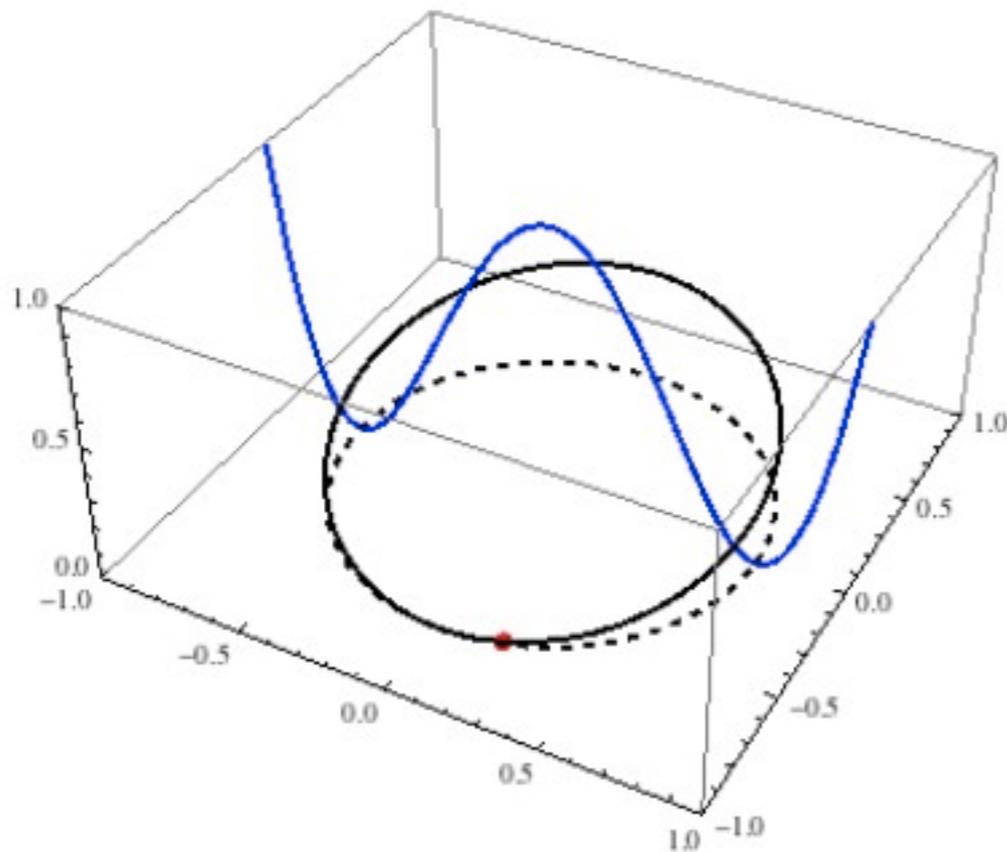
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)

$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

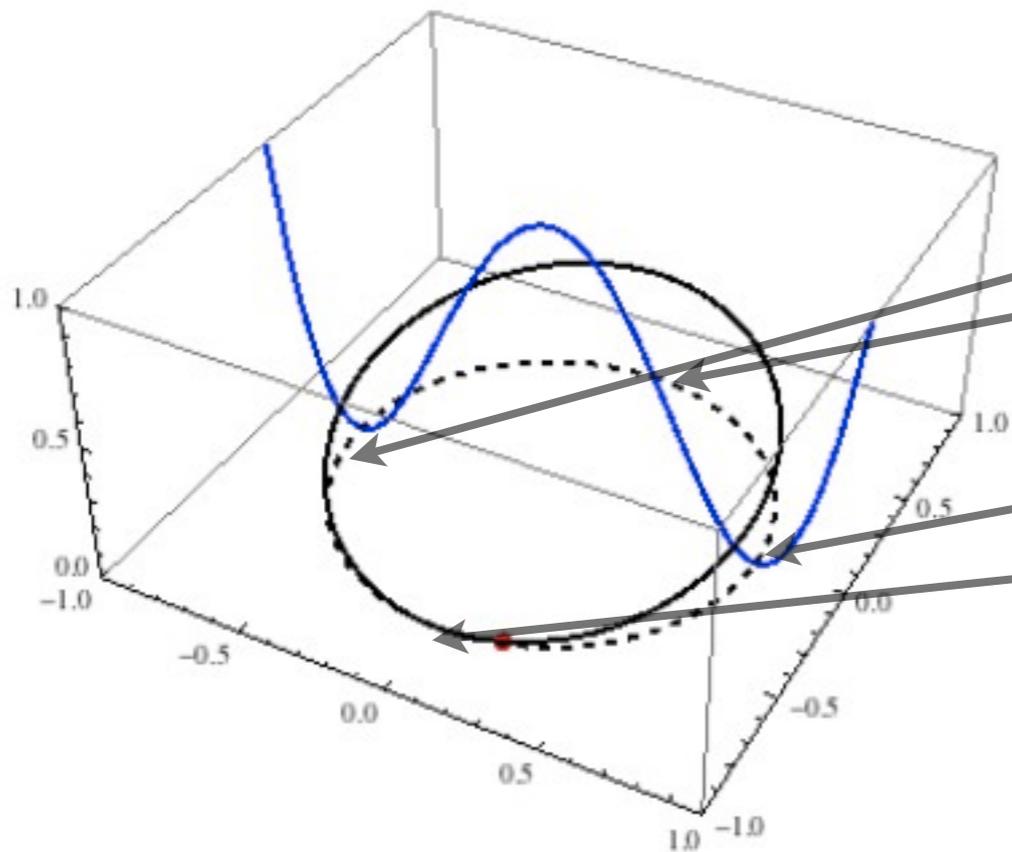
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)

$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

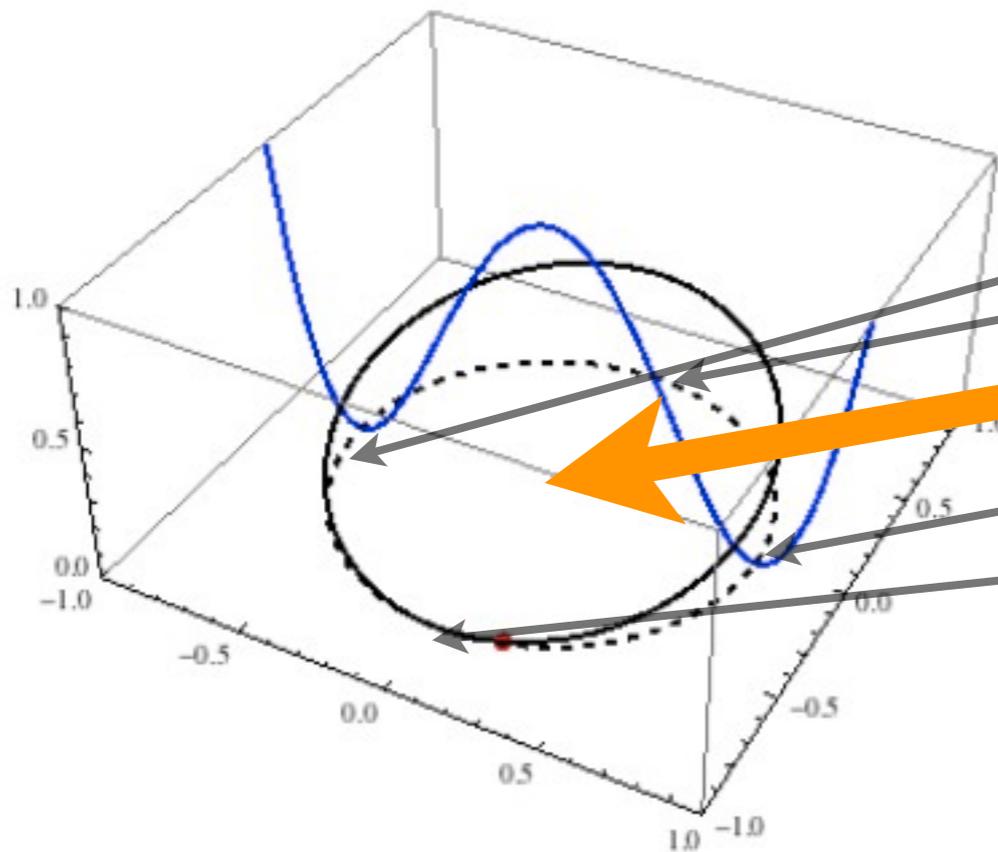
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)

$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

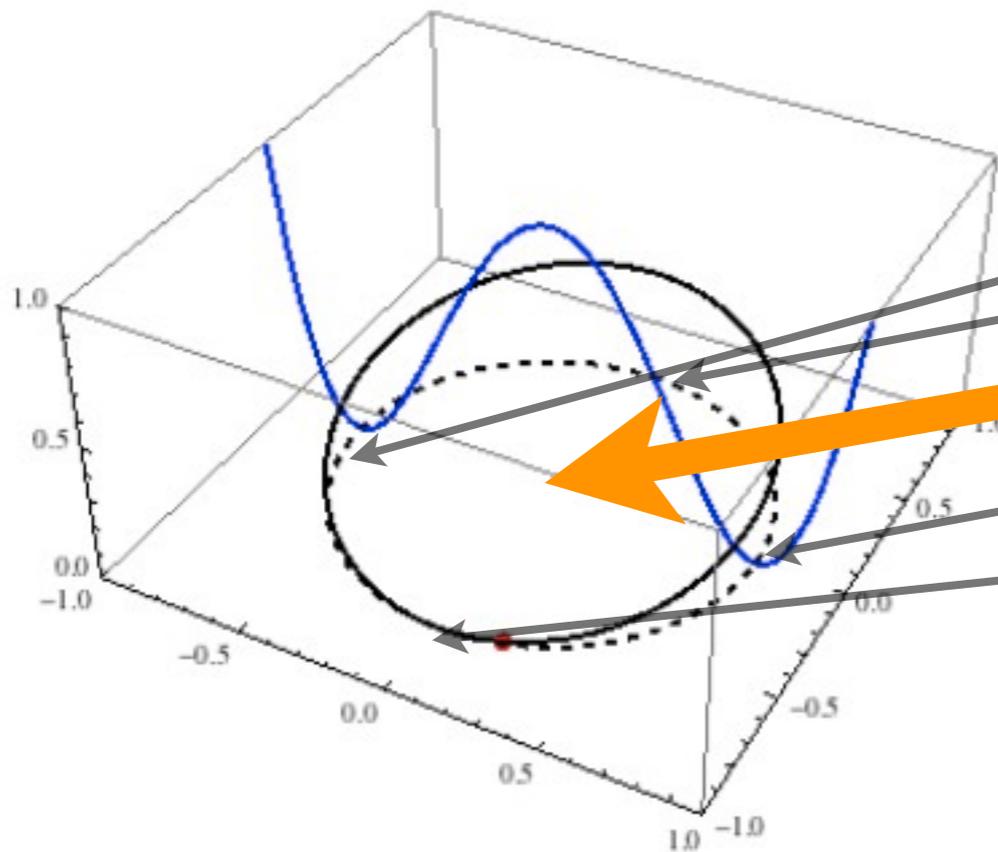
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

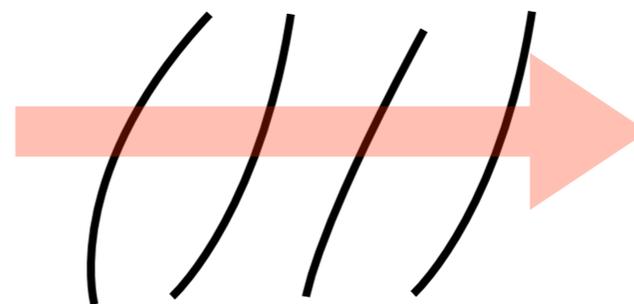
(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

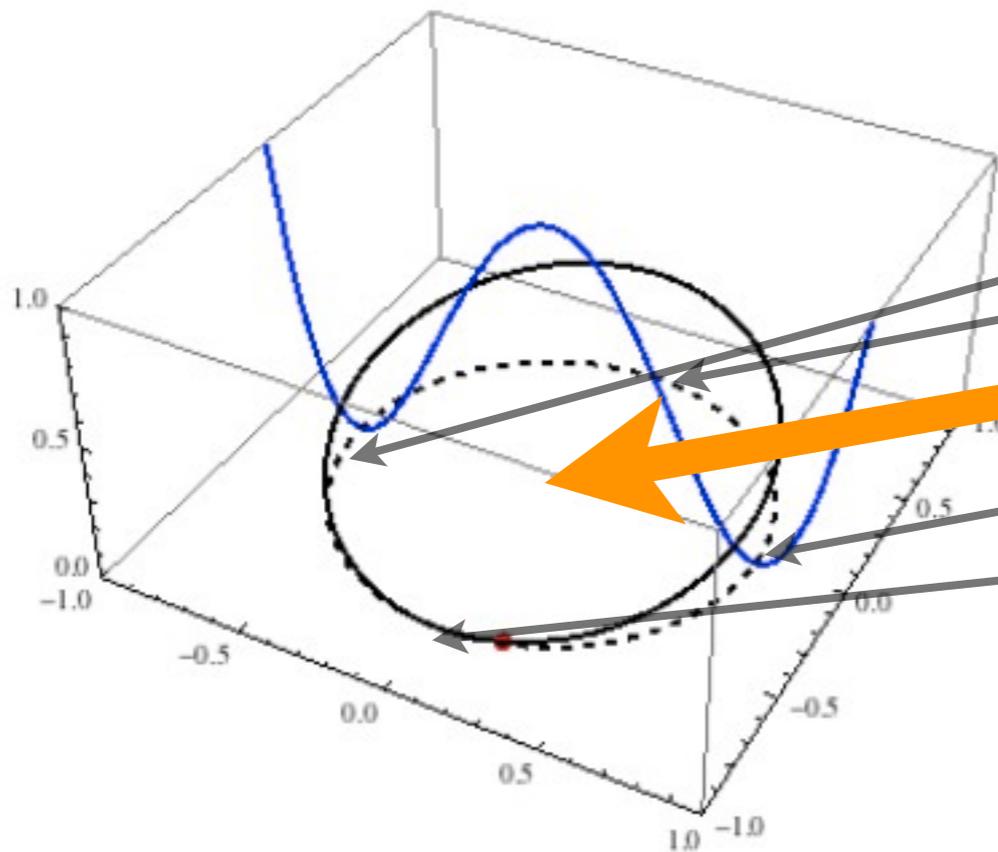
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

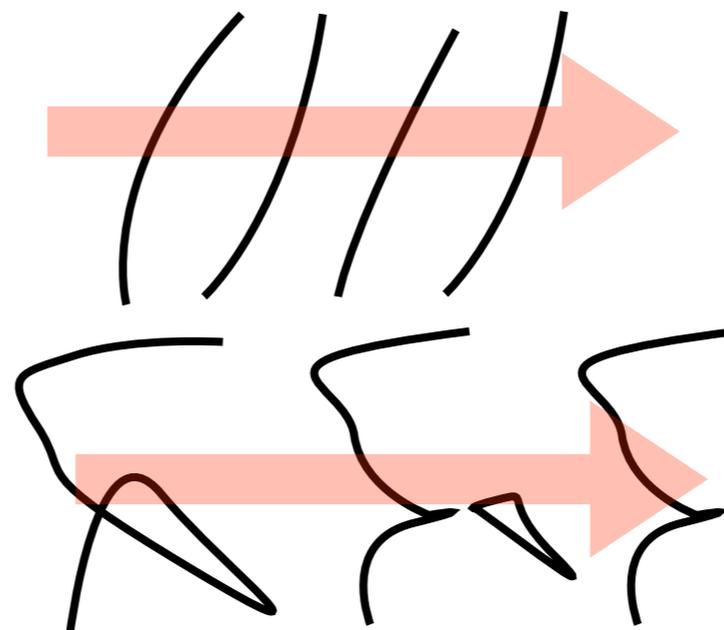
(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

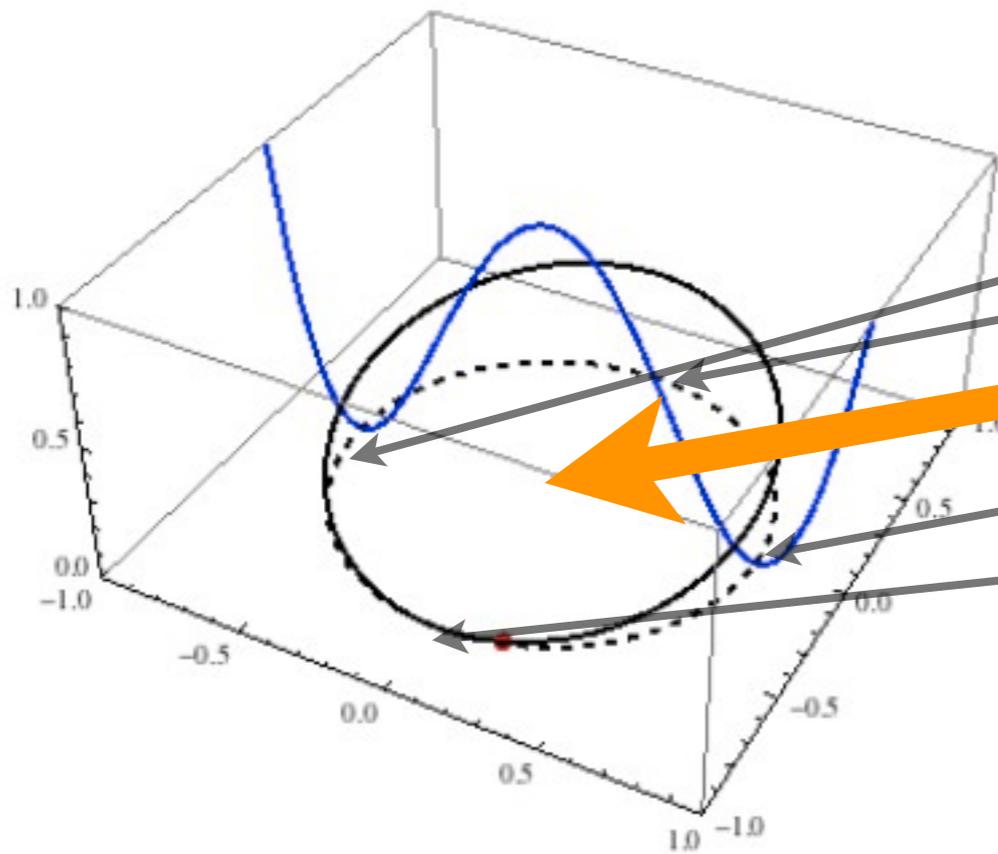
$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

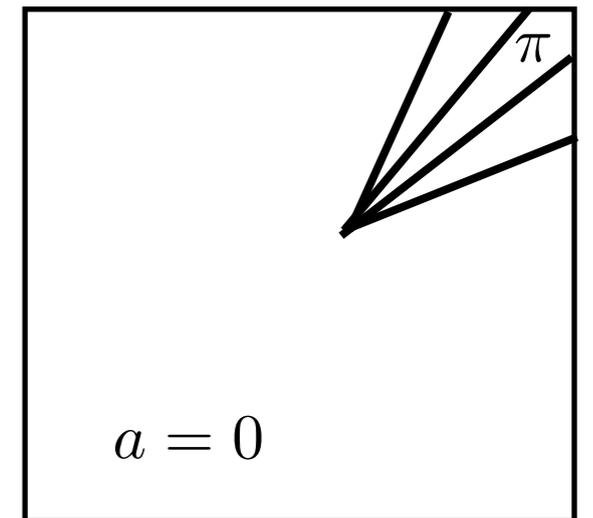
(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

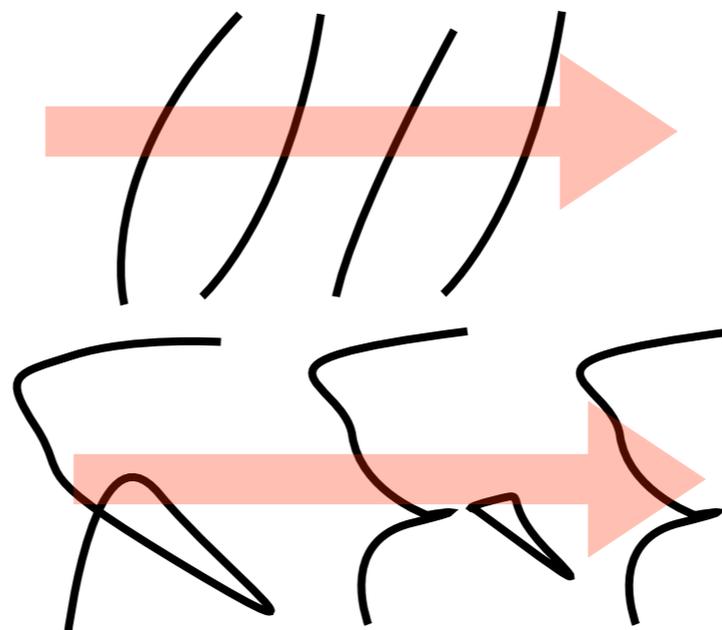
Domain Walls

($T < QCD$)



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40 \mu eV}{m_a} \right)^{1.184}$$

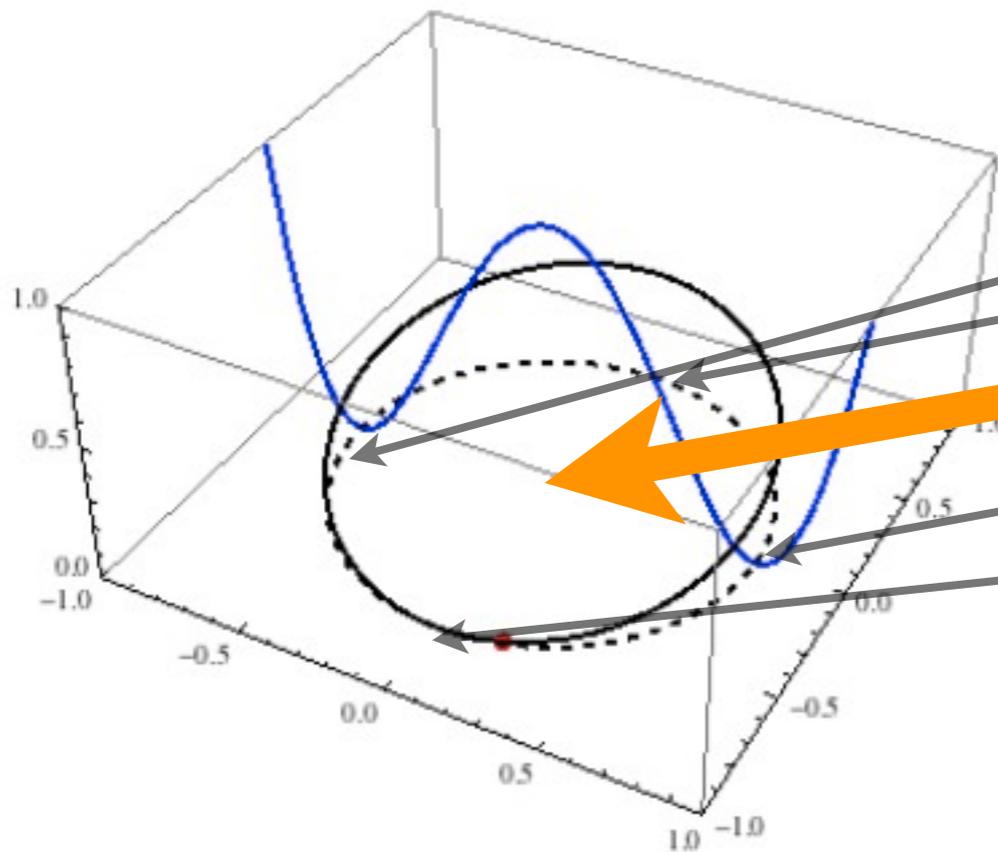


Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

(Position space)

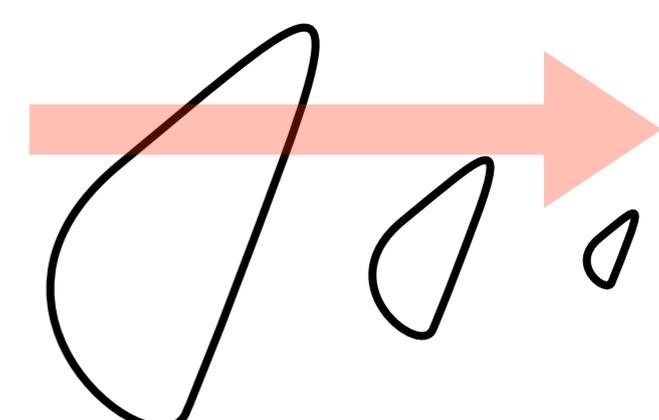
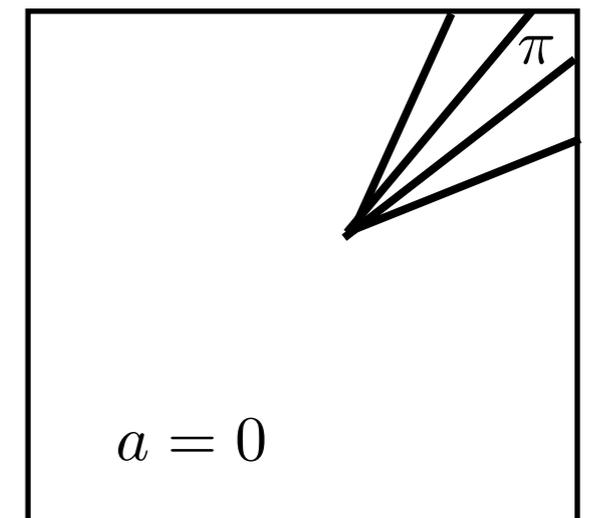
($T > \text{QCD}$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$



Domain Walls

($T < \text{QCD}$)



$$\Phi(x) = \rho(x) e^{i \frac{a(x)}{f_a}}$$

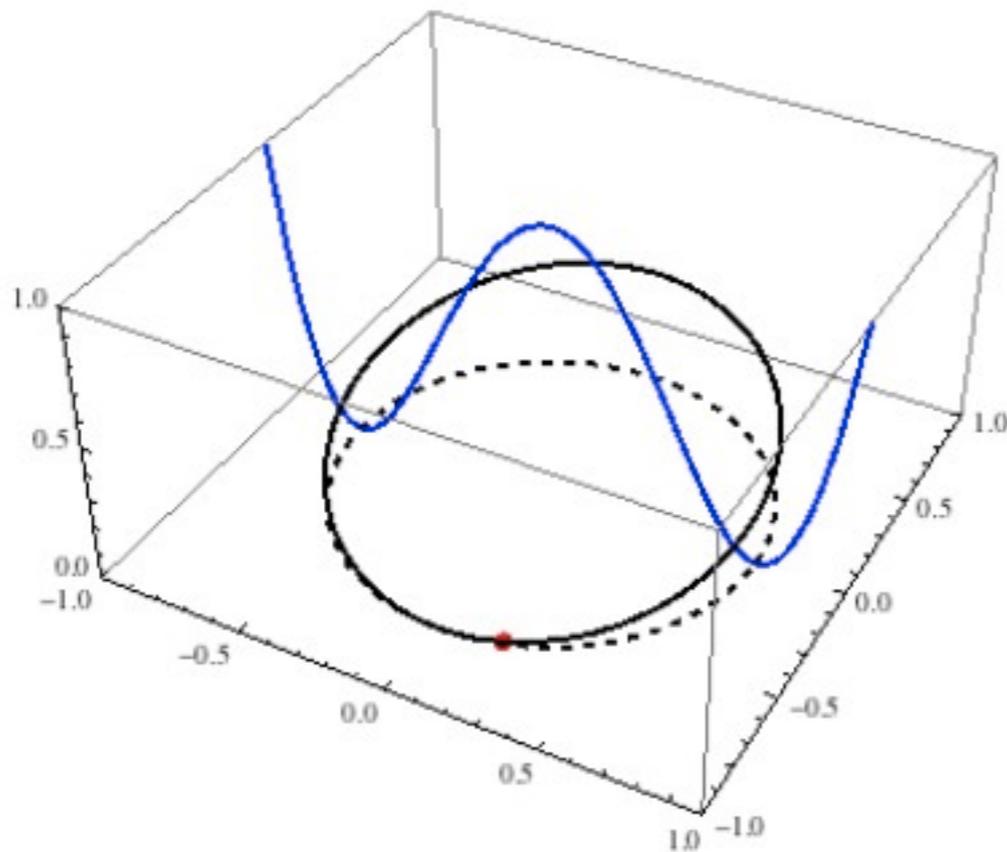
$$\frac{\Omega_{a,VR}}{\Omega_{\text{obs}}} \sim \left(\frac{40 \mu\text{eV}}{m_a} \right)^{1.184}$$

Axion cold Dark Matter

Axions (and ALPs) are produced non-thermally by three mechanisms

Realignment mechanism

(Field space)



Cosmic Strings

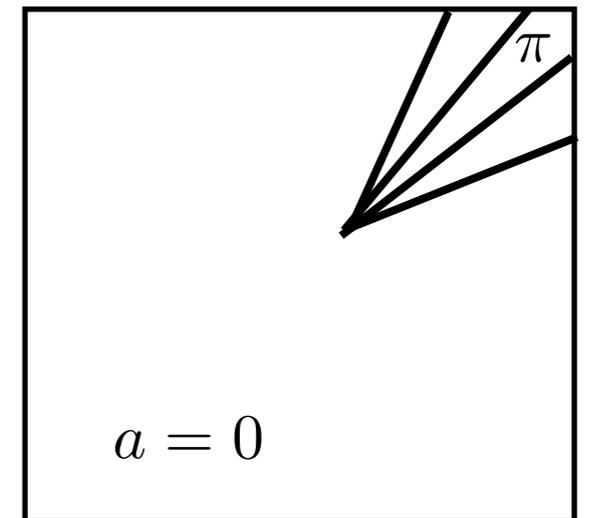
(Position space)

($T > QCD$)

$a = \frac{3\pi}{2}$	$a = \pi$
$a = 0$	$a = \frac{\pi}{2}$

Domain Walls

($T < QCD$)



$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \left(\frac{40\mu eV}{m_a} \right)^{1.184}$$

$$\frac{\Omega_{a,DW+ST}}{\Omega_{obs}} \left\{ \begin{array}{l} \sim \left(\frac{40\mu eV}{m_a} \right)^{1.184} \\ \sim \left(\frac{400\mu eV}{m_a} \right)^{1.184} \end{array} \right.$$

Sikivie, Harari et al.

Shellard, Davis et al.
Kawasaki, Hiramatsu et al.

Understanding the behavior $\Omega_{a,\text{cDM}} \propto 1/m_a$

E.o.m. $\ddot{a} + 3H\dot{a} + m_a^2 a = \dots \sim 0$

Understanding the behavior $\Omega_{a,\text{cDM}} \propto 1/m_a$

E.o.m. $\ddot{a} + 3H\dot{a} + m_a^2 a = \dots \sim 0$

$$H \gg m_a$$

$$\dot{a} \sim 0$$

Understanding the behavior $\Omega_{a,\text{cDM}} \propto 1/m_a$

E.o.m. $\ddot{a} + 3H\dot{a} + m_a^2 a = \dots \sim 0$

$$H \gg m_a$$

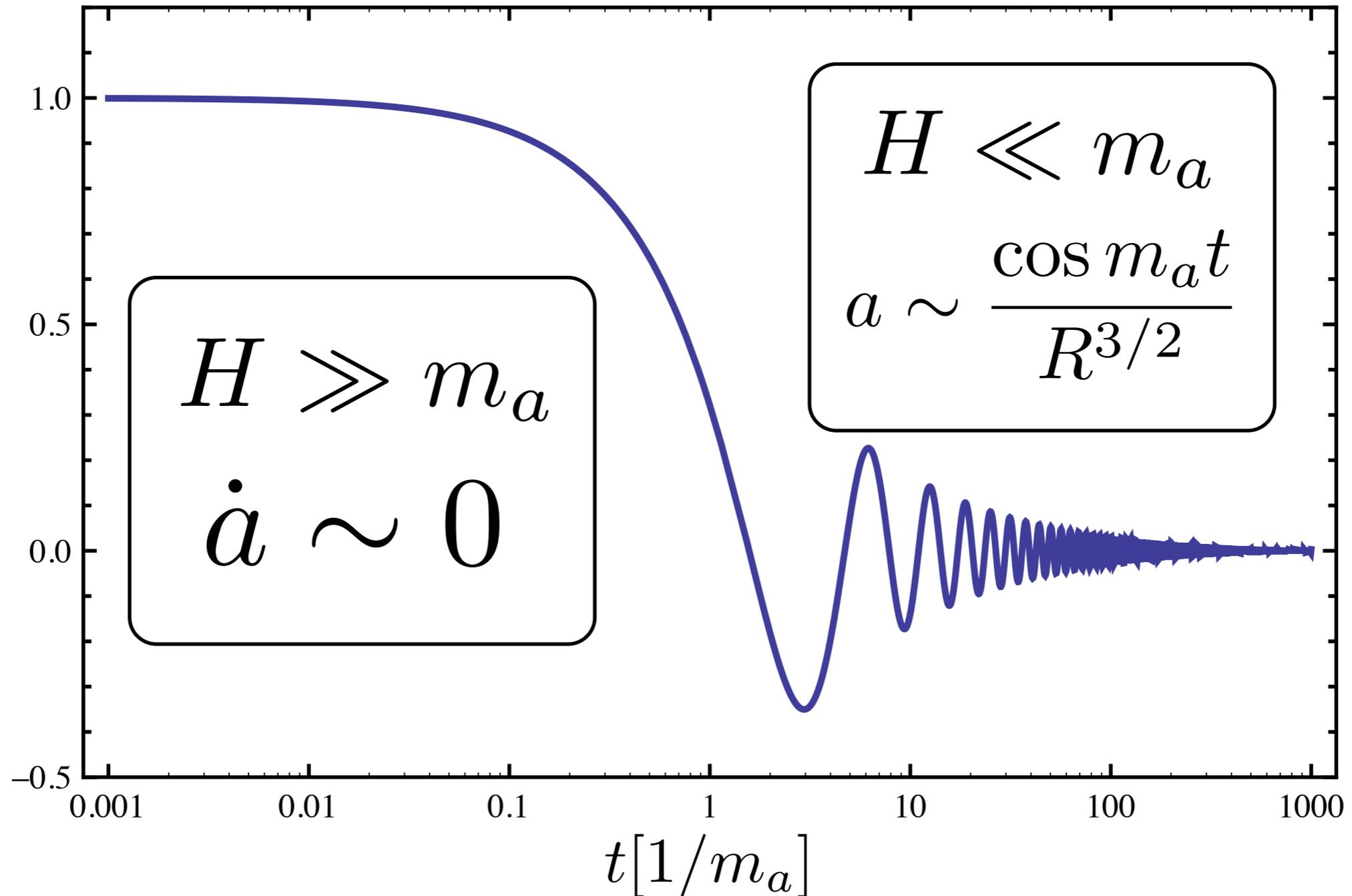
$$\dot{a} \sim 0$$

$$H \ll m_a$$

$$a \sim \frac{\cos m_a t}{R^{3/2}}$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

E.o.m. $\ddot{a} + 3H\dot{a} + m_a^2 a = \dots \sim 0$



Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

$$a_1 \sim f_a$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

$$a_1 \sim f_a$$

$$\Omega_{a,cDM} \propto \rho_a(t_0) \propto \sqrt{m_a} f_a^2 \propto m_a^{-3/2}$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

$$a_1 \sim f_a$$

$$f_a \propto 1/m_a$$

$$\Omega_{a,cDM} \propto \rho_a(t_0) \propto \sqrt{m_a} f_a^2 \propto m_a^{-3/2}$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

$$a_1 \sim f_a$$

$$f_a \propto 1/m_a$$

$$\Omega_{a,cDM} \propto \rho_a(t_0) \propto \sqrt{m_a} f_a^2 \propto m_a^{-3/2}$$

Understanding the behavior $\Omega_{a,cDM} \propto 1/m_a$

comoving axion number conserved

$$\rho_a = \frac{1}{2}(\dot{a})^2 + \frac{1}{2}m_a^2 a^2 \longrightarrow N = \frac{\rho_a R^3}{m_a} = \text{ct.} = \frac{1}{2}m_a R_1^3 a_1^2$$

$$\rho_a(t_0) = m_a \frac{N}{R_0^3} = \frac{1}{2}m_a^2 a_1^2 \left(\frac{R_1}{R_0}\right)^3$$

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{m_a m_{\text{Pl}}}}\right)^3 \propto m_a^{-3/2}$$

$$a_1 \sim f_a$$

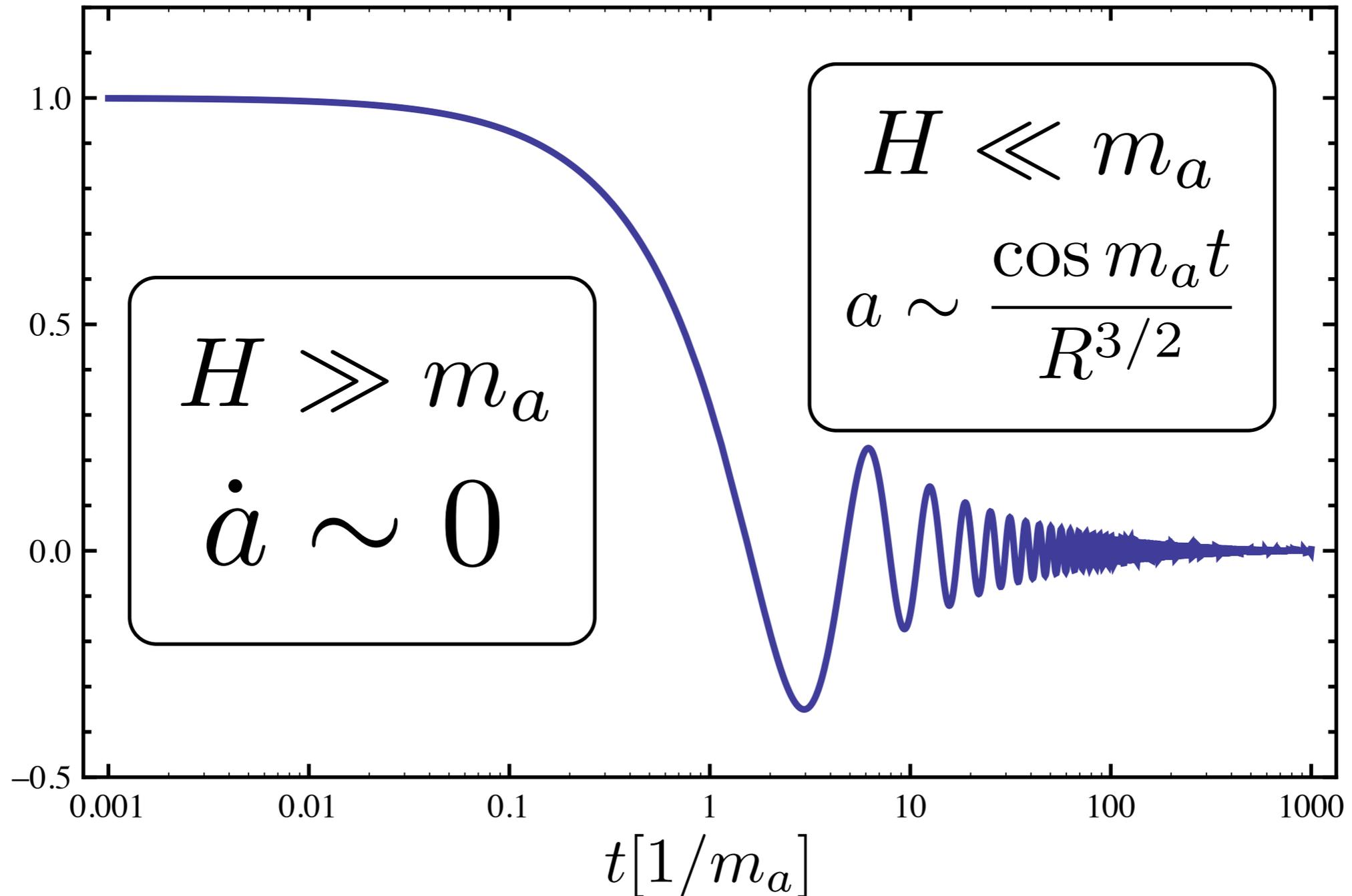
$$f_a \propto 1/m_a$$

$$\Omega_{a,cDM} \propto \rho_a(t_0) \propto \sqrt{m_a} f_a^2$$

$$\propto m_a^{-3/2}$$

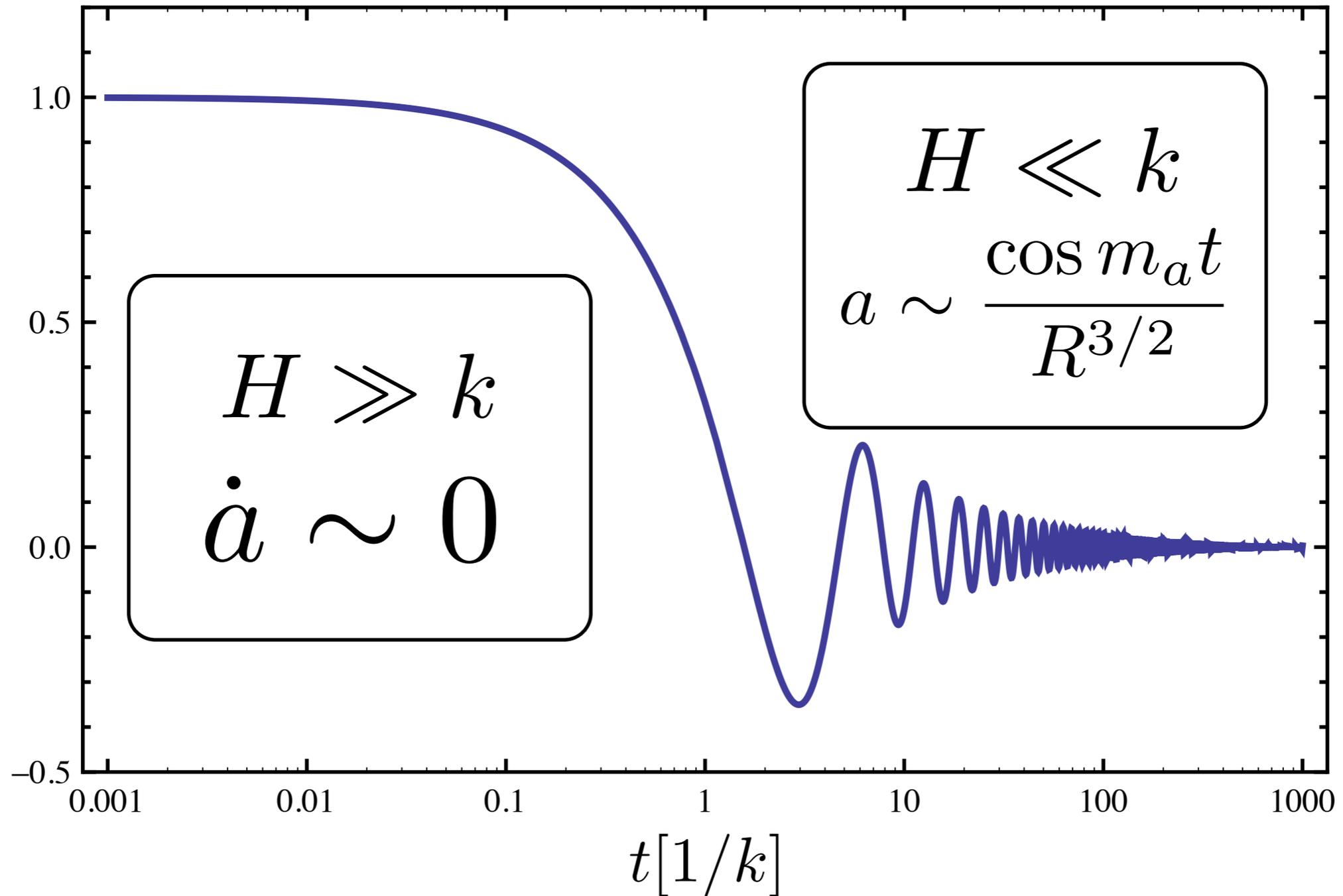
Why so cold?

E.o.m. $\ddot{a} + 3H\dot{a} + m_a^2 a = \dots \sim 0$



Why so cold?

E.o.m. $\ddot{a} + 3H\dot{a} + (m_a^2 + k^2)a = \dots \sim 0$

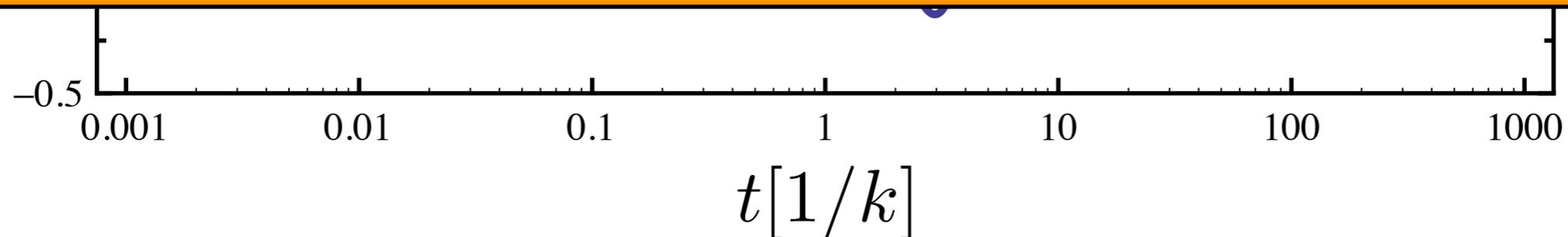


Why so cold?

E.o.m. $\ddot{a} + 3H\dot{a} + (m_a^2 + k^2)a = \dots \sim 0$

**Modes inside the horizon decay before!
and therefore ... more!**

$$\left(\frac{R_1}{R_0}\right)^3 \sim \left(\frac{T_0}{T_1}\right)^3 \sim \left(\frac{T_0}{\sqrt{H_1 m_{\text{Pl}}}}\right)^3 \sim \left(\frac{T_0}{\sqrt{k m_{\text{Pl}}}}\right)^3 \propto k^{-3/2}$$

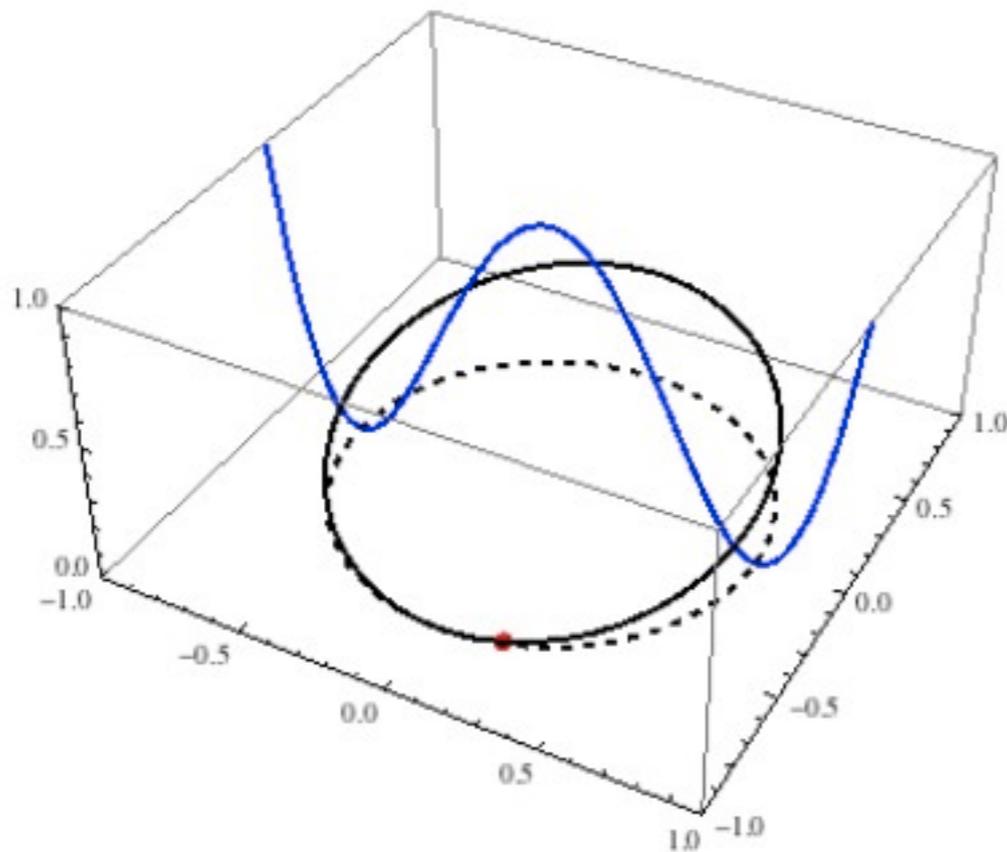


Axion cold Dark Matter*

If the Peccei-Quinn phase transition happens before inflation ...

Realignment mechanism

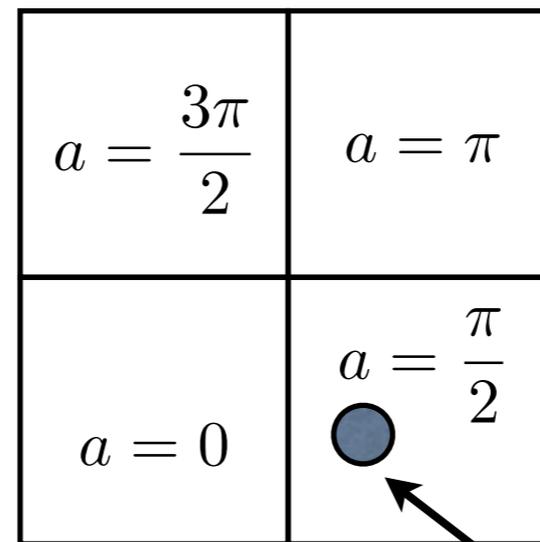
(Field space)



Cosmic Strings

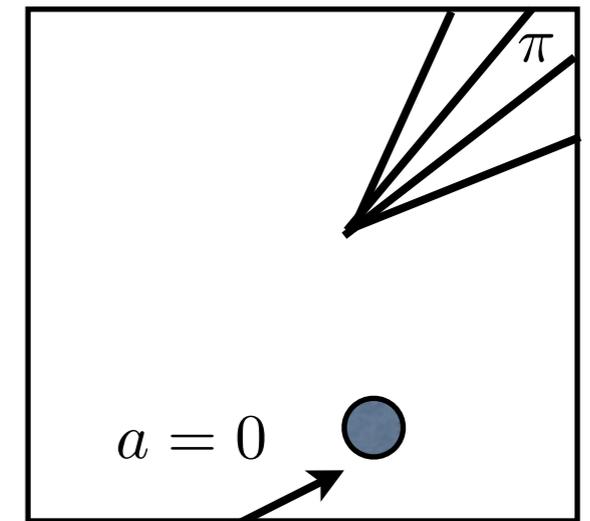
(Position space)

($T > QCD$)



Domain Walls

($T < QCD$)

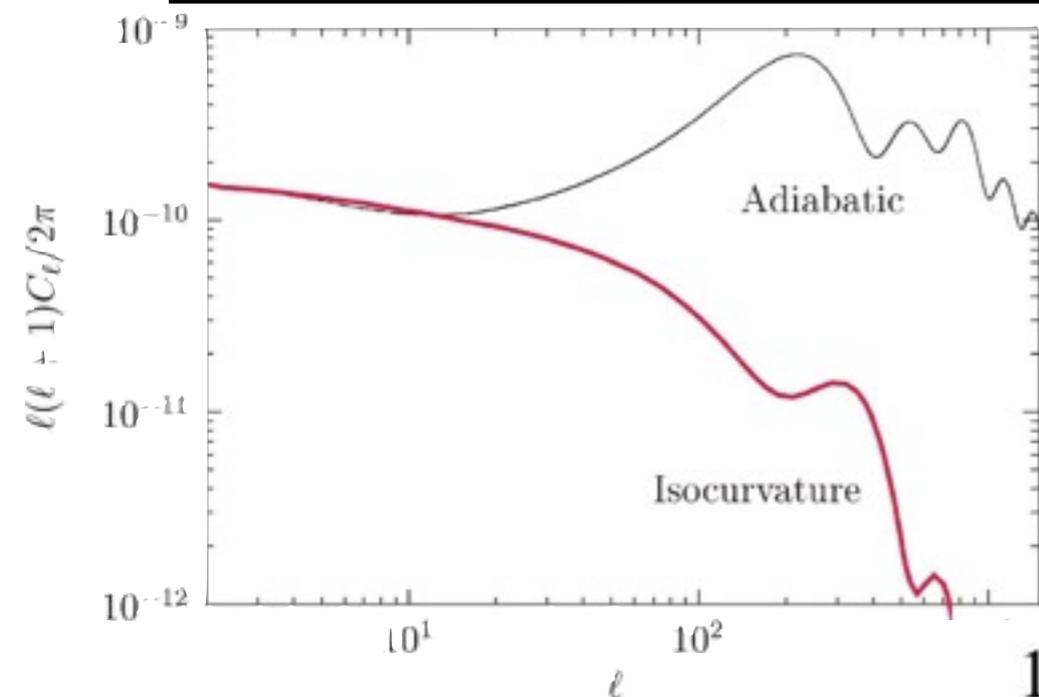


Size of our universe after inflation fits inside one of these domains

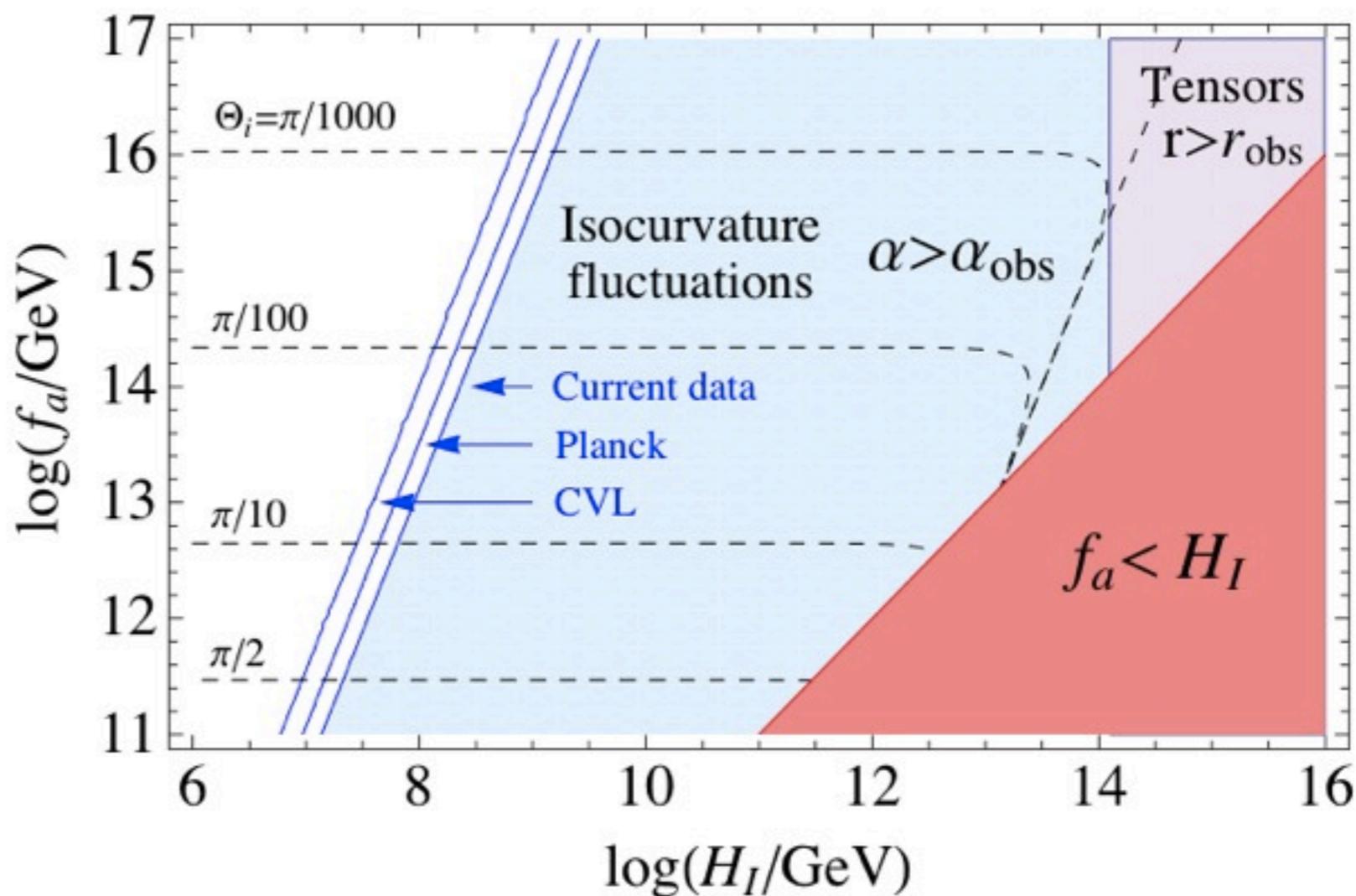
- CSs and DWs are diluted by expansion
- Whole universe has 1 initial value for a

$$\frac{\Omega_{a,VR}}{\Omega_{obs}} \sim \theta_0^2 \left(\frac{12\mu eV}{m_a} \right)^{1.184}$$

And they imprint ISOCURVATURE perturbations

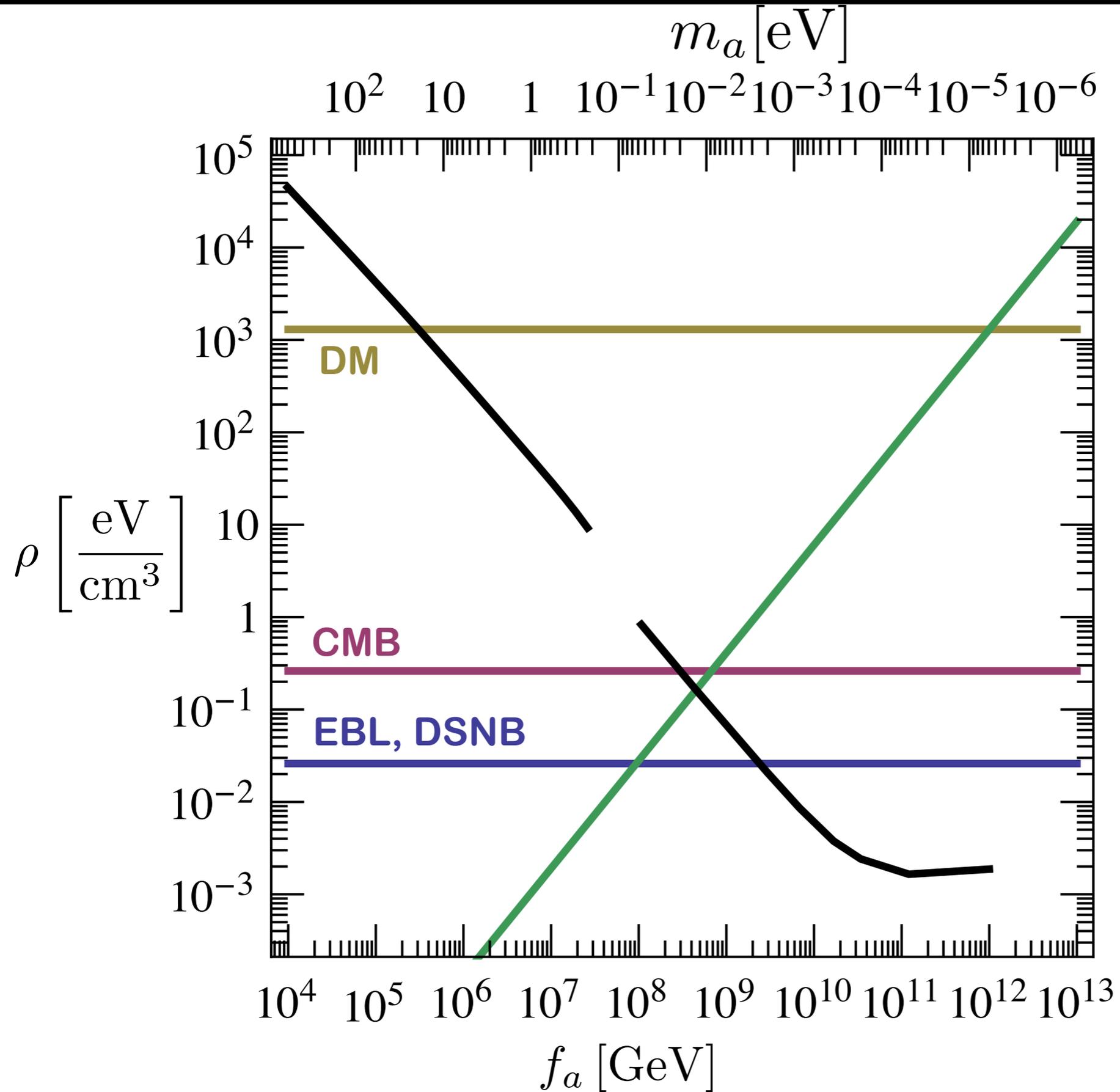


but this depends on H during inflation...

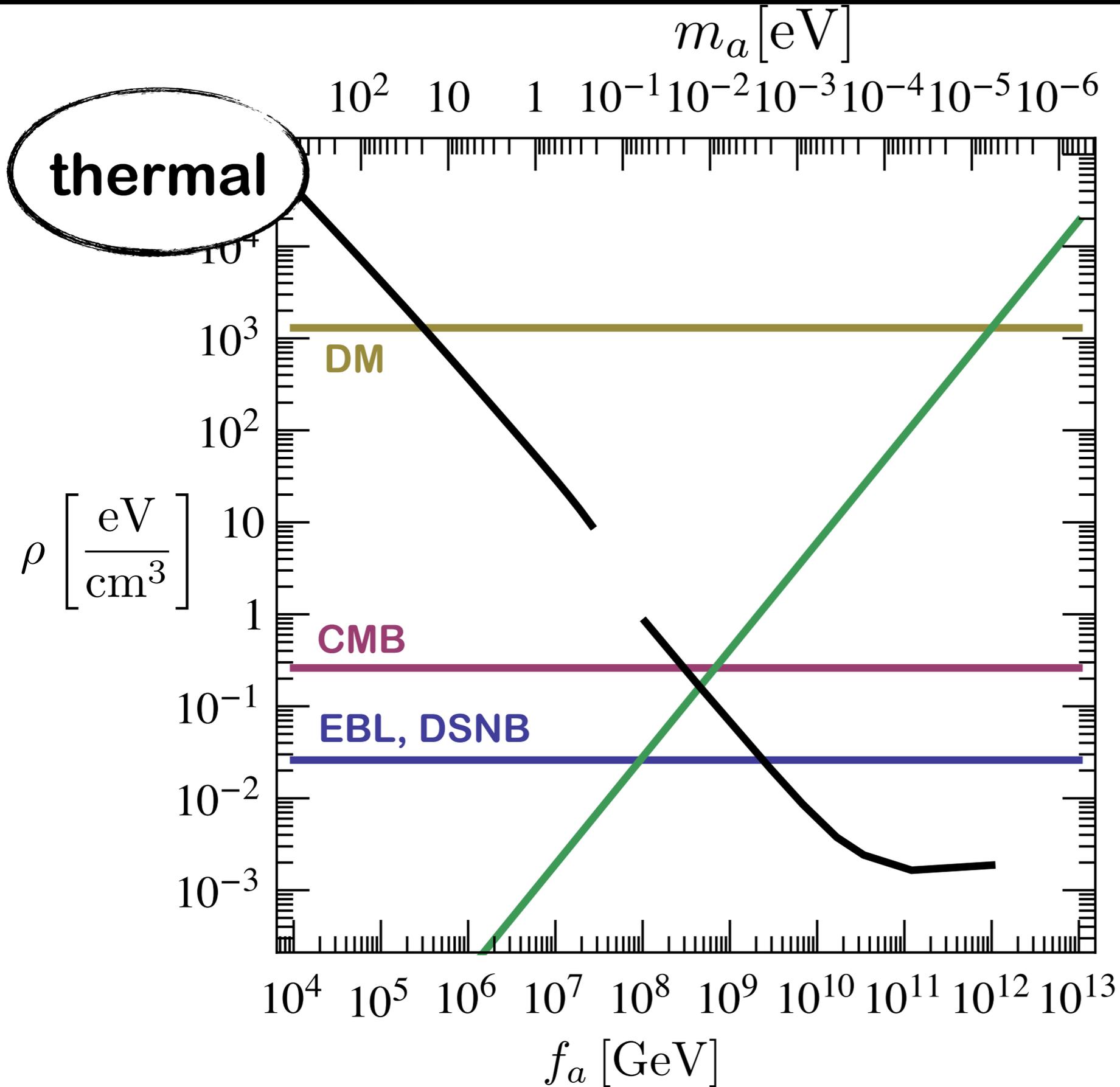


Hamman, Hannestad, Raffelt and Wong JCAP (2009)

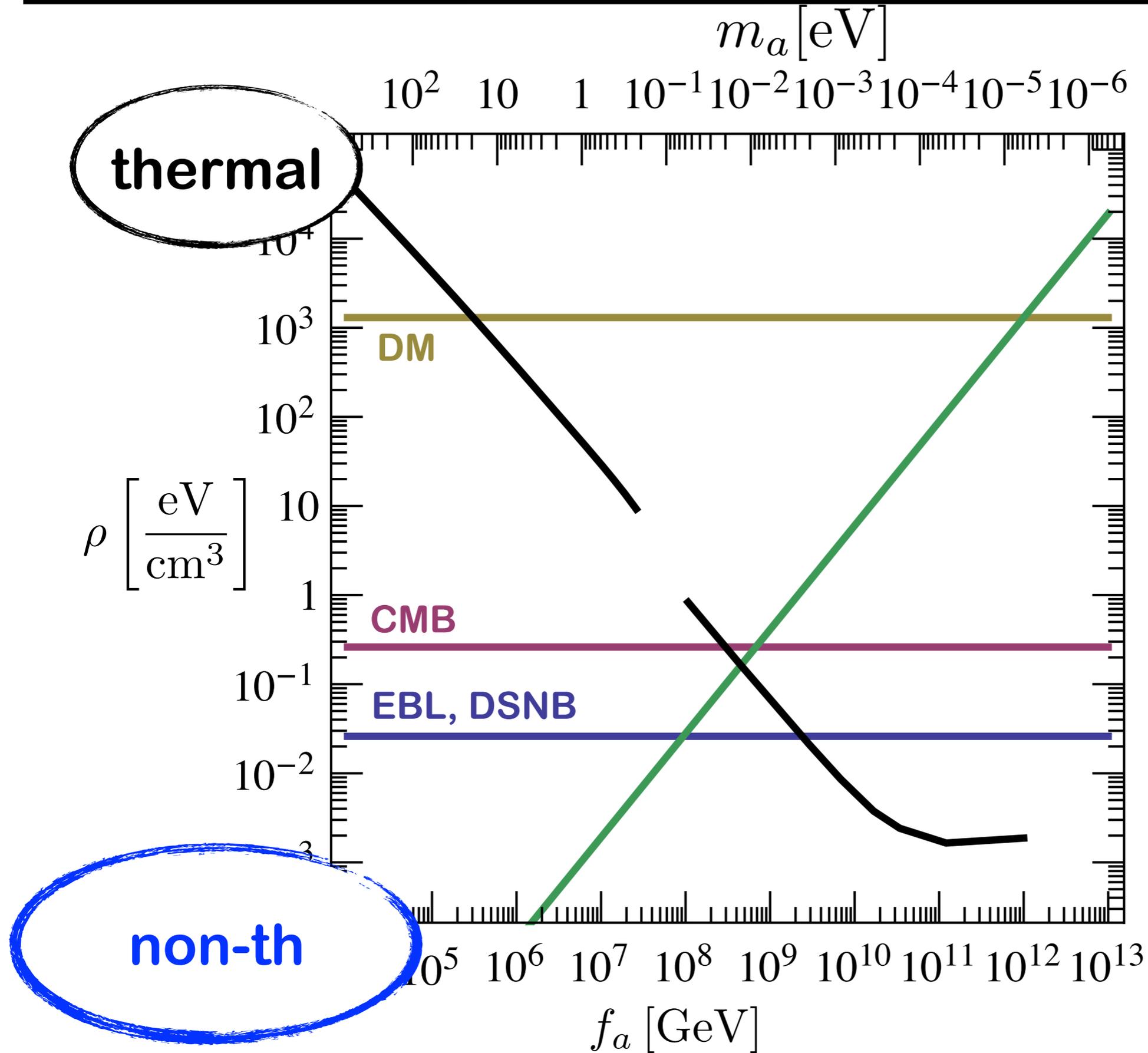
Axion energy density today



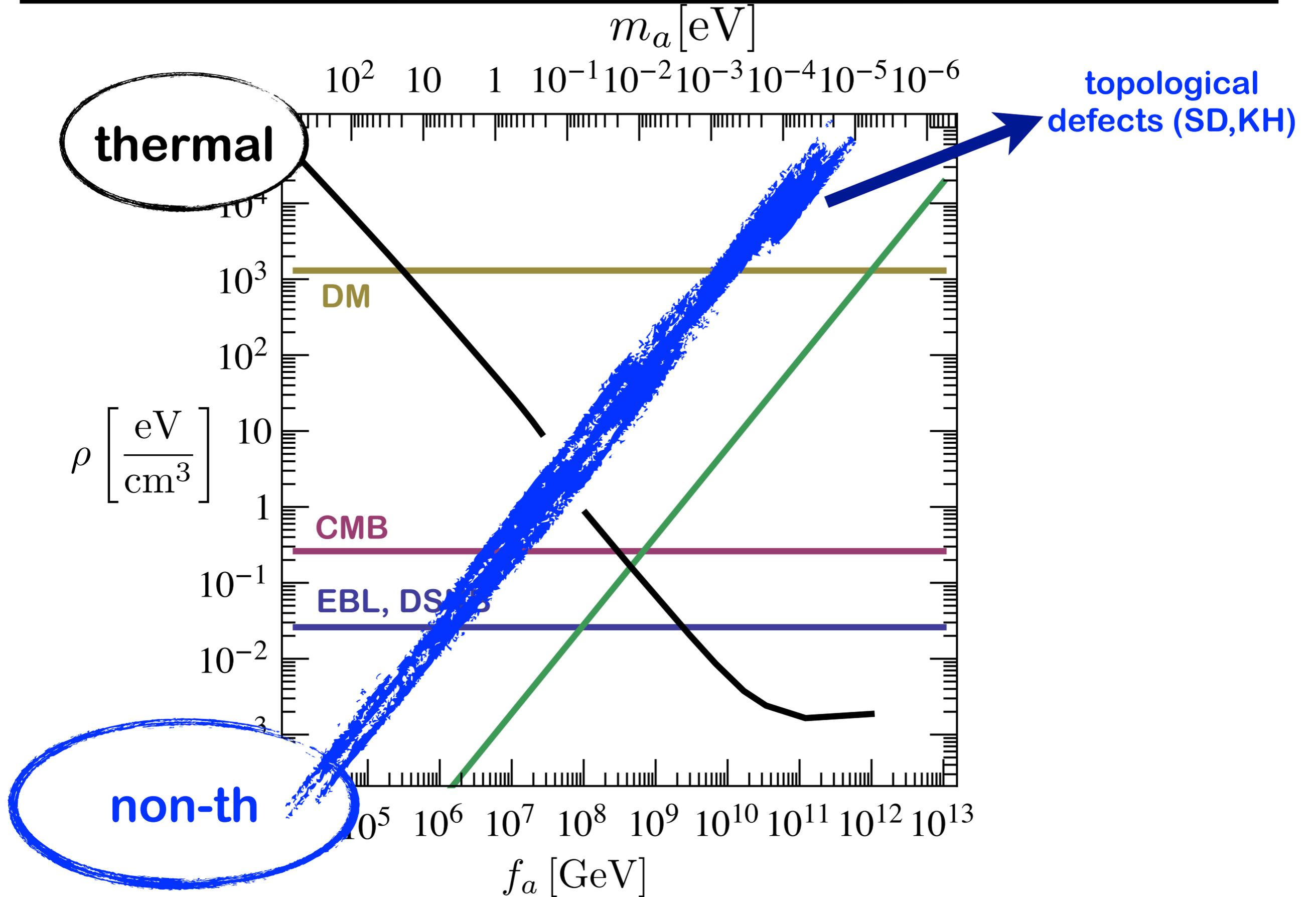
Axion energy density today



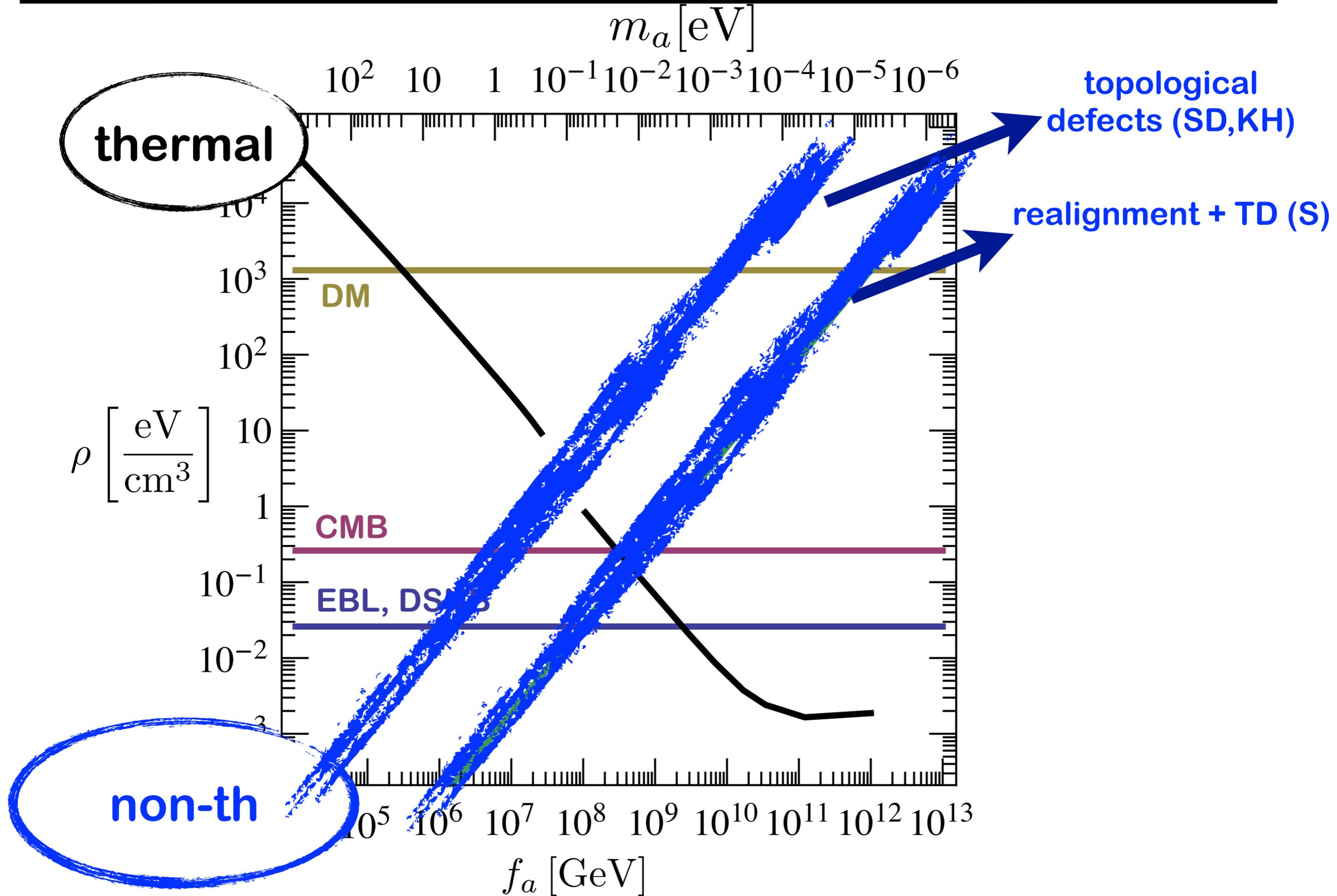
Axion energy density today



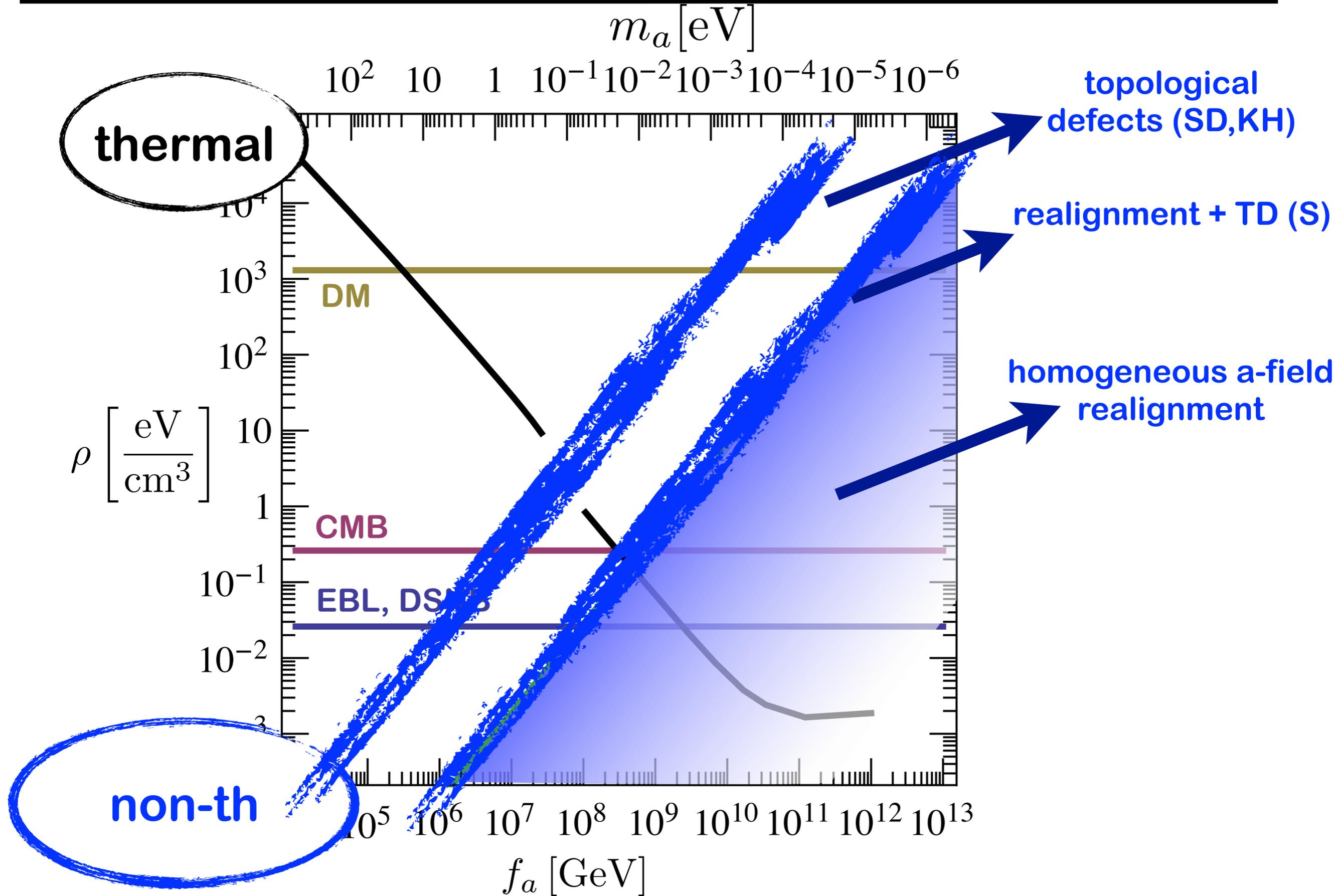
Axion energy density today



Axion energy density today

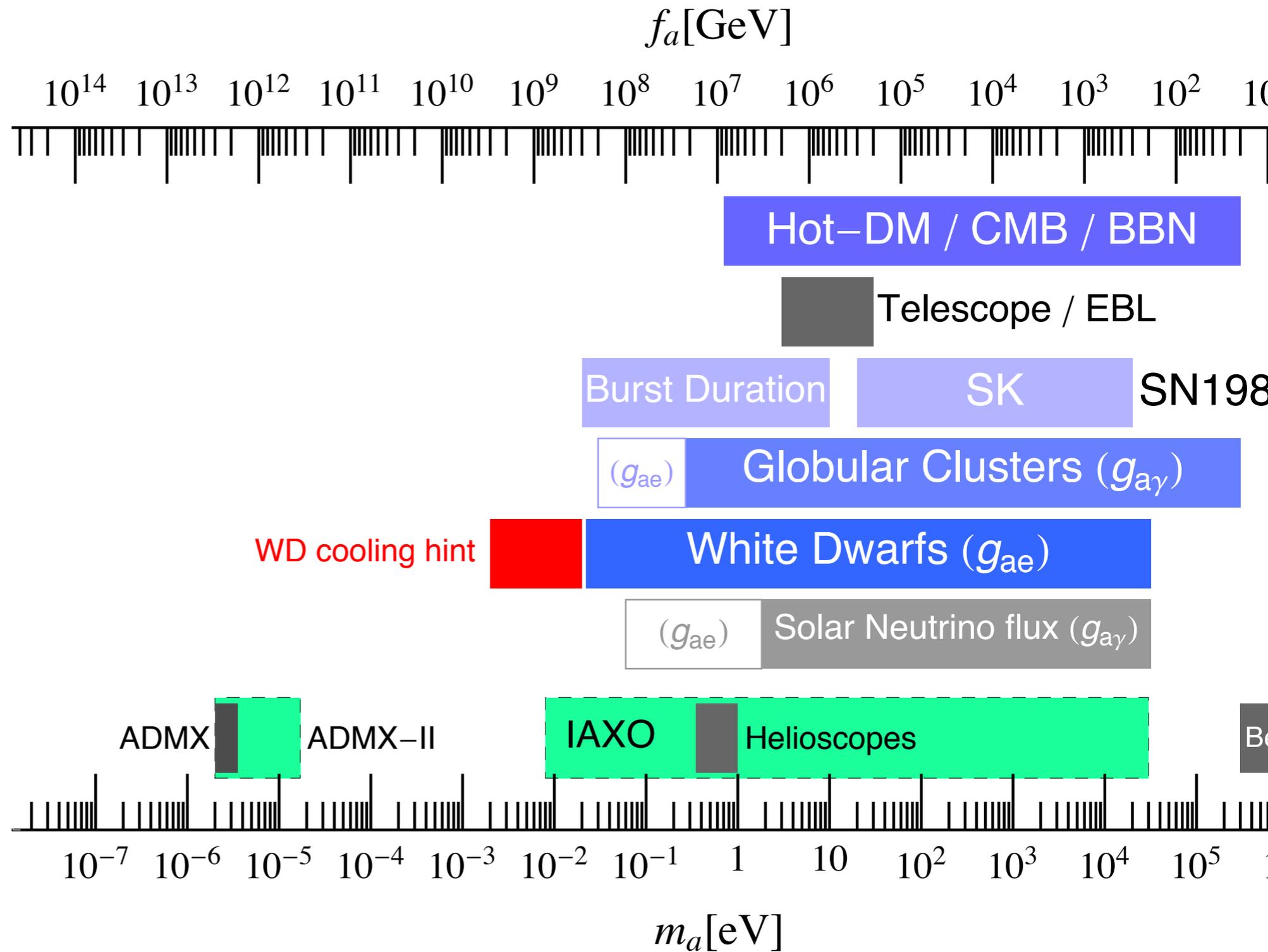


Axion energy density today



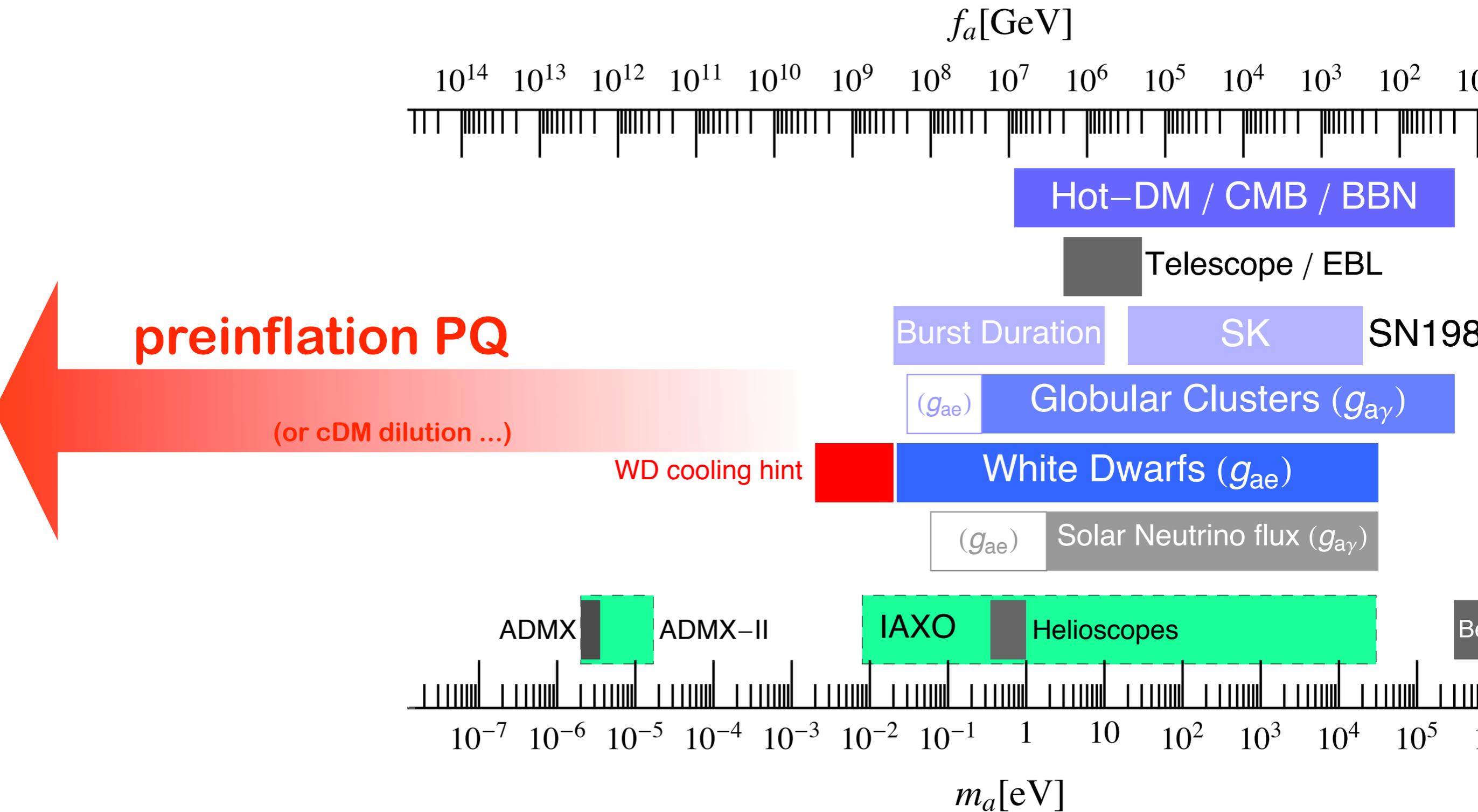
Where we are

Hewett et al. arXiv:1205.2671



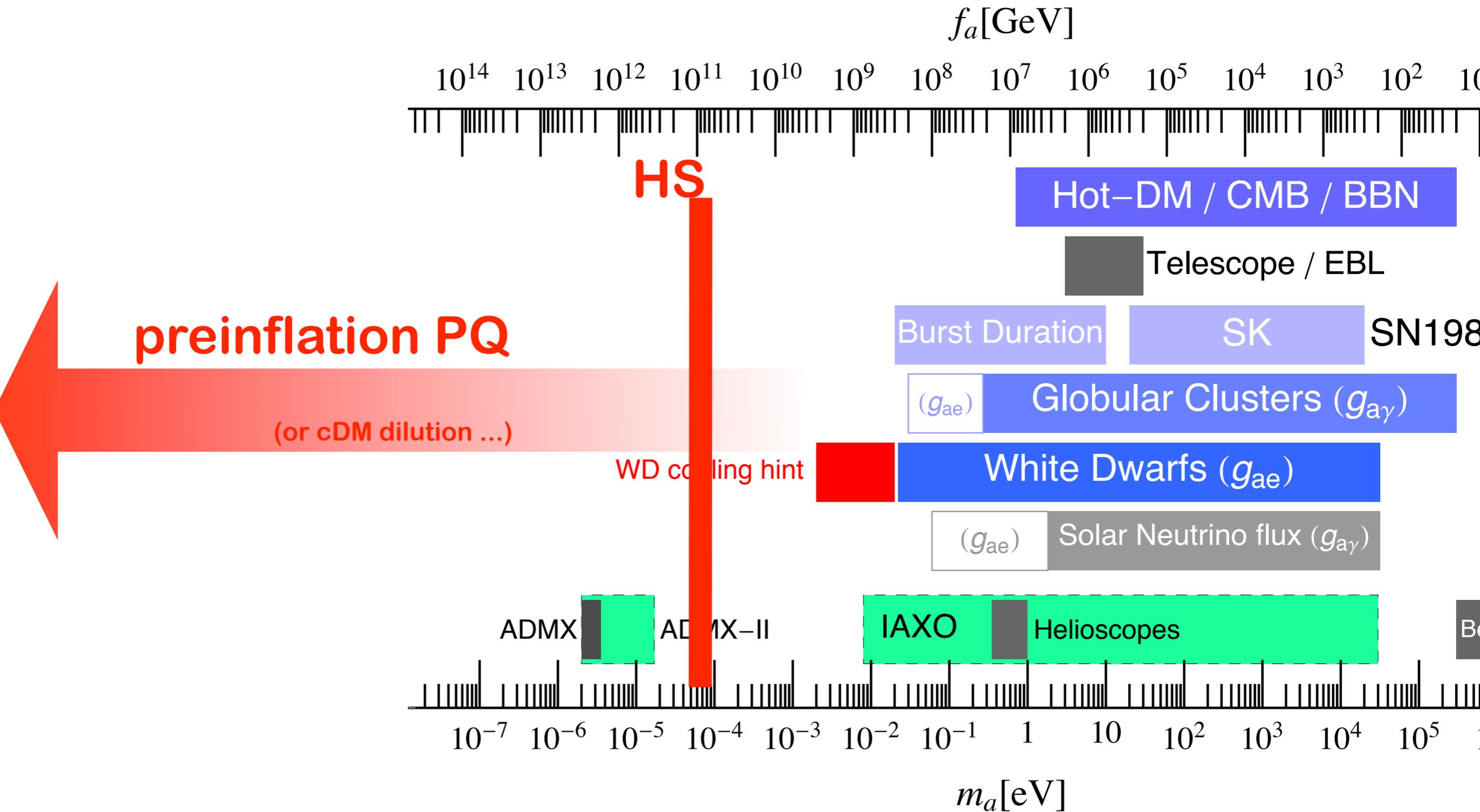
Where we are

Hewett et al. arXiv:1205.2671



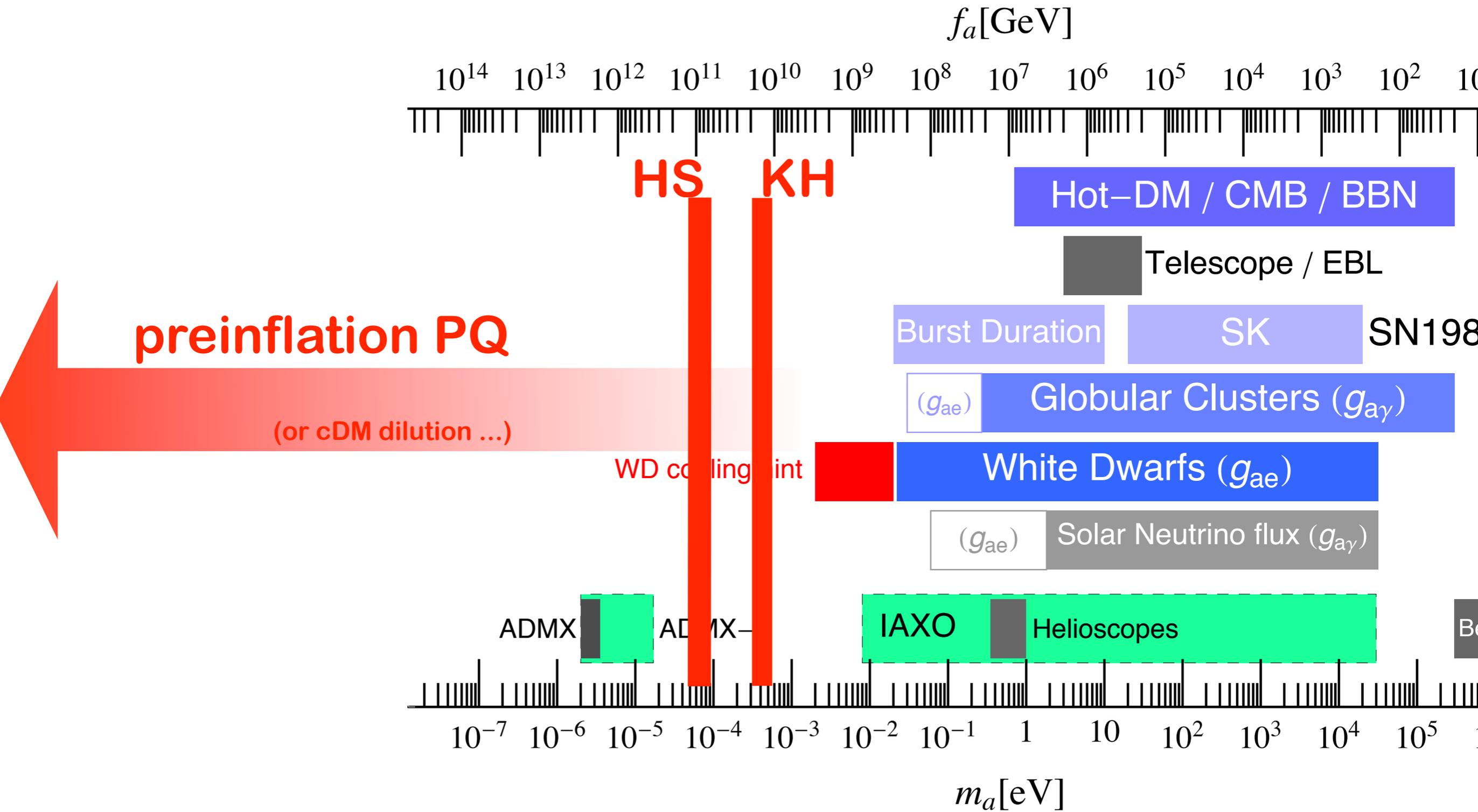
Where we are

Hewett et al. arXiv:1205.2671



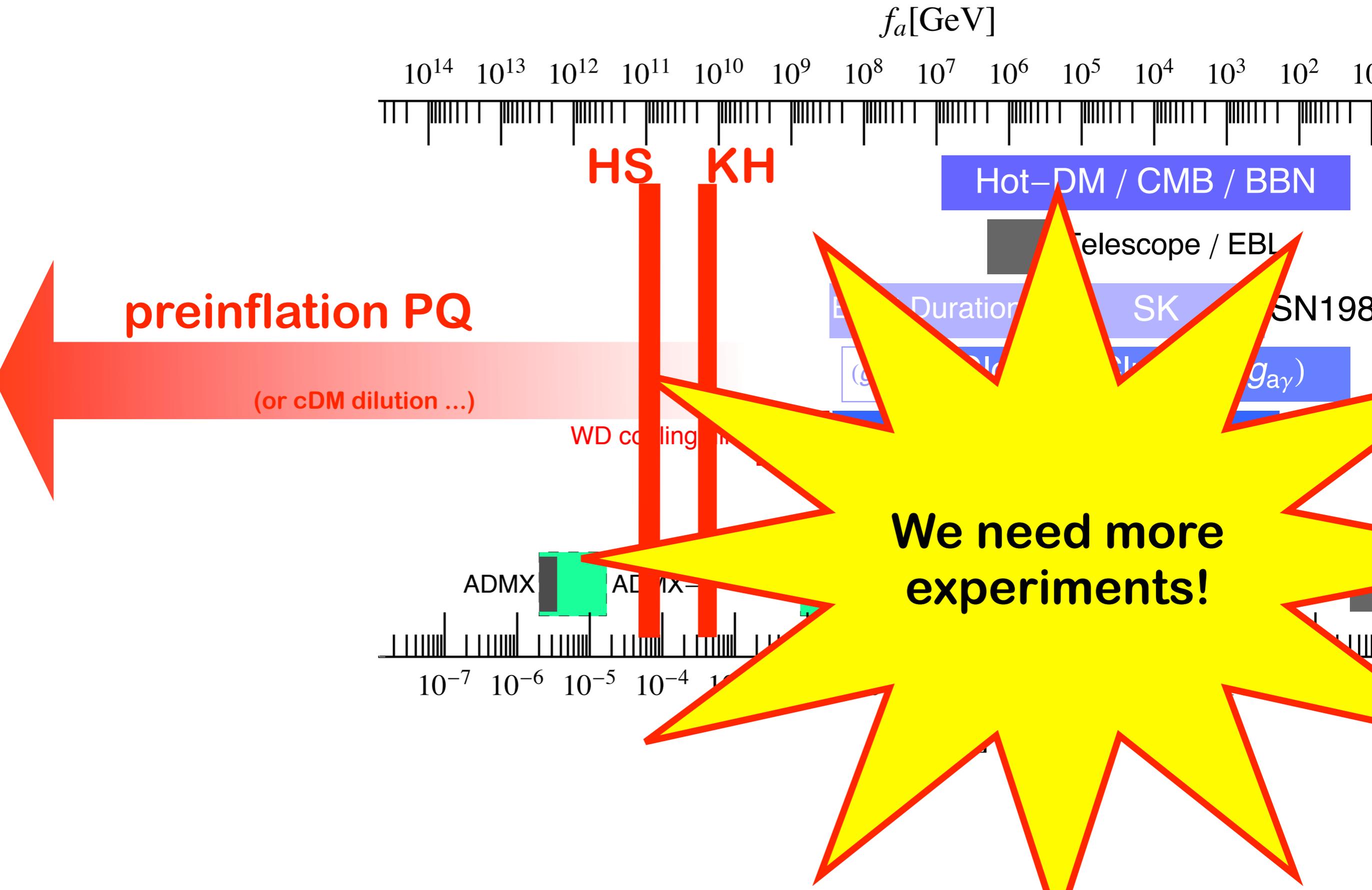
Where we are

Hewett et al. arXiv:1205.2671

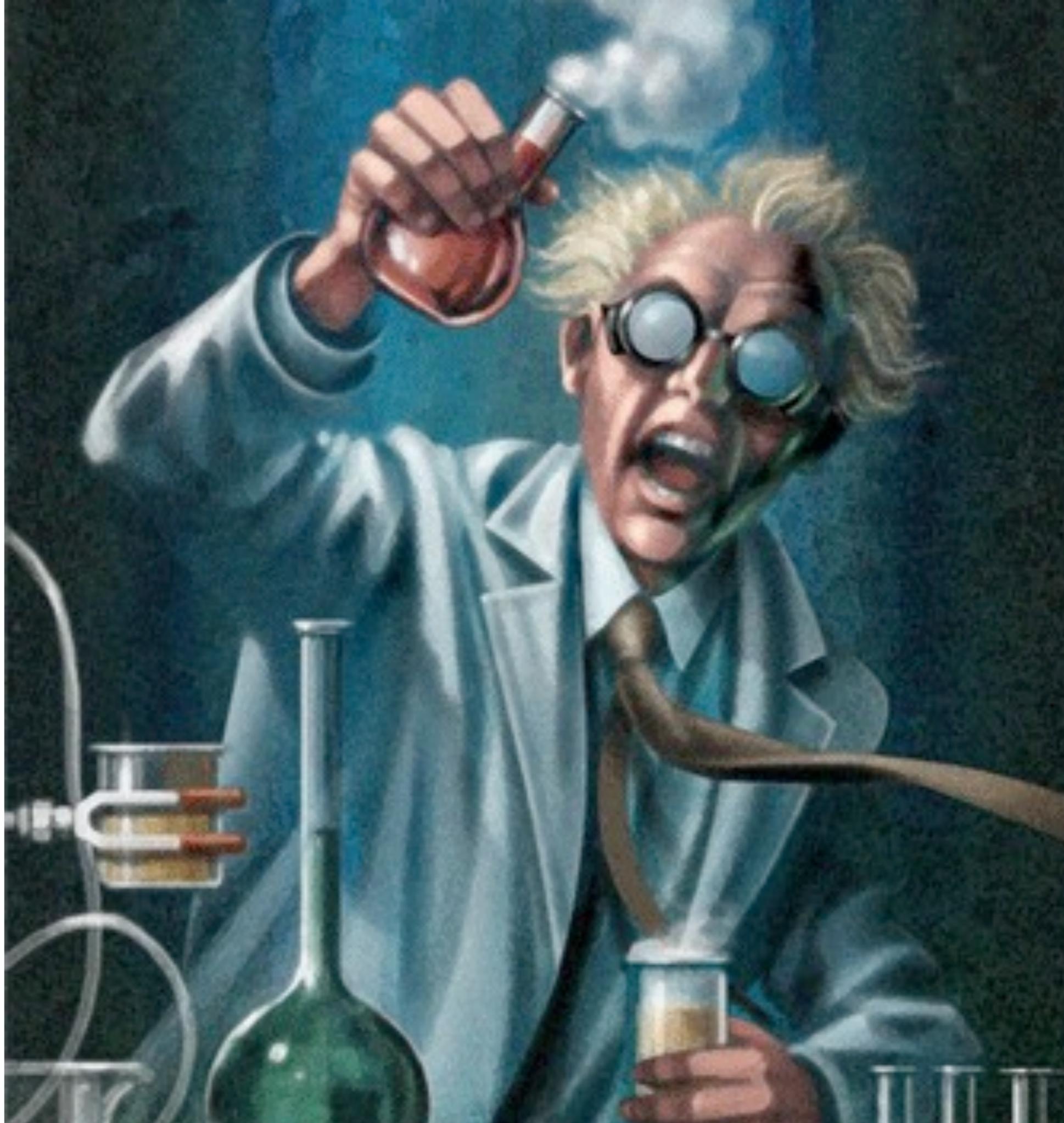


Where we are

Hewett et al. arXiv:1205.2671



Laboratory



Experimental searches for Axion Cold Dark Matter

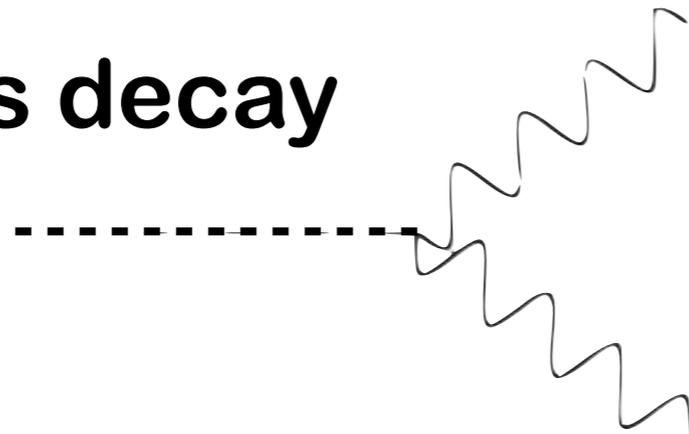
How do you search for particles whose interactions are suppressed by $f_a > 10^9 \text{ GeV}$?

.....

Experimental searches for Axion Cold Dark Matter

How do you search for particles whose interactions are suppressed by $f_a > 10^9 \text{ GeV}$?

Axions decay



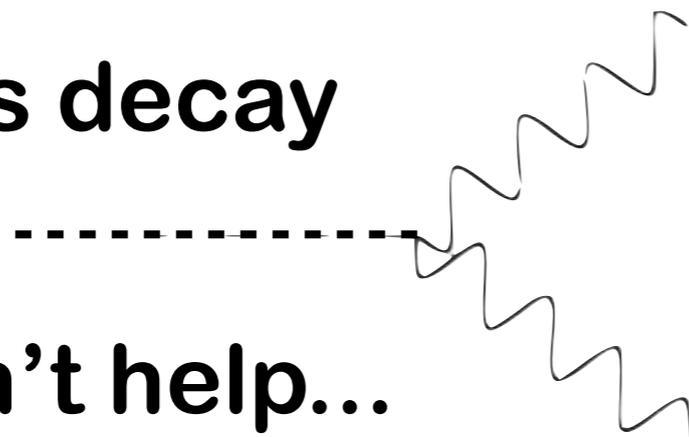
$$\tau_a \sim \frac{64\pi}{g_{a\gamma}^2 m_a^3} \sim 10^{24} \left(\frac{f_a}{10^6} \right)^2 \text{ s}$$

Experimental searches for Axion Cold Dark Matter

How do you search for particles whose interactions are suppressed by $f_a > 10^9 \text{ GeV}$?

Axions decay

doesn't help...



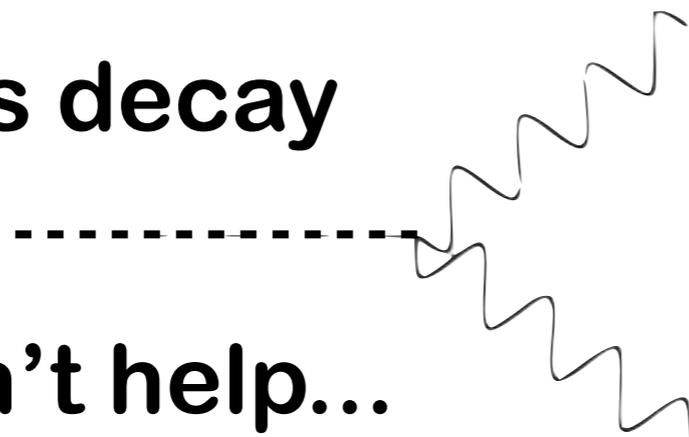
$$\tau_a \sim \frac{64\pi}{g_{a\gamma}^2 m_a^3} \sim 10^{24} \left(\frac{f_a}{10^6} \right)^2 \text{ s}$$

Experimental searches for Axion Cold Dark Matter

How do you search for particles whose interactions are suppressed by $f_a > 10^9 \text{ GeV}$?

Axions decay

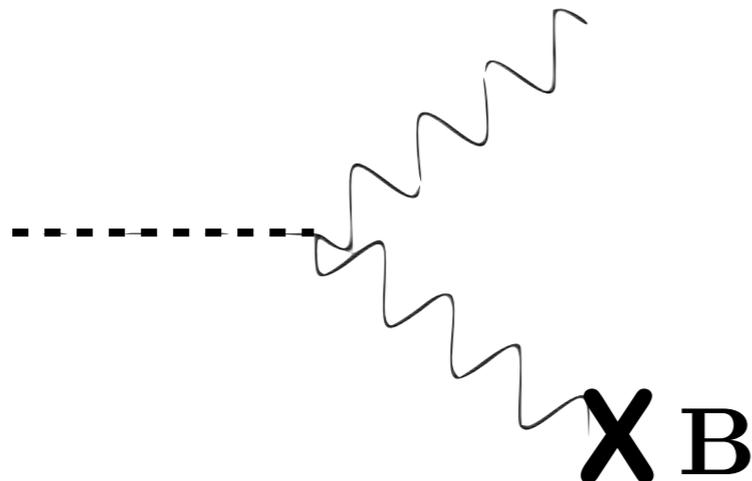
doesn't help...



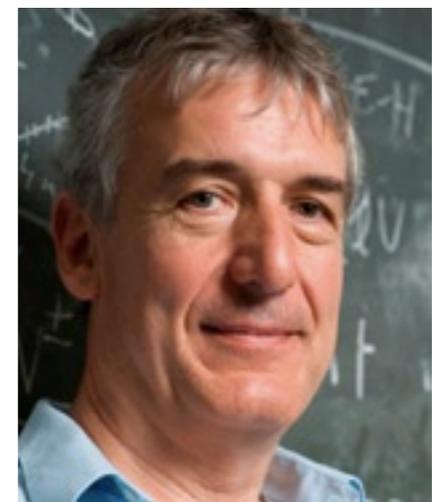
$$\tau_a \sim \frac{64\pi}{g_{a\gamma}^2 m_a^3} \sim 10^{24} \left(\frac{f_a}{10^6} \right)^2 \text{ s}$$

Experimental Tests of the Invisible Axion

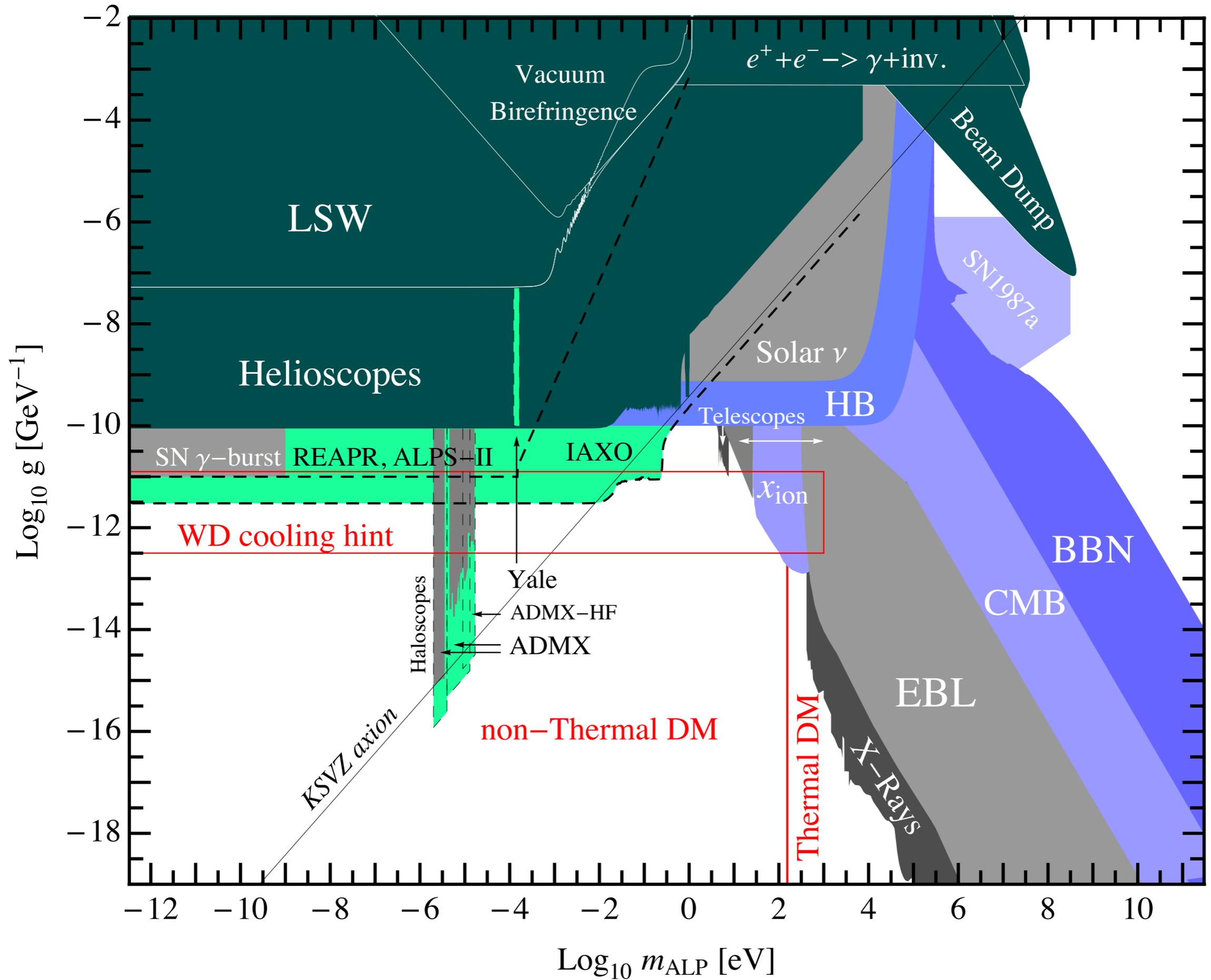
Phys.Rev.Lett. 51 (1983) 1415



Axion-Photon coherent conversion in macroscopic magnetic fields !!

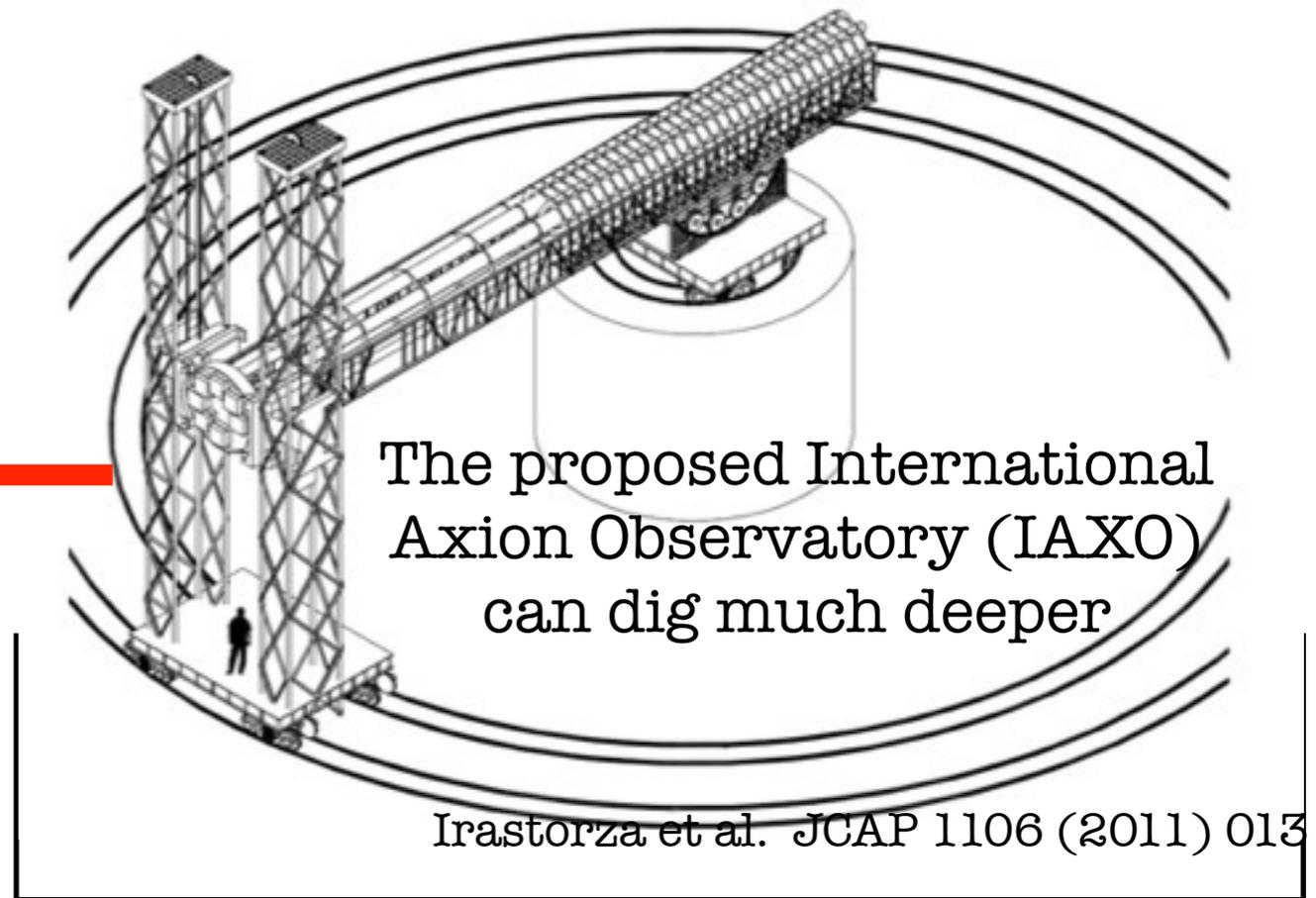
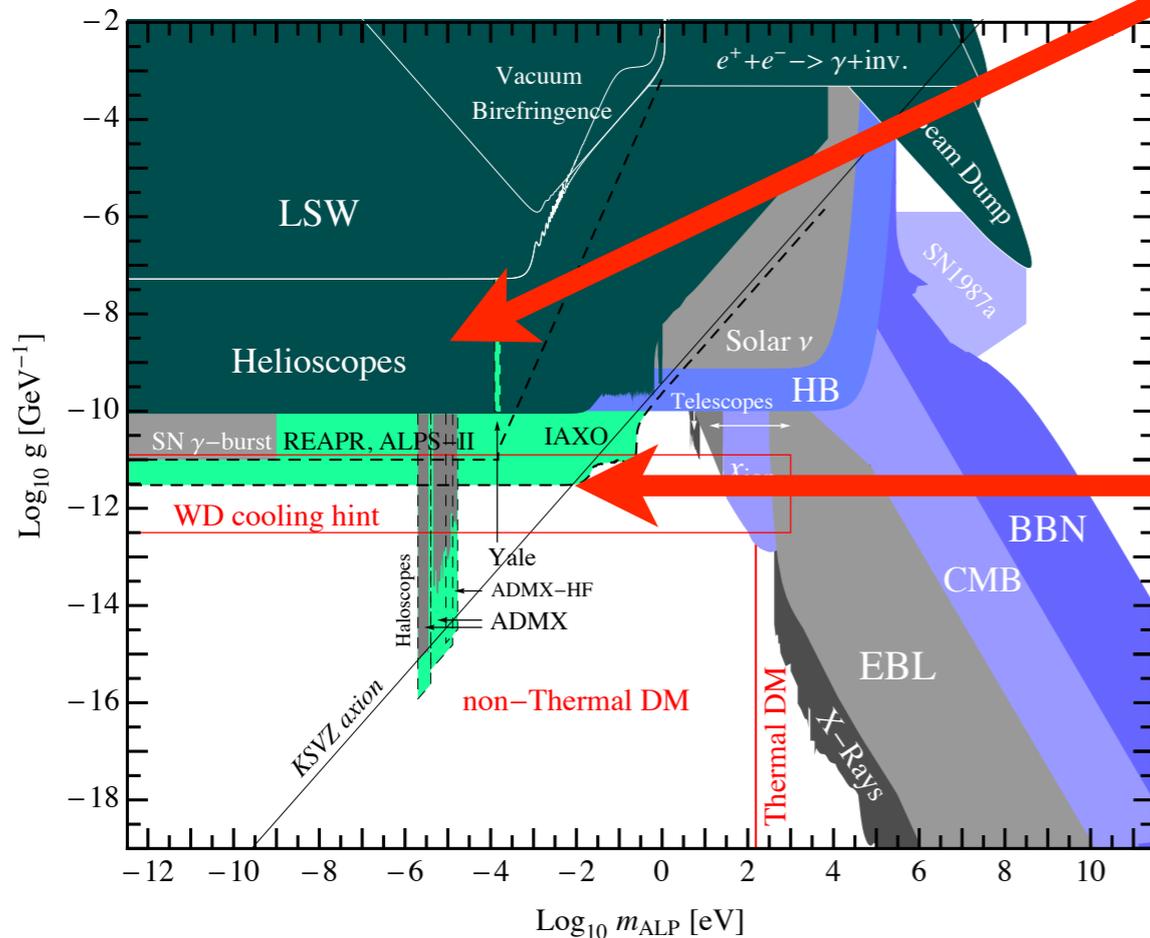
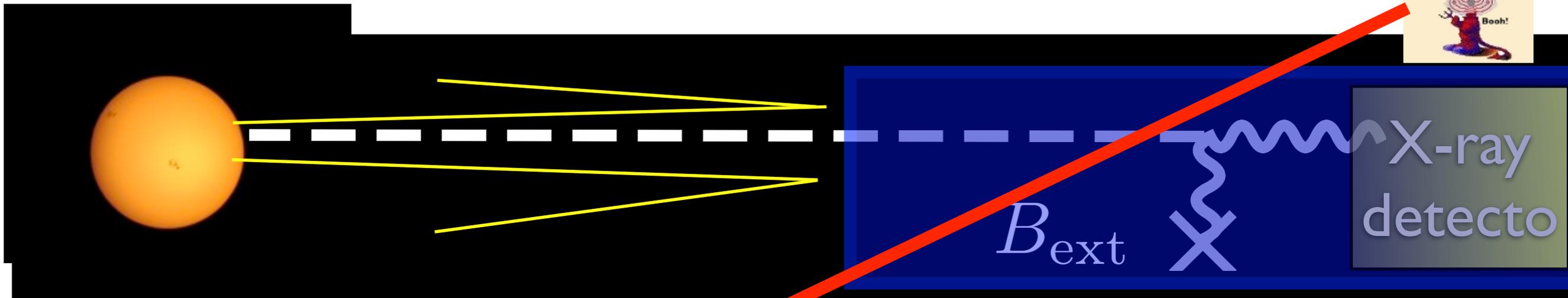


P. Sikivie



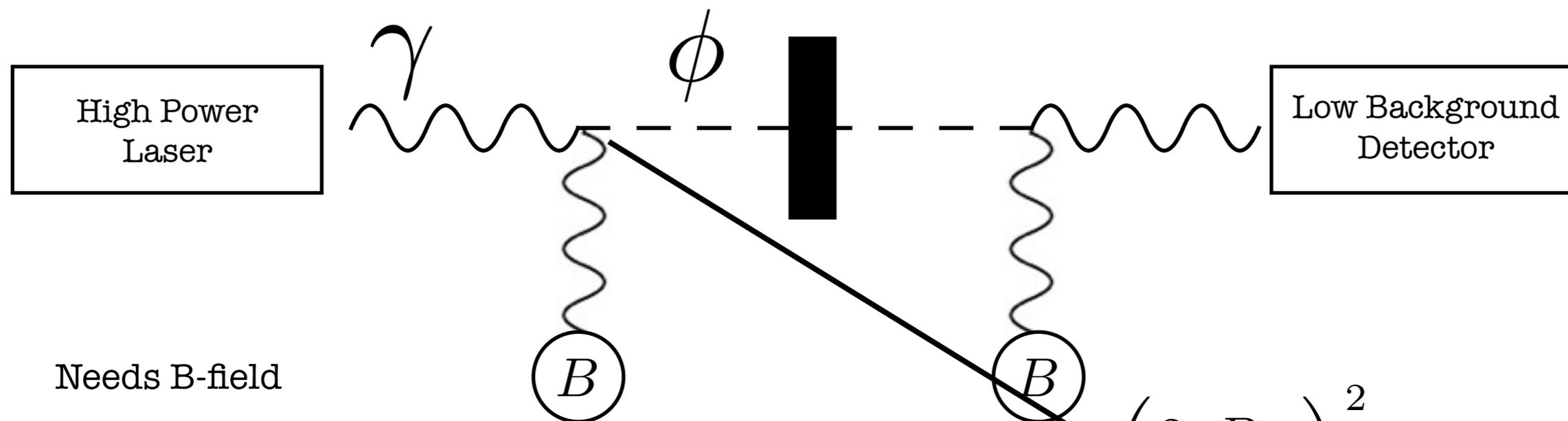
HELIOSCOPES

Detect Solar ALPs at earth by means of inverse Primakoff conversion in a strong magnetic field

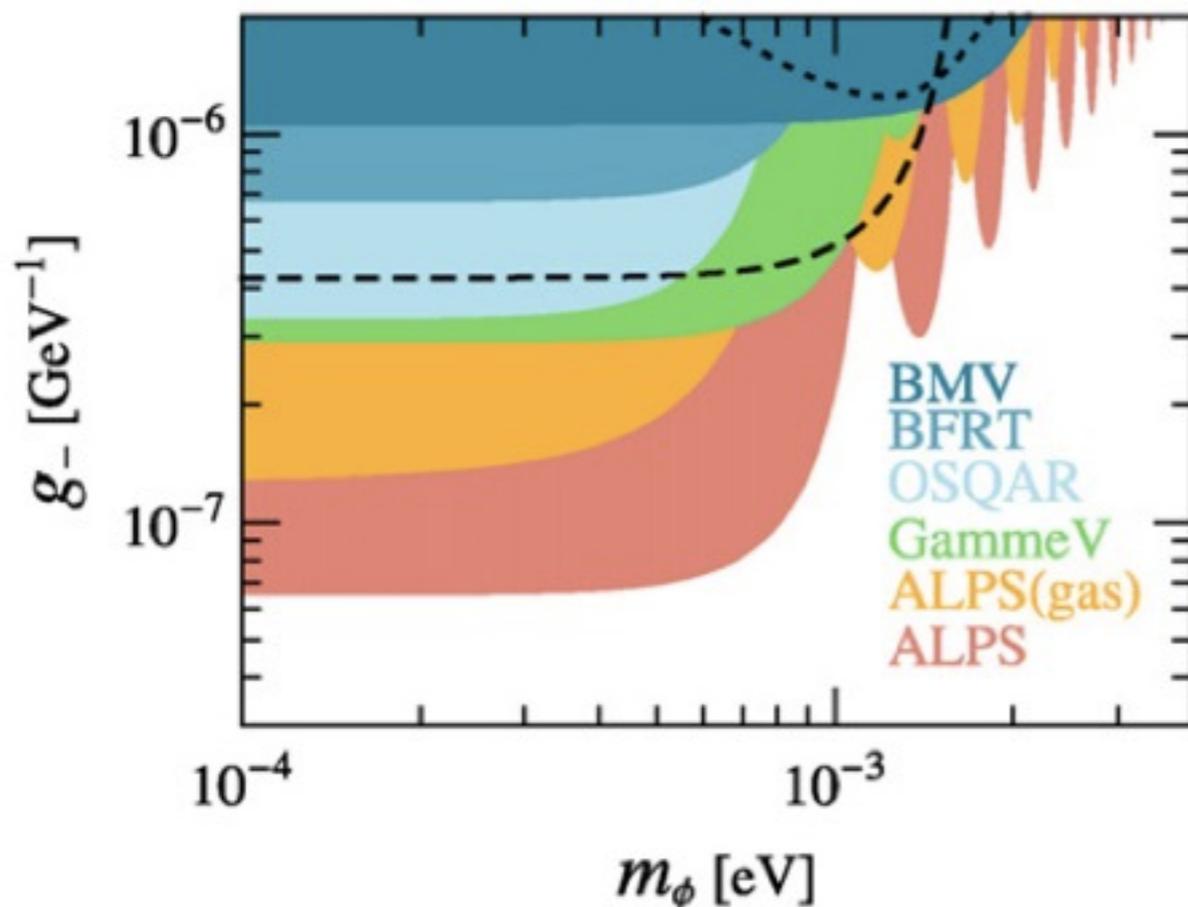


Laboratory Experiments

Laser shining through walls (LSW)



$$P(\gamma \rightarrow \phi) = \left(\frac{2gB\omega}{m_\phi^2} \right)^2 \times \sin^2 \frac{m_\phi^2 L}{4\omega}$$



Ehret et al. 2010

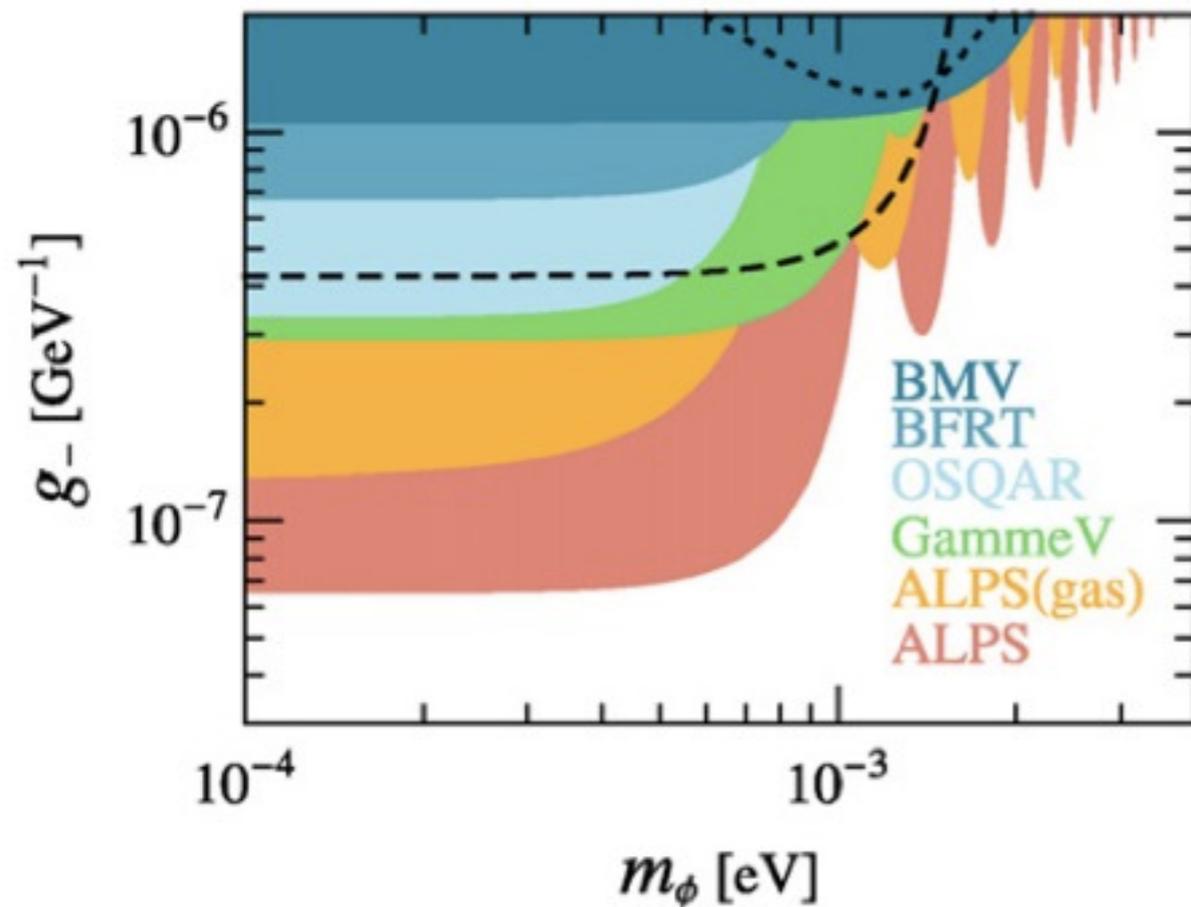


Laboratory Experiments

High
L



Need



$$P(\gamma \rightarrow \phi) = \left(\frac{2gB\omega}{m_\phi^2} \right) \times \sin^2 \frac{m_\phi^2 L}{4\omega}$$

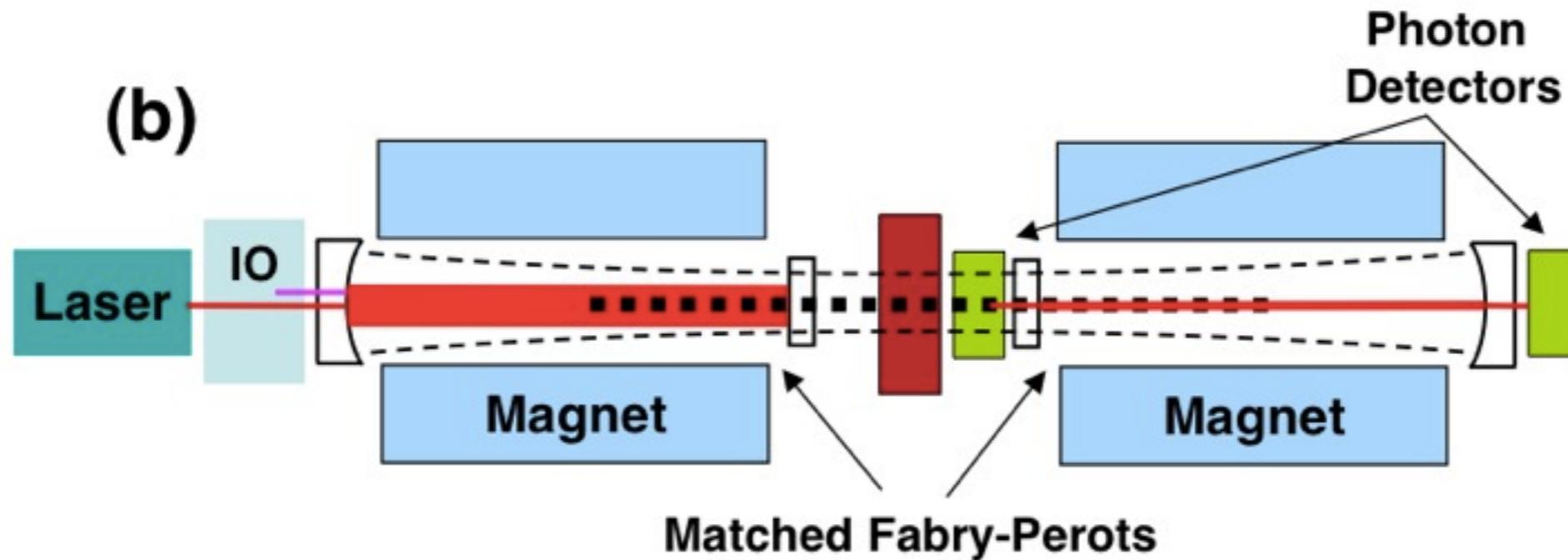


Ehret et al. 2010

Much longer experiments + 2nd resonant cavity

$O(100 \text{ m})$

$Q \sim 10^5$

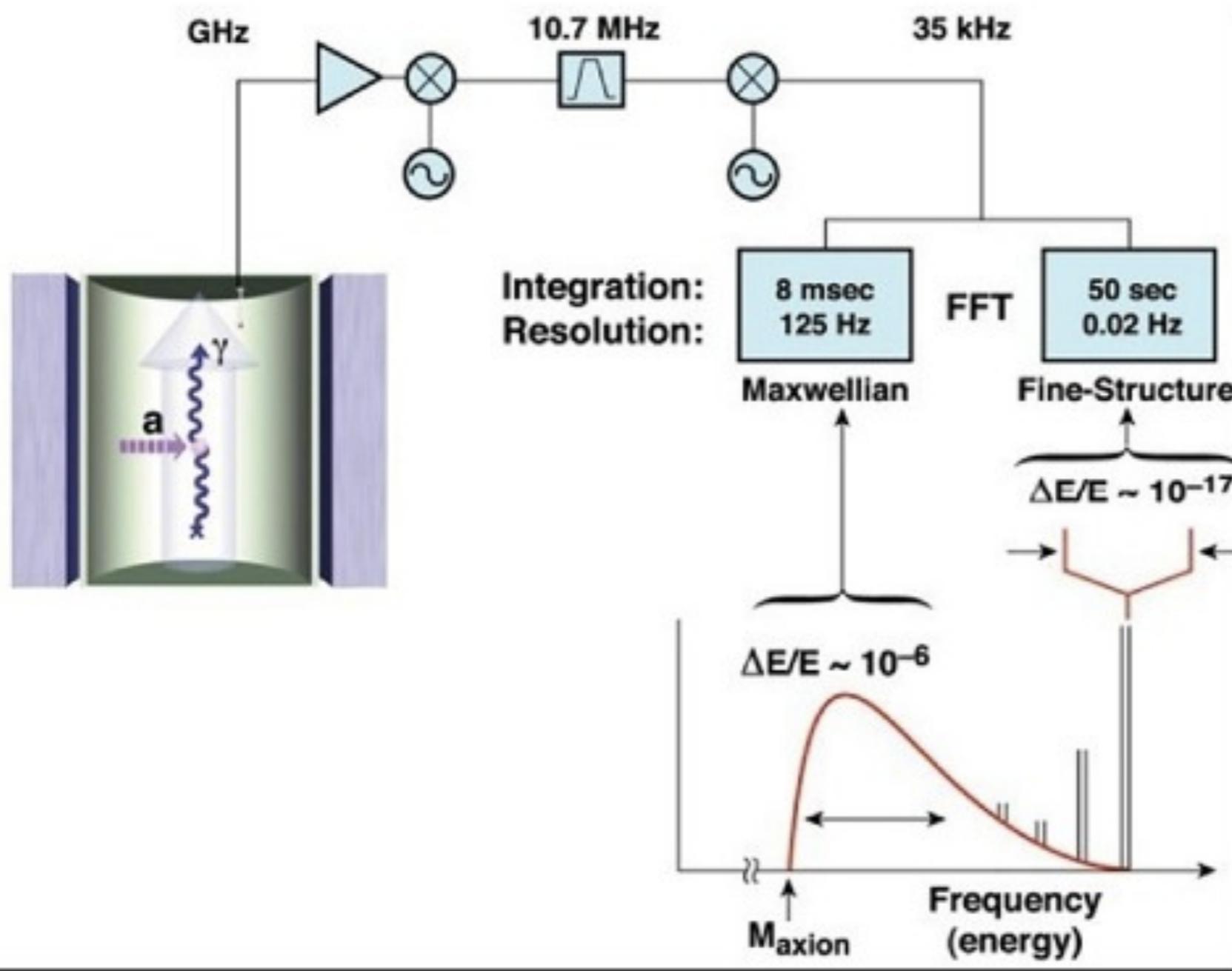


Two competing groups:
ALPS II @ DESY vs. Fermilab

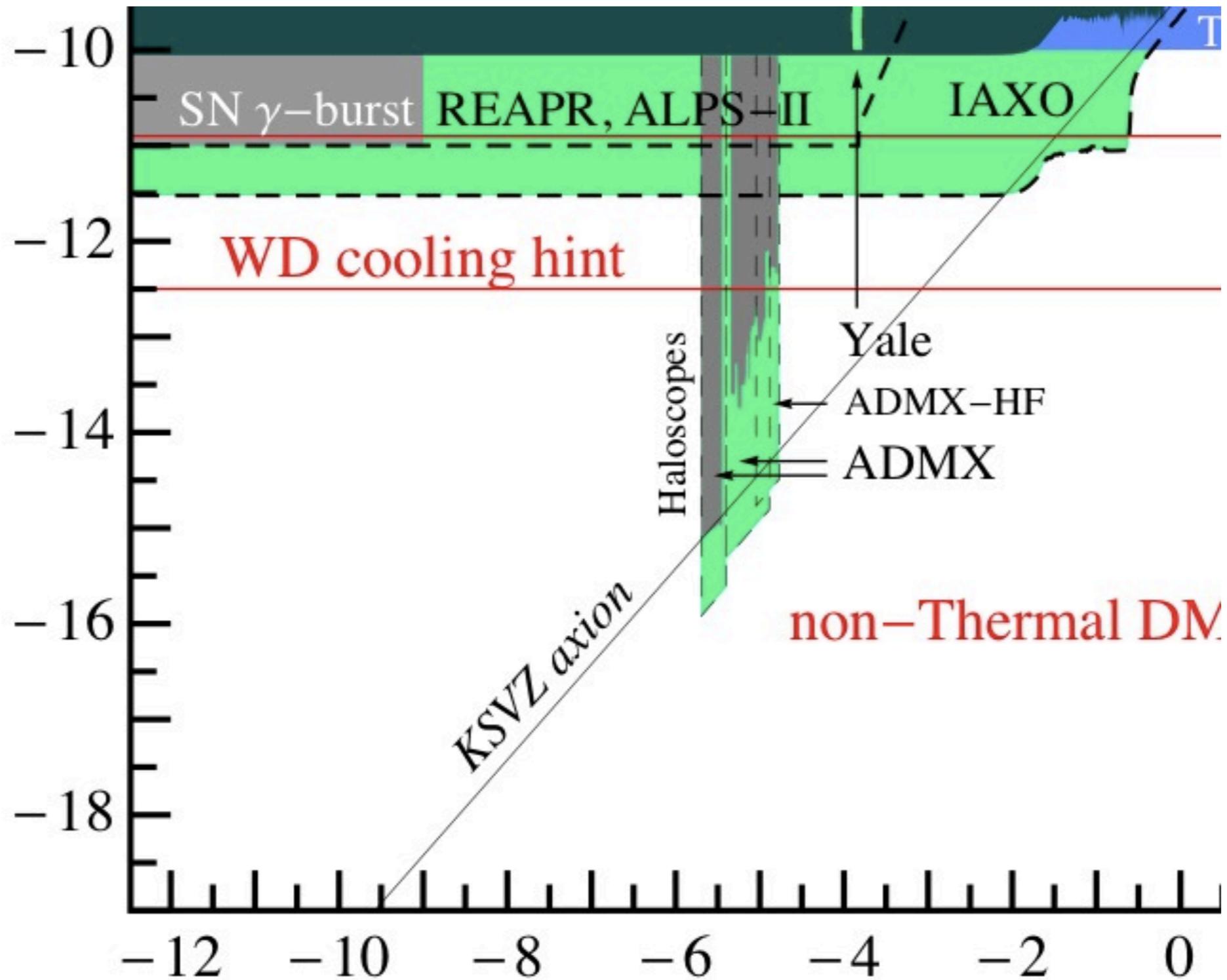
Cavity experiments (Haloscopes)

Axions excite electromagnetic waves in a cavity

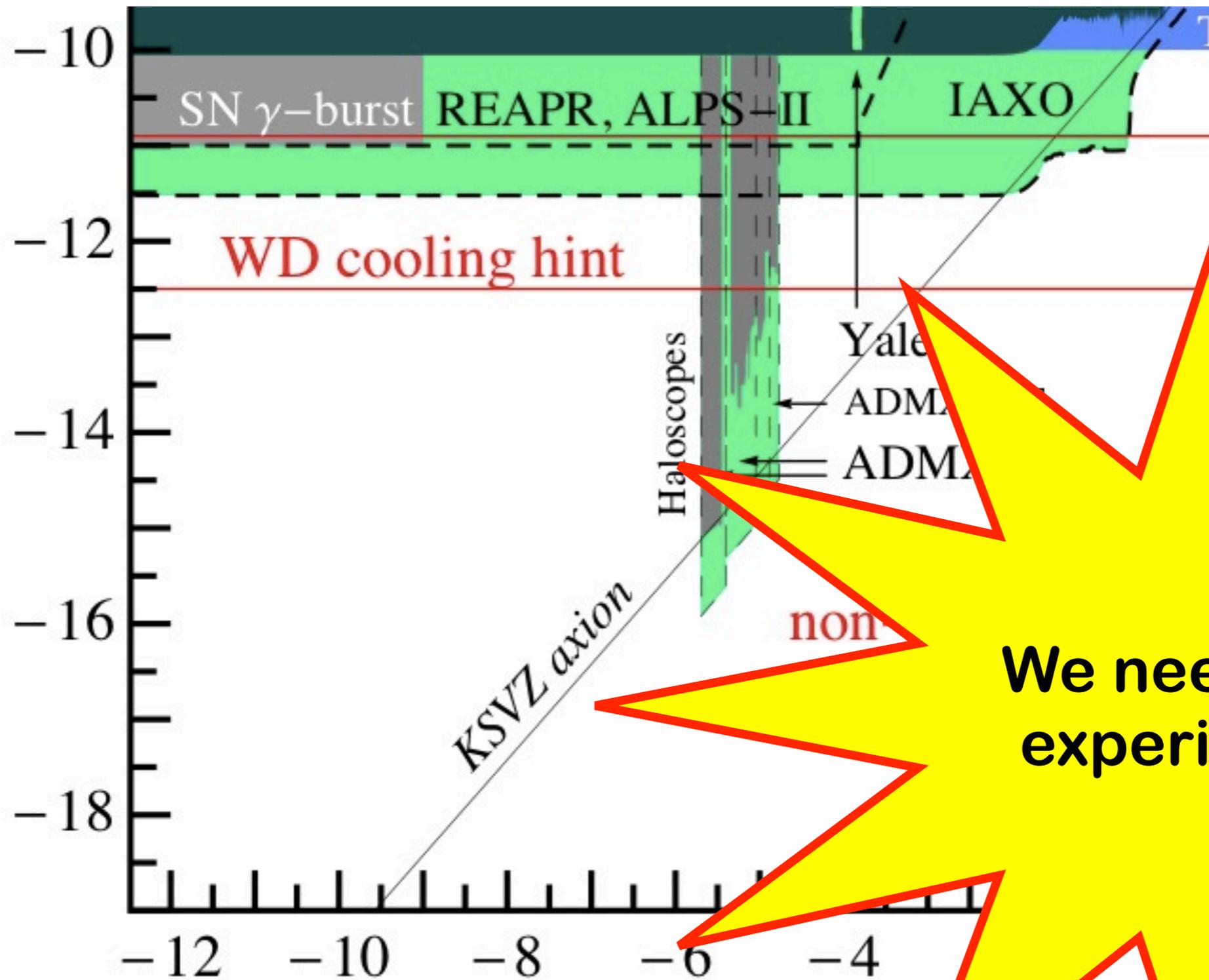
$$\omega \sim m_a$$



Cavity experiments (Haloscopes)



Cavity experiments (Haloscopes)



Conclusions

- Invite me again to know more about experiments
- Dynamical mechanism to solve Strong CP implies
detectable cold Dark Matter axions
- Different cosmologies/uncertainties
large range of masses to scan
- Powerful but insufficient ongoing experiments
many more are to come!

The End

Javier Redondo (LMU & MPP München)

27 Nov 2012, Invisible seminar

