



Neutrino masses from cosmological intergalactic data

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Webminar for Invisibles 27th January 2015*



OUTLINE

INTRO: the Intergalactic Medium and its main manifestation

TOOLS: Beyond linear theory with N-body/hydrodynamic simulations

DATA: State of the art observables at large and small scales

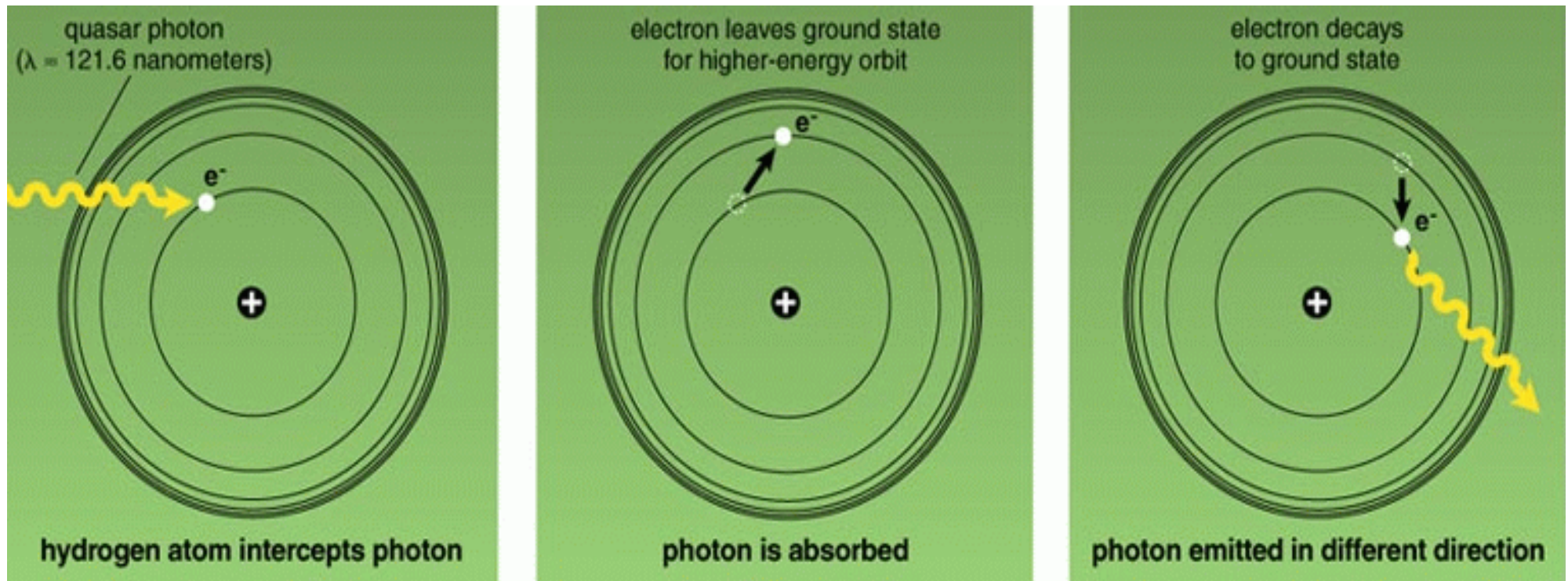
INTRO

Let's learn:

- why atomic physics is important for intergalactic space
- baryons in intergalactic space are diffuse/low density
- physics of the IGM is relatively simple (at least at large scales)
- semi-analytical models can describe it well within 10% uncertainties or so

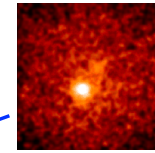
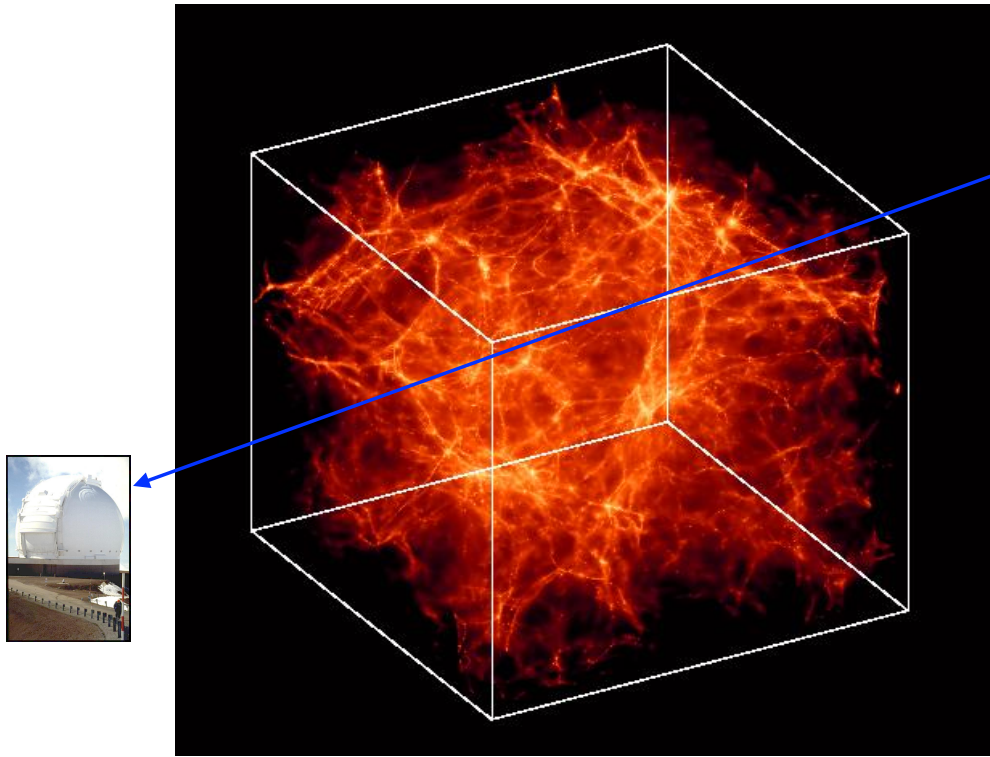
The Lyman- α forest

Lyman- α absorption is the main manifestation of the IGM



Tiny neutral hydrogen fraction after reionization.... But large cross-section

The Intergalactic Medium: Theory vs. Observations



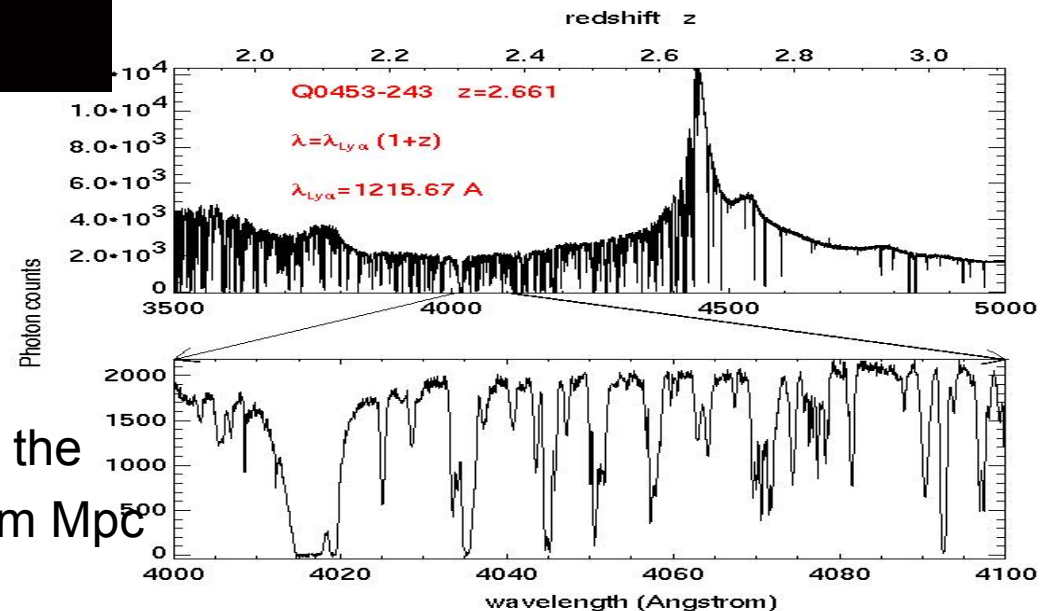
80 % of the baryons at $z=3$
are in the **Lyman- α forest**

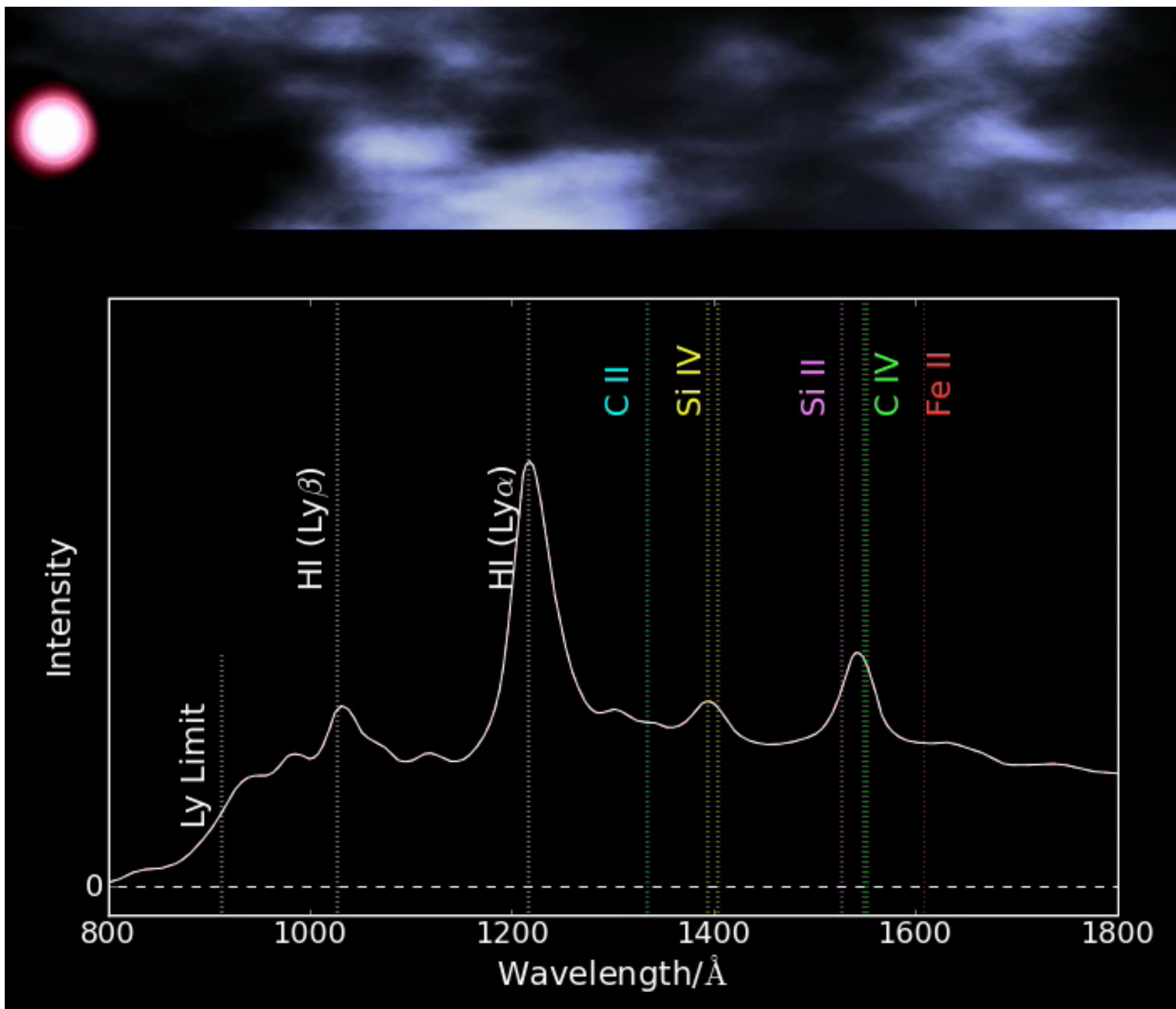
Bi & Davidsen (1997), Rauch (1998)
Review by Meiksin (2009)

baryons as tracer of the dark
matter density field

$\delta_{\text{IGM}} \sim \delta_{\text{DM}}$ at scales larger than the
Jeans length $\sim 1 \text{ com Mpc}$

$$\tau \sim (\delta_{\text{IGM}})^{1.6} T^{-0.7}$$





Modelling the IGM – I: Physics

Dark matter evolution: linear theory of density perturbation +
Jeans length $L_J \sim \sqrt{T/\rho}$ + mildly non linear evolution

Hydrodynamic processes: mainly **gas cooling**
cooling by adiabatic expansion of the universe
heating of gaseous structures (reionization)

- **photoionization** by a uniform Ultraviolet Background
- **Hydrostatic equilibrium** of gas clouds

dynamical time = $1/\sqrt{G \rho}$ $\sim$ **sound crossing time** = size / gas sound speed



Size of the cloud: > 100 kpc
Temperature: $\sim 10^4$ K
Mass in the cloud: $\sim 10^9 M_\odot$
Neutral hydrogen fraction: 10^{-5}

In practice, since the process is mildly non linear you need numerical simulations
To get convergence of the simulated flux at the percent level (observed)

Modelling the IGM – II: Analytical models for the Ly-a forest

(Bi 1993, Bi & Davidsen 1997, Hui & Gnedin 1998, Matarrese & Mohayaee 2002)

$$k_J^{-1}(z) \equiv H_0^{-1} \left[\frac{2\gamma k_B T_m(z)}{3\mu m_p \Omega_{0m}(1+z)} \right]^{1/2}$$

Jeans length

$$\delta_0^{\text{IGM}}(\mathbf{k}, z) = \frac{\delta_0^{\text{DM}}(\mathbf{k}, z)}{1 + k^2/k_J^2(z)} \equiv W_{\text{IGM}}(k, z) D_+(z) \delta_0^{\text{DM}}(\mathbf{k})$$

Filtering of linear DM density field

$$\mathbf{v}^{\text{IGM}}(\mathbf{k}, z) = E_+(z) \frac{i\mathbf{k}}{k^2} W_{\text{IGM}}(k, z) \delta_0^{\text{DM}}(\mathbf{k})$$

Peculiar velocity

$$n_{\text{IGM}}(\mathbf{x}, z) = \bar{n}_{\text{IGM}}(z) \exp \left[\delta_0^{\text{IGM}}(\mathbf{x}, z) - \frac{\langle (\delta_0^{\text{IGM}})^2 \rangle D_+^2(z)}{2} \right]$$

Non linear density field

$$T(\mathbf{x}, z) = T_0(z) (1 + \delta^{\text{IGM}}(\mathbf{x}, z))^{\gamma(z)-1}$$

'Equation-of-state'

$$\alpha(z, T(z)) n_p n_e = J(z) n_{\text{HI}},$$

Neutral hydrogen ionization equilibrium equation

$$\tau(u) = \frac{\sigma_{0,\alpha} c}{H(z)} \int_{-\infty}^{\infty} dy n_{\text{HI}}(y) \mathcal{V}[u - y - v_{\parallel}^{\text{IGM}}(y), b(y)]$$

Optical depth

Density

Velocity

Temperature

Linear fields:
density, velocity



Non linear fields

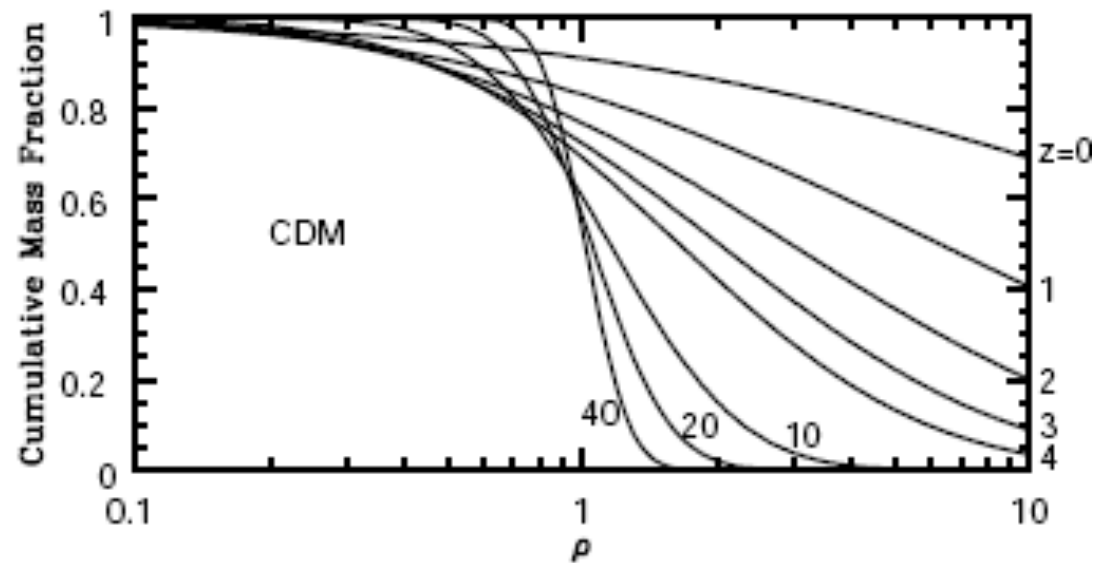


Temperature

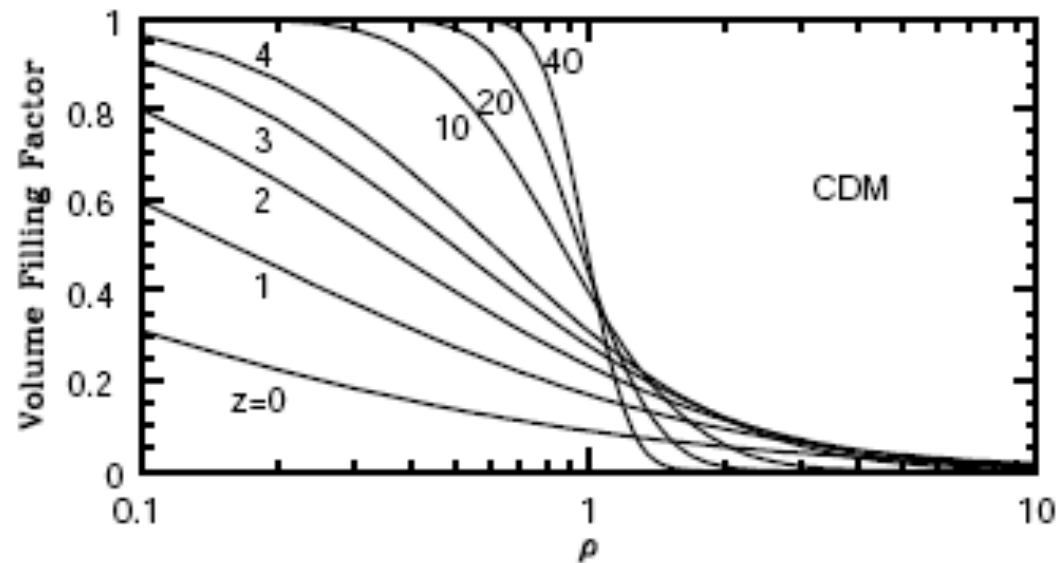


Spectra:
Flux=exp(-τ)

Modelling the IGM – III: IGM in a CDM universe

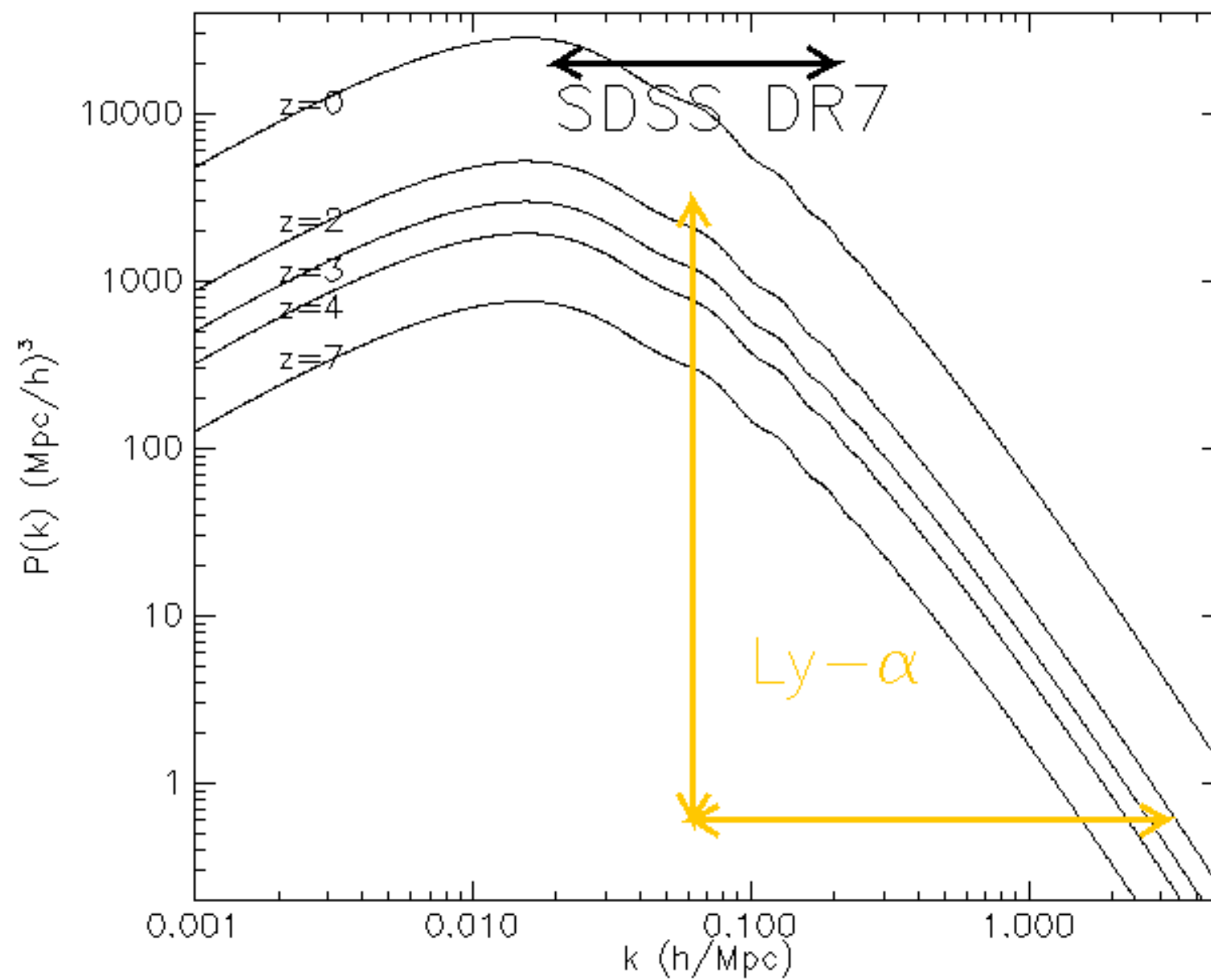


$M(>\rho)$



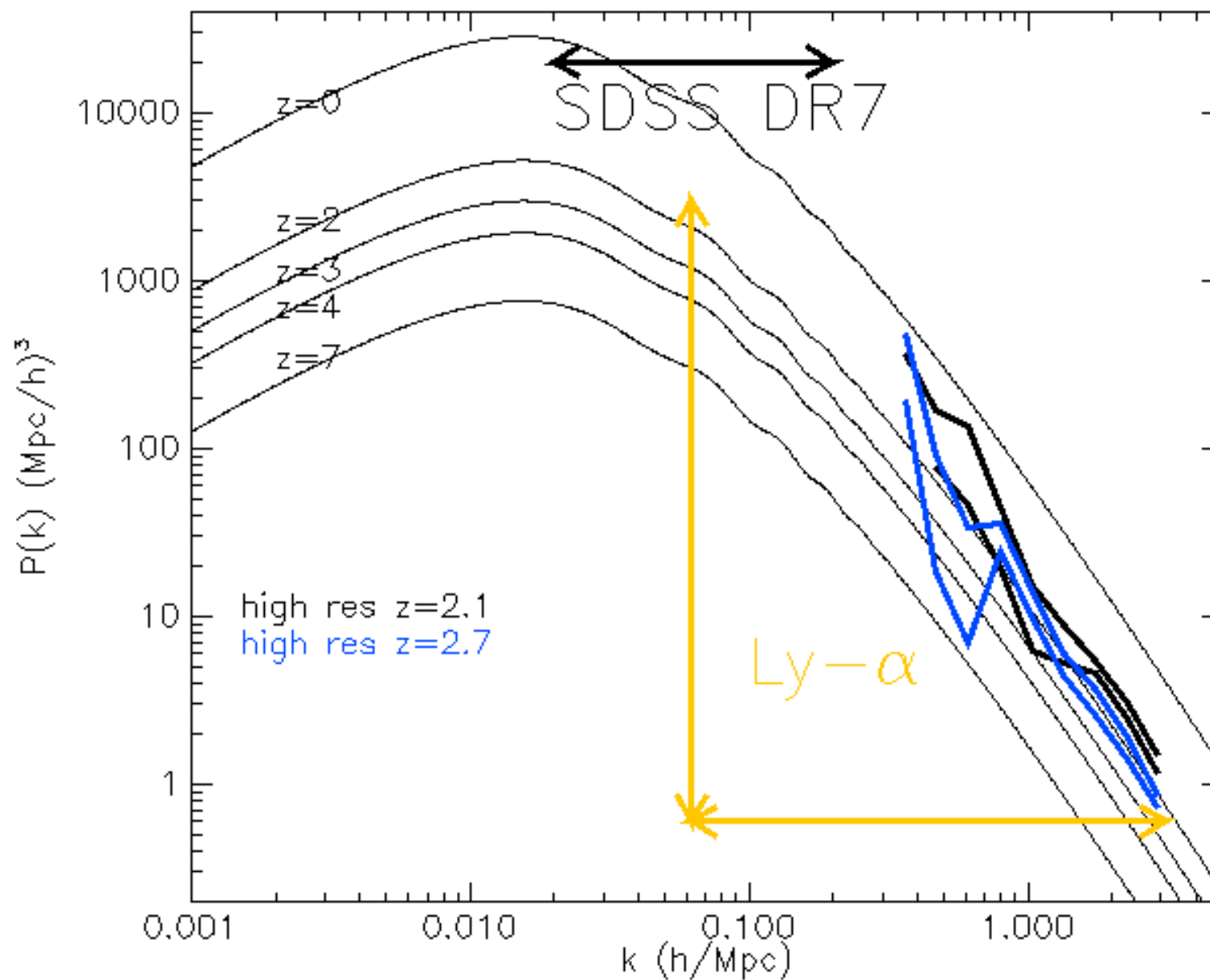
$V(>\rho)$

DATA vs THEORY

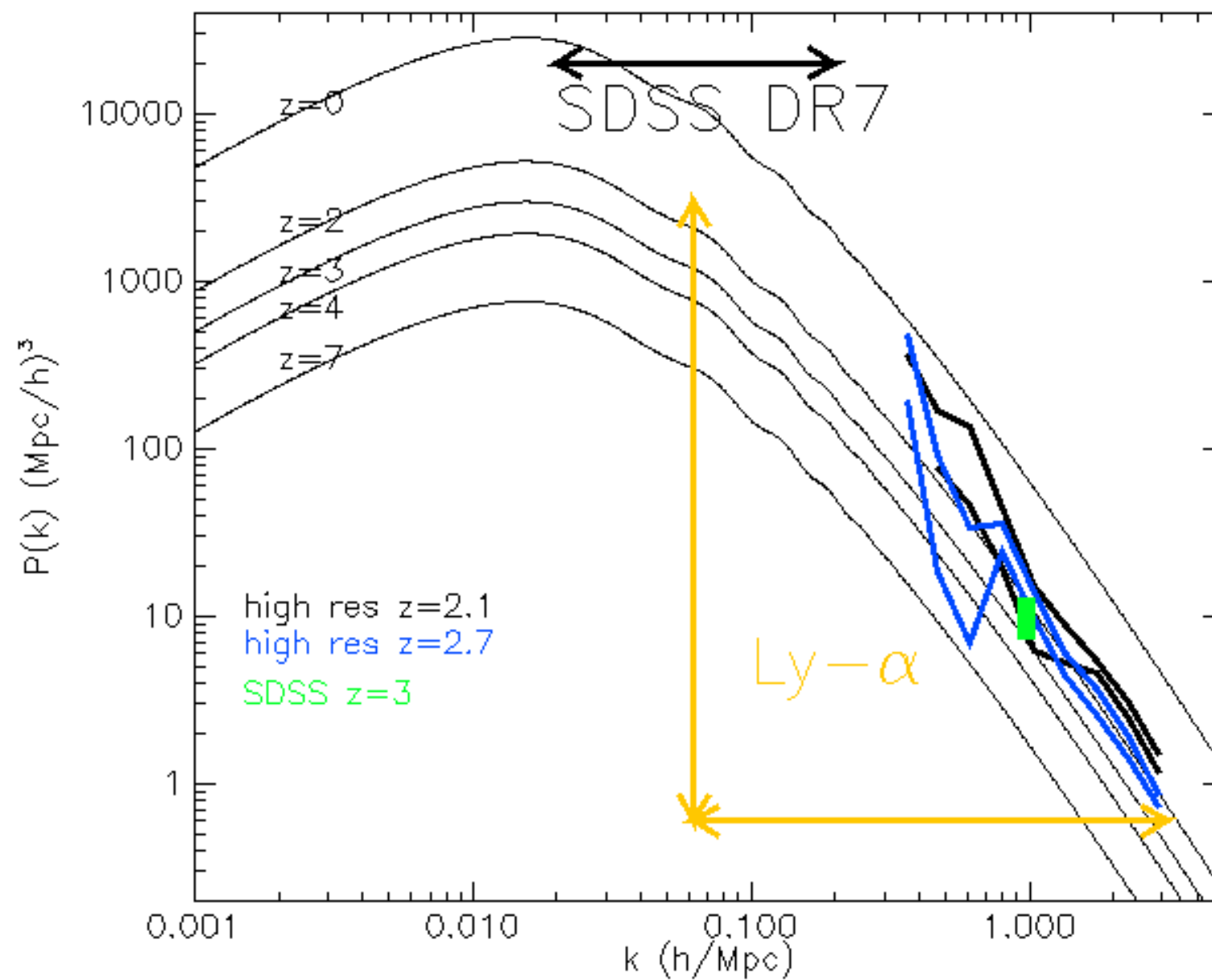


DATA vs THEORY

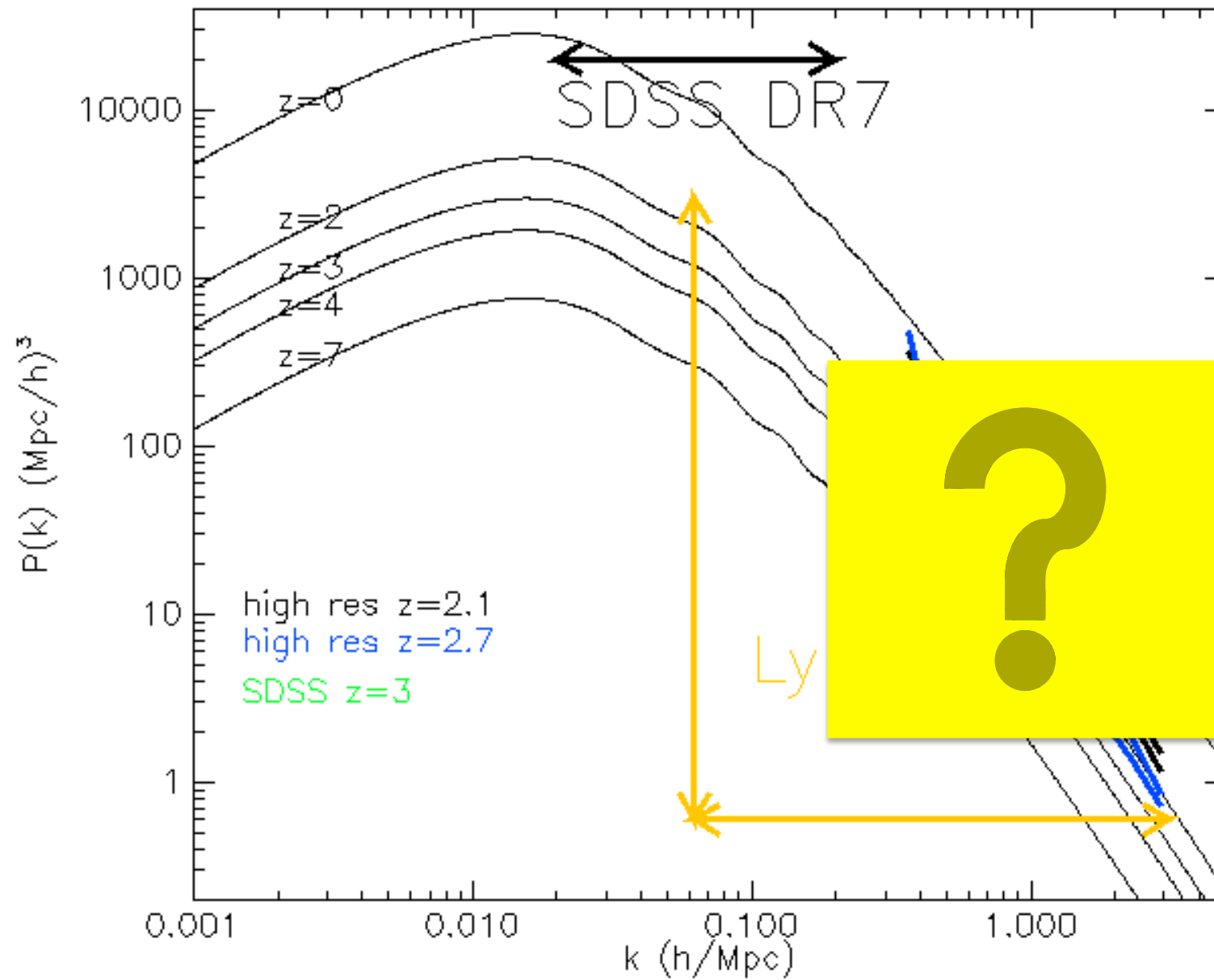
$$P_{\text{FLUX}}(k,z) = \text{bias}^2(k,z) \times P_{\text{MATTER}}(k,z)$$



DATA vs THEORY



DATA vs THEORY



END OF INTRO

We have characterized *the physics of the IGM*
and we can now fully exploit the fact that:

The IGM is a probe of matter fluctuations,
a laboratory for fundamental physics.
a sink (and a reservoir) for (of) galactic baryons

RESULTS FROM BOSS/SDSS-III

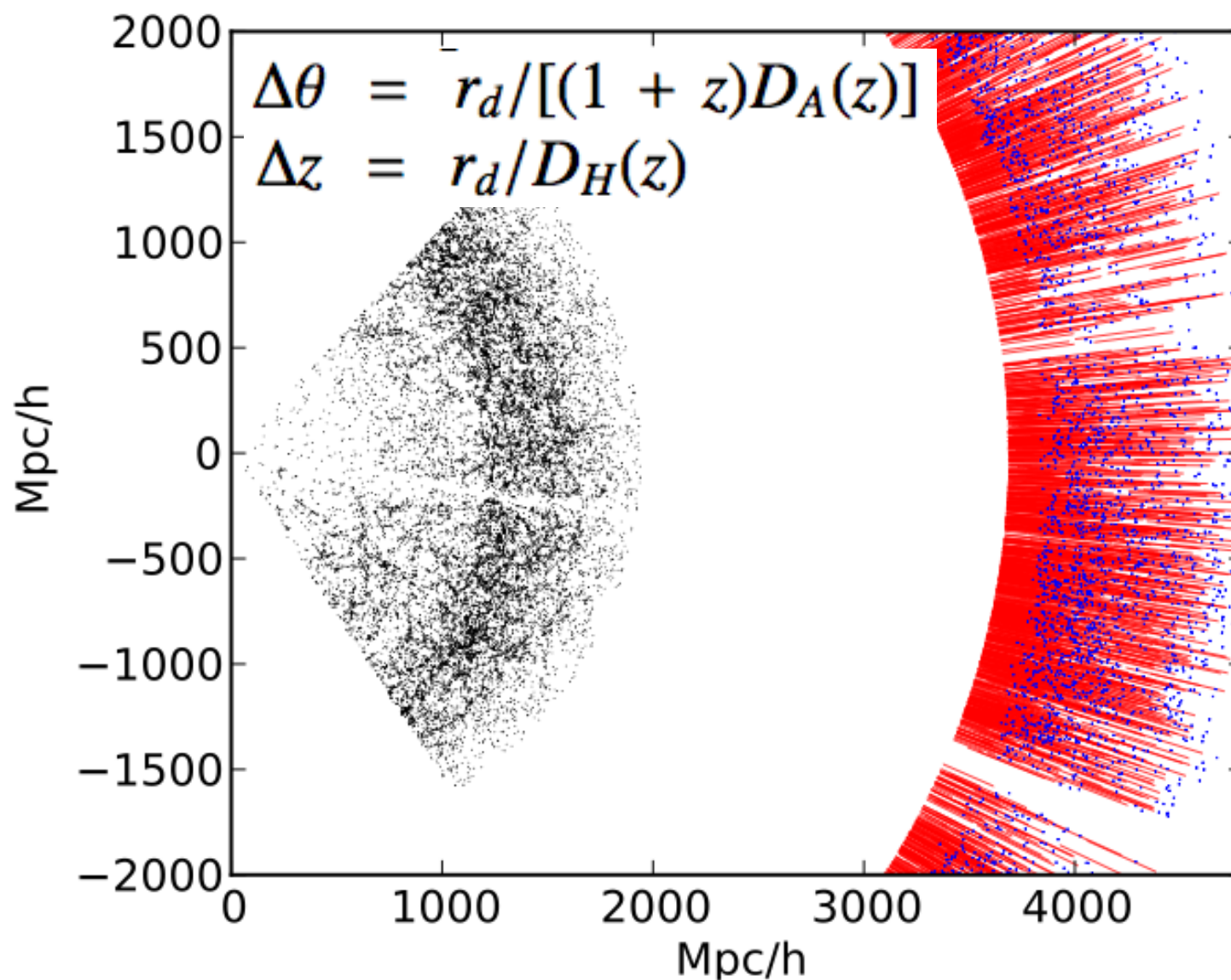
Geometrical and dynamical state of the Universe at $z = 2.3$

SDSS- I

New regime to be probed with Lyman- α forest in 3D



Slosar et al. 11
Busca et al. 13
Slosar et al. 13

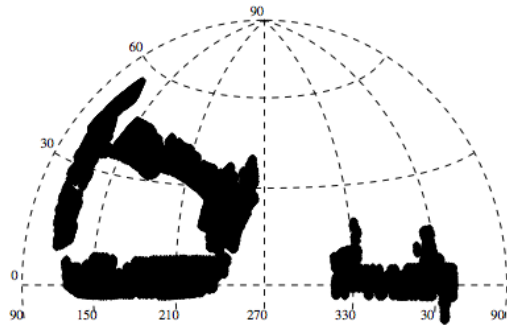


SDSS- II

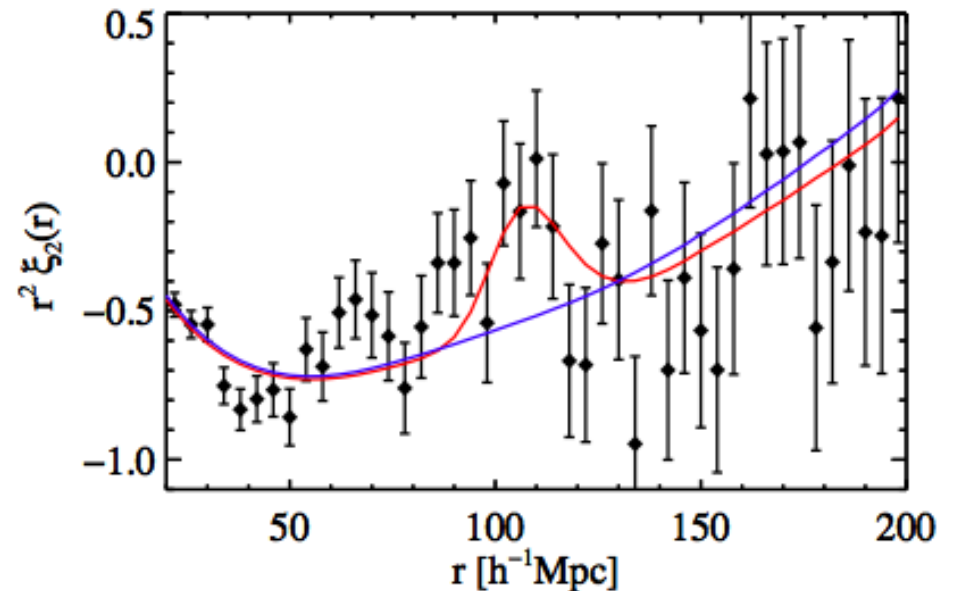
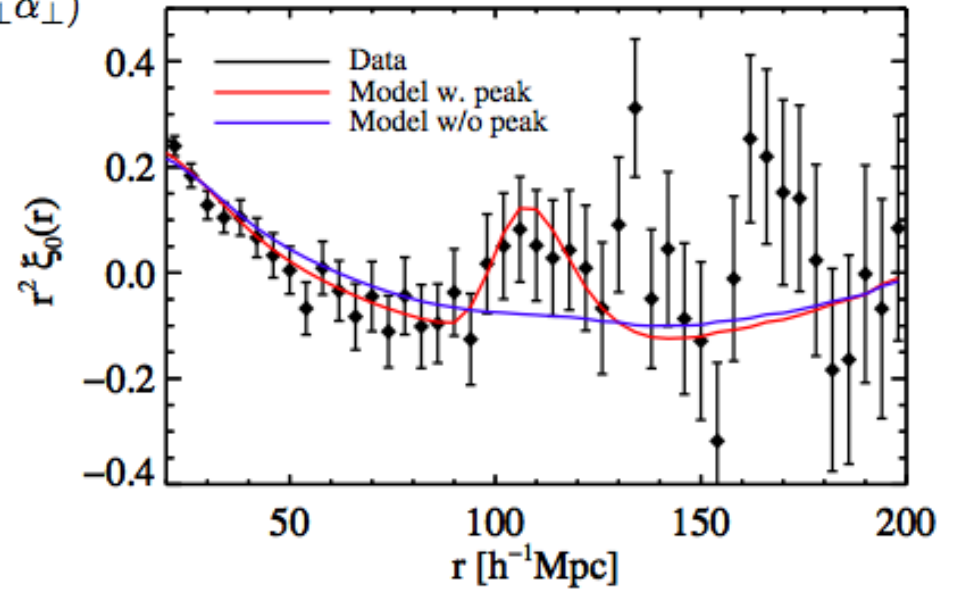
Busca et al. 13

$$\xi_{\text{cosmo}}(r_{\parallel}, r_{\perp}) = \xi_{\text{smooth}}(r_{\parallel}, r_{\perp}) + a_{\text{peak}} \cdot \xi_{\text{peak}}(r_{\parallel} \alpha_{\parallel}, r_{\perp} \alpha_{\perp})$$

$$\xi(r_{\parallel}, r_{\perp}) = \xi_{\text{cosmo}}(r_{\parallel}, r_{\perp}, \alpha_{\parallel}, \alpha_{\perp}) + \xi_{\text{bb}}(r_{\parallel}, r_{\perp})$$



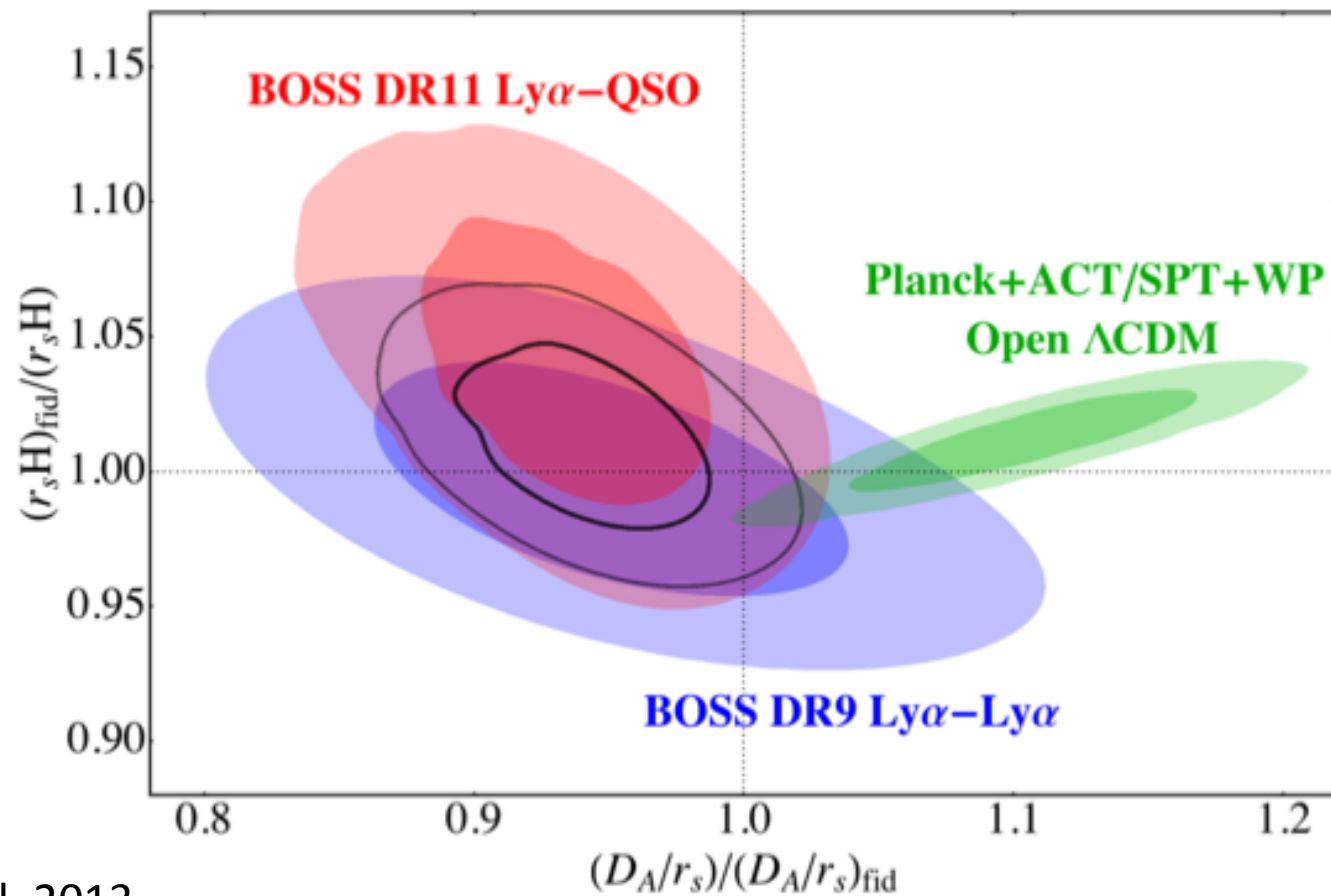
BAO feature detected at $z=2.3$
From 3000 deg², using 50000 QSOs
Significance of the detection at
around 3σ



SDSS- III

3D cross-correlation between Lyman- α flux and quasars

$$P_{qF}(\mathbf{k}) = b_q [1 + \beta_q \mu_k^2] b_F [1 + \beta_F \mu_k^2] P(k)$$

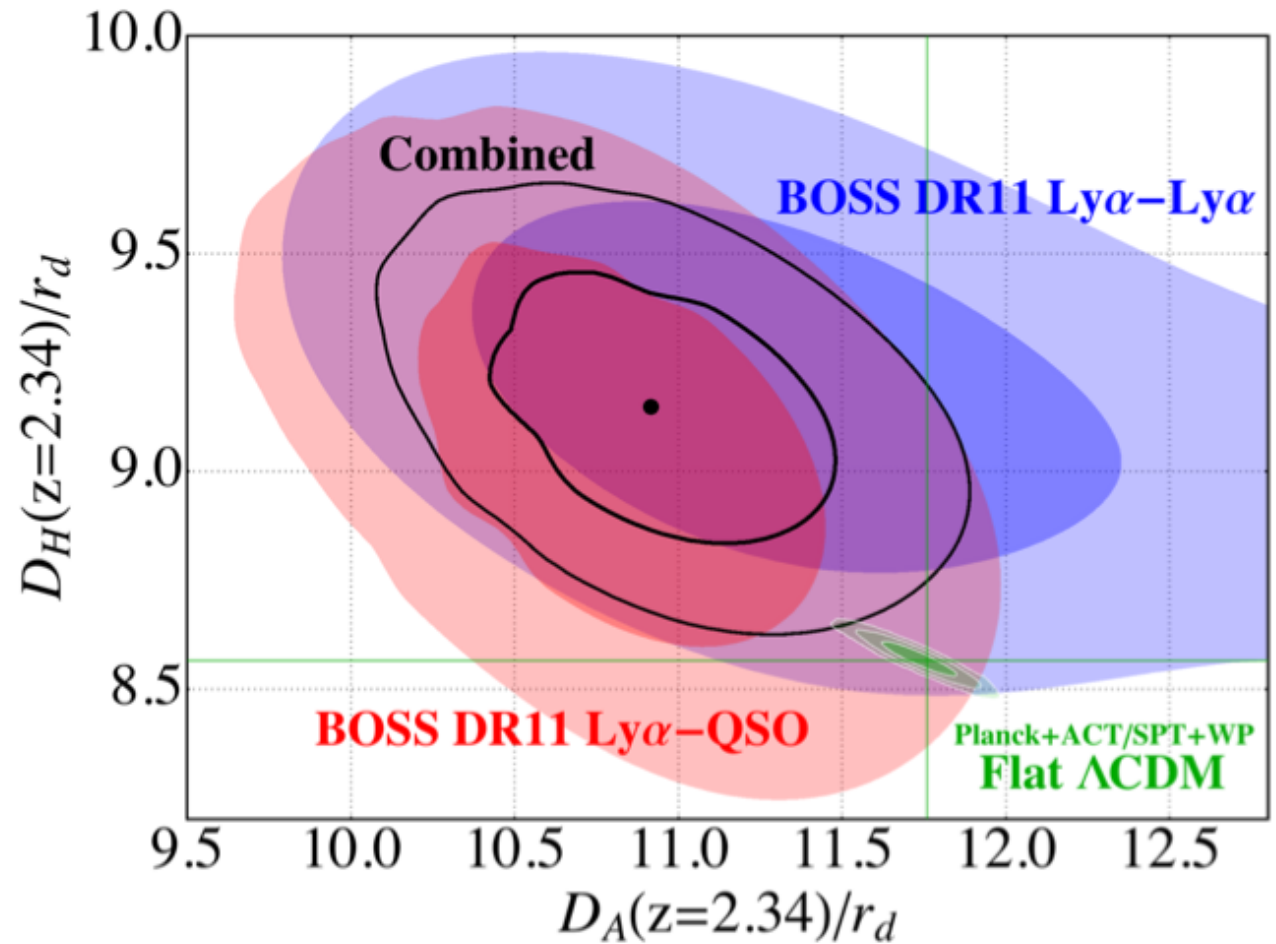


SDSS-IV

6% precision measurement
of D_A/r_d
3% precision measurement
of D_H/r_d

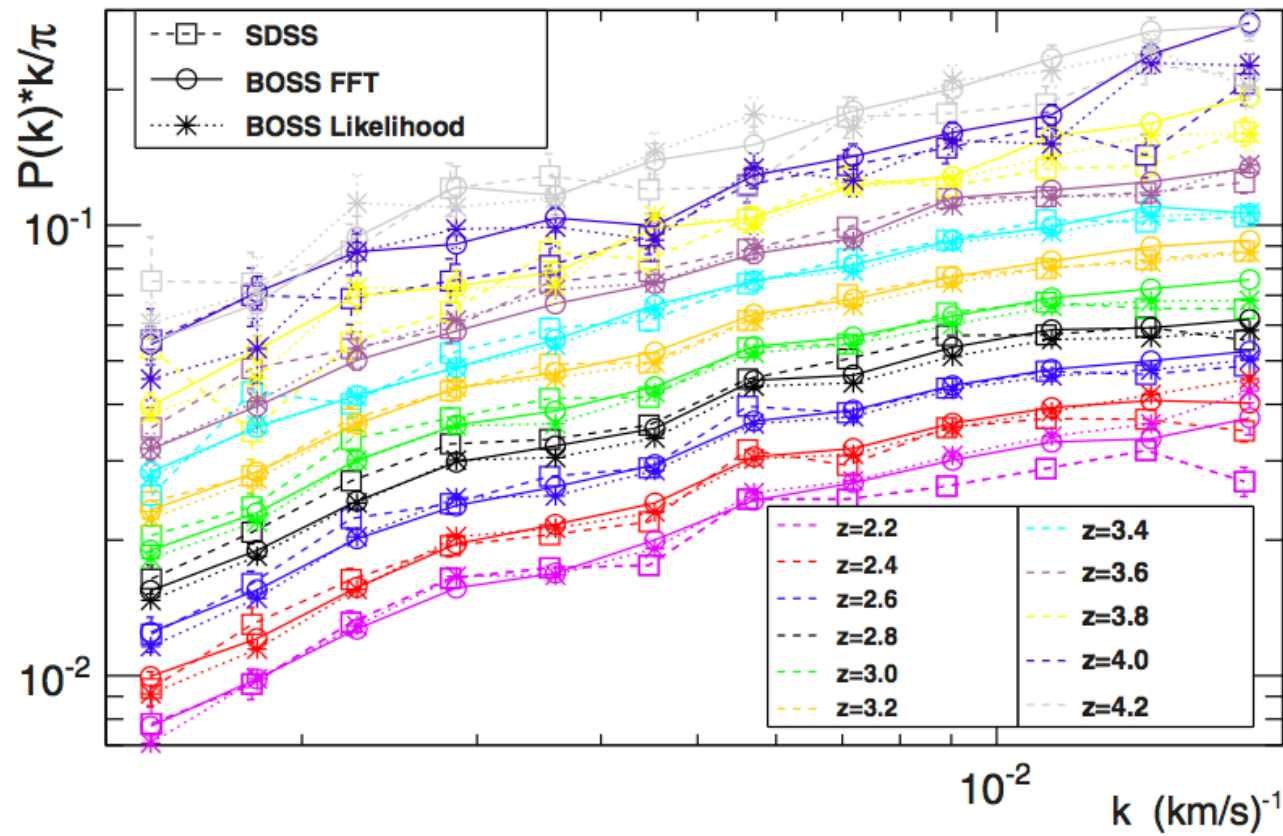
!

$$\frac{\rho_{\text{de}}(z = 2.34)}{\rho_{\text{de}}(z = 0)} = -1.2 \pm 0.8$$

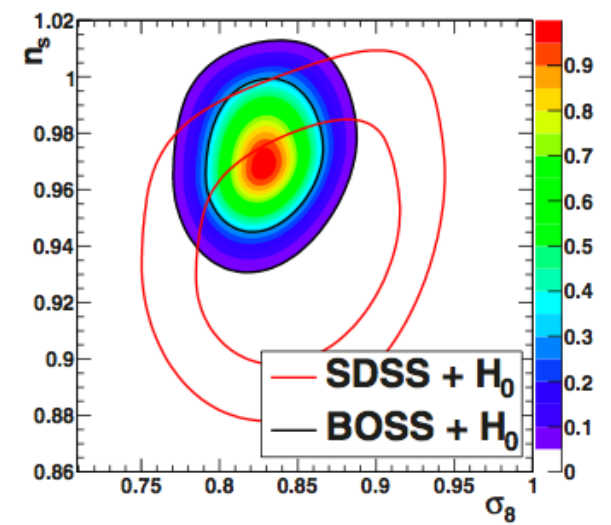


SDSS- IV

1D Lyman- α flux power



Palanque-Delabrouille et al. 2013



WHY LYMAN- α ???

1) ONE DIMENSIONAL

$$\langle \tilde{F}_k^2 \rangle = \frac{1}{(2\pi)^2} \int dk_x \int dk_y P(k_x, k_y, k) = \frac{1}{2\pi} \int_k^\infty P(y) y dy$$

e.g. Kaiser & Peacock 91

2) AND ALSO THREE DIMENSIONAL

$$P(k) = 2\pi \int_0^\infty dr_\perp r_\perp J_0(r_\perp \sqrt{k^2 - q^2}) \pi(q|r_\perp)$$

e.g. Viel et al. 02

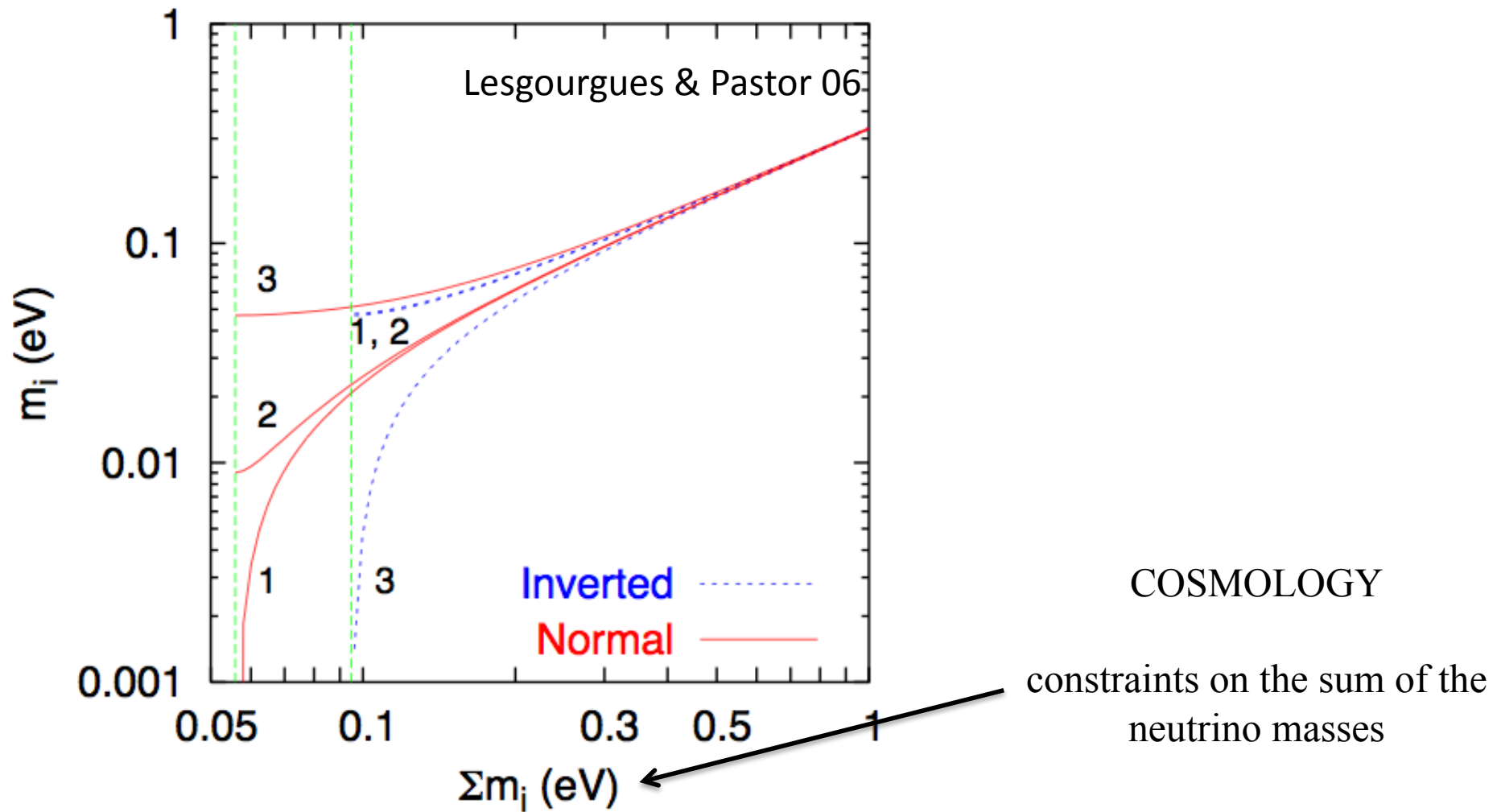
3) HIGH REDSHIFT

Where you are possibly closer to primordial $P(k)$

...unfortunately non-linearities and thermal state of the IGM are quite important....

CONSTRAINTS ON COSMOLOGICAL NEUTRINOS

COSMOLOGICAL NEUTRINOS - I: WHAT TO START FROM



$$0.056 \text{ (0.095) eV} \lesssim \sum_i m_i \lesssim 6 \text{ eV}$$

COSMOLOGICAL NEUTRINOS - II: FREE-STREAMING SCALE

Neutrino thermal
velocity

$$v_{\text{th}} \equiv \frac{\langle p \rangle}{m} \simeq \frac{3T_\nu}{m} = \frac{3T_\nu^0}{m} \left(\frac{a_0}{a} \right) \simeq 150(1+z) \left(\frac{1 \text{ eV}}{m} \right) \text{ km s}^{-1}$$

Neutrino free-streaming scale

$$k_{FS}(t) = \left(\frac{4\pi G \bar{\rho}(t) a^2(t)}{v_{\text{th}}^2(t)} \right)^{1/2}$$

Scale of non-relativistic transition

$$k_{\text{nr}} \simeq 0.018 \Omega_m^{1/2} \left(\frac{m}{1 \text{ eV}} \right)^{1/2} h \text{ Mpc}^{-1}$$

THREE
COSMIC
EPOCHS

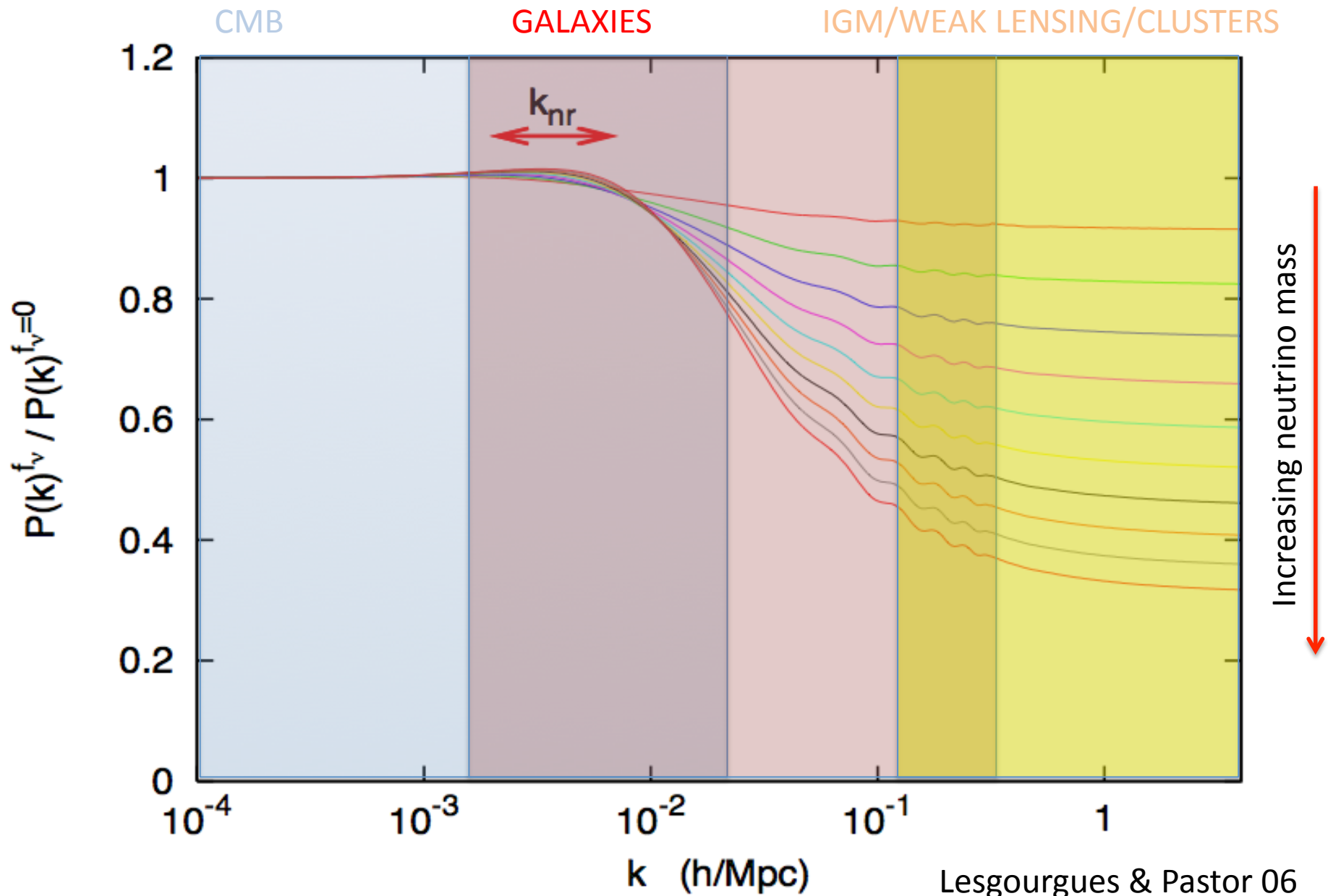
RADIATION ERA $z > 3400$

MATTER RADIATION $z < 3400$

NON-RELATIVISTIC TRANSITION $z \sim 500$

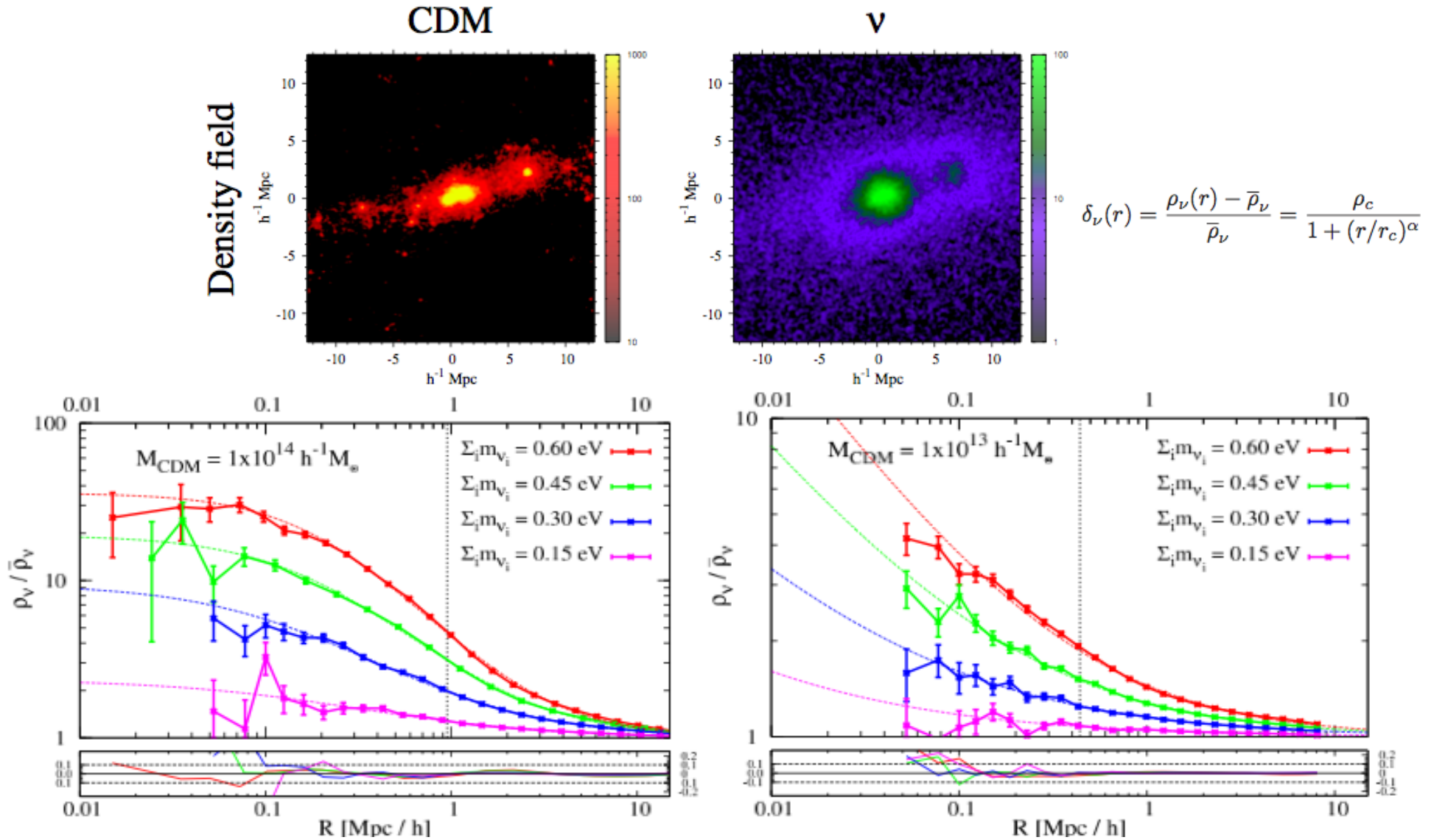
Below k_{nr} there is suppression in power at scales that are cosmologically important

COSMOLOGICAL NEUTRINOS - III: LINEAR MATTER POWER



MASSIVE NEUTRINOS

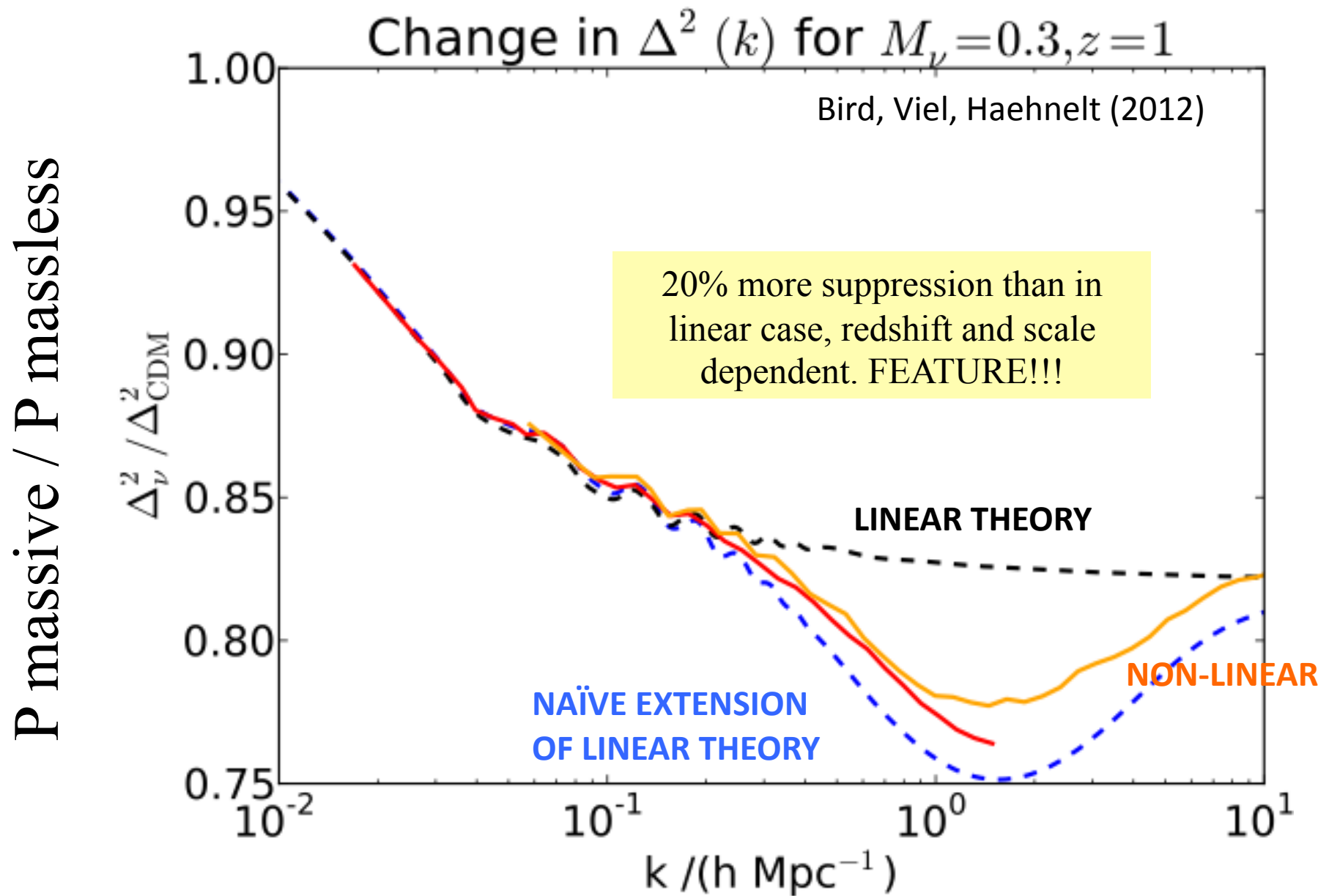
THE FUTURE: THE NEUTRINO HALO?



Villaescusa-Navarro, Bird, Garay, Viel, 2013, JCAP, 03, 019

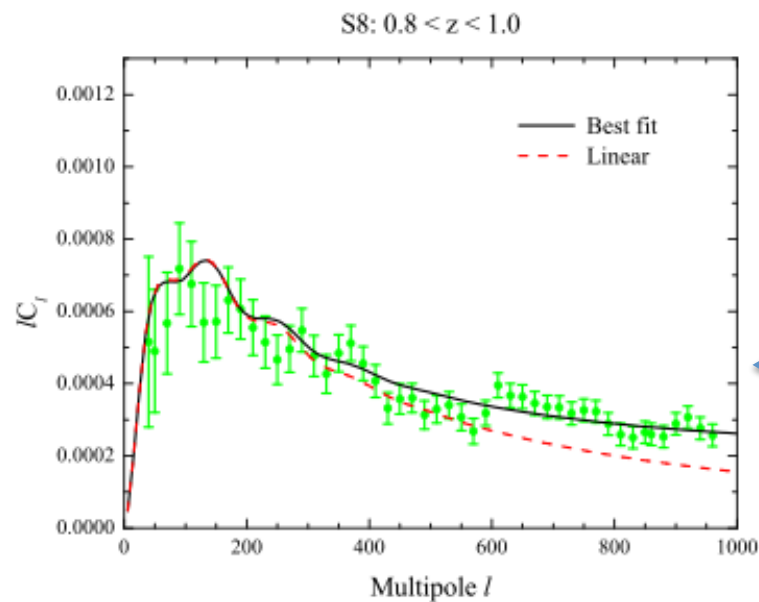
Marulli, Carbone, Viel+ 2011, MNRAS, 418, 346

COSMOLOGICAL NEUTRINOS : NON-LINEAR MATTER POWER

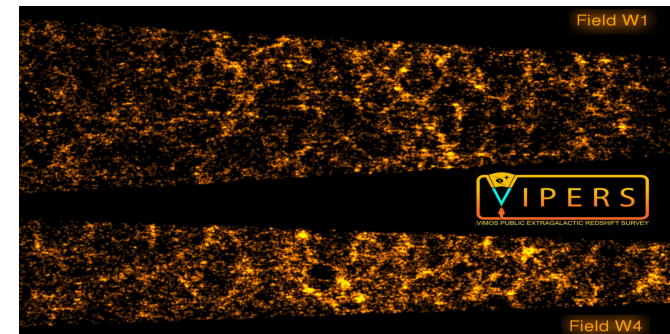
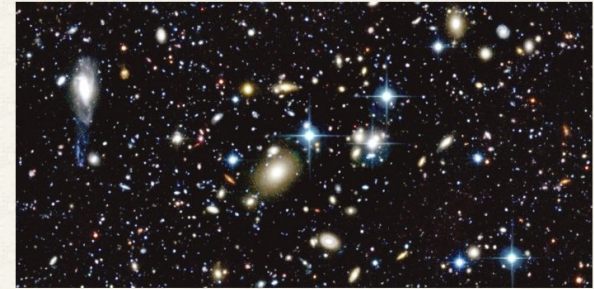


CONSTRAINTS on NEUTRINO MASSES USING NON-LINEARITIES

Xia, Granett, Viel, Bird, Guzzo+ 2012 JCAP, 06, 010



Canada-France-Hawaii Telescope
Legacy Survey

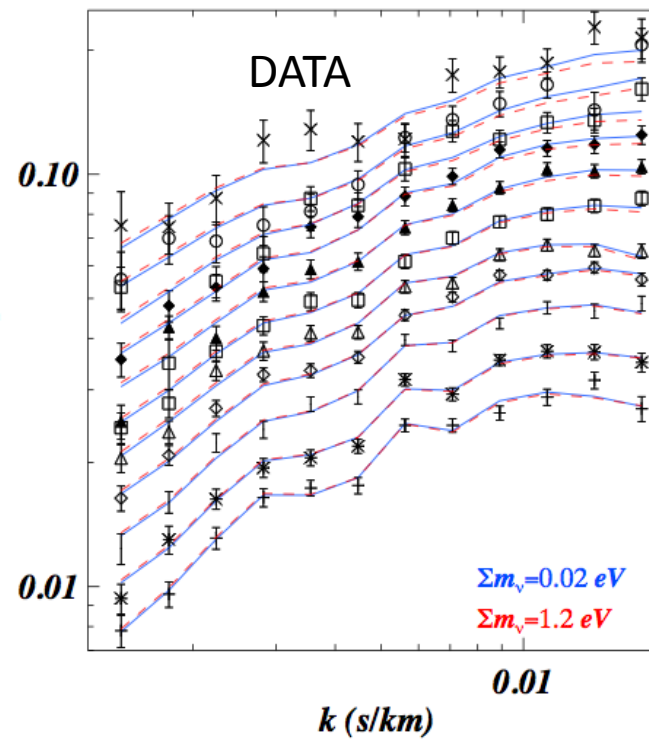
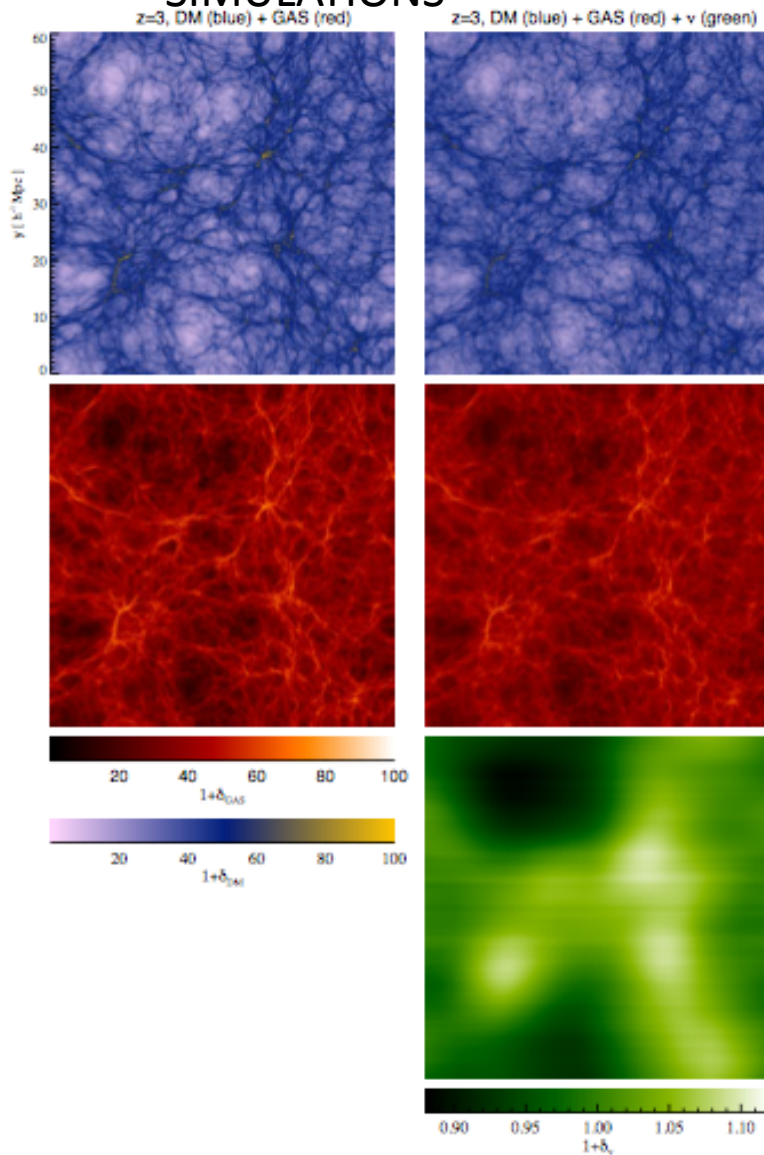


95% C.L. $\sum m_\nu$ [eV]	Without HST Prior		With HST Prior	
	$\ell_{\max} = 630$	$\ell_{\max} = 960$	$\ell_{\max} = 630$	$\ell_{\max} = 960$
WMAP7	1.17		0.50	
WMAP7 + CFHTLS	0.64	0.43	0.41	0.29
WMAP7 + SDSS + CFHTLS	0.47	0.35	0.35	0.28

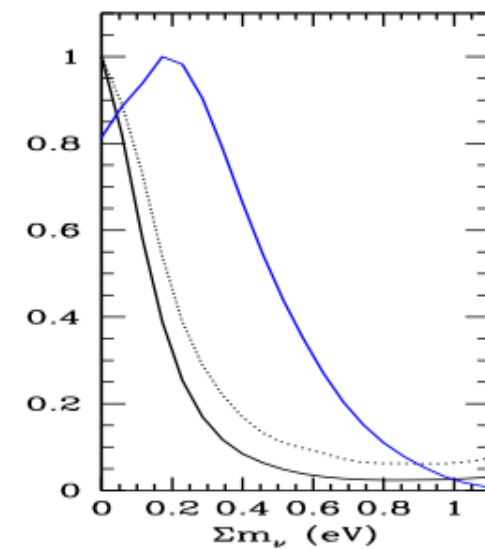
If using just linear 0.43eV – Improvement is about 20% when extending to non-linear 29

NEUTRINOS IN THE IGM

SIMULATIONS



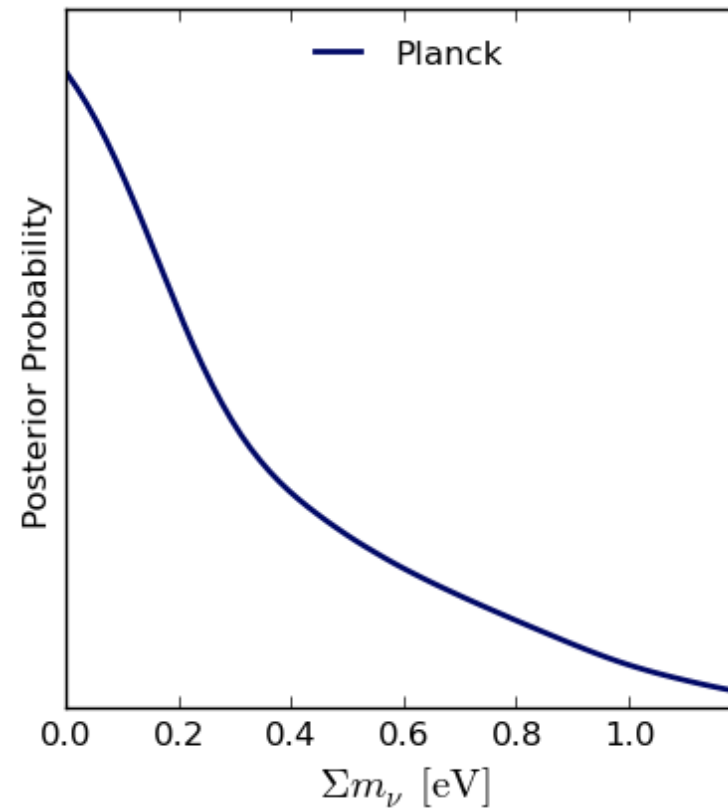
CONSTRAINTS



FROM IGM ONLY:
 $\Sigma m_\nu < 0.9 \text{ eV} (2\sigma)$

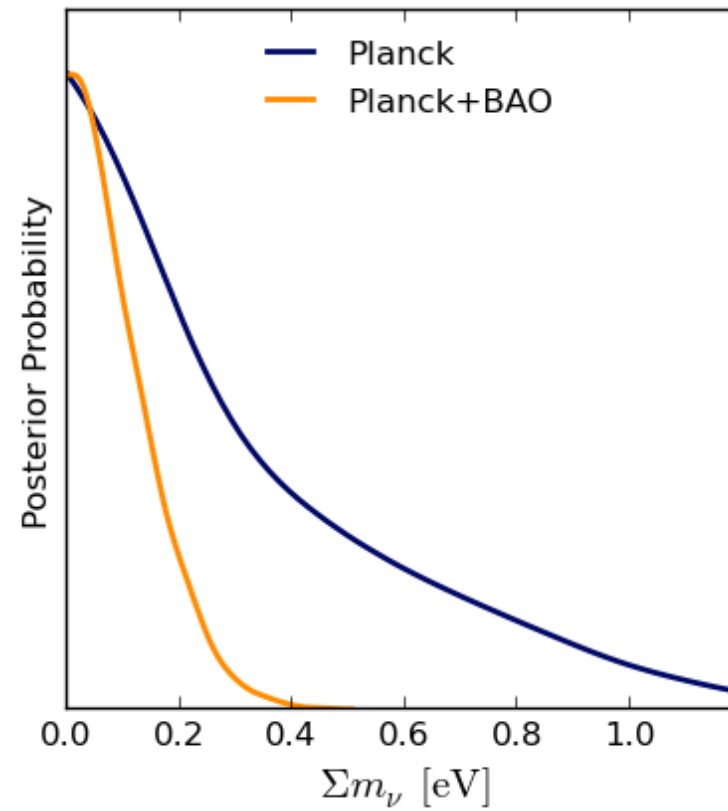
Viel, Haehnelt, Springel 2010

CONSTRAINTS on NEUTRINO MASSES FROM Planck: I



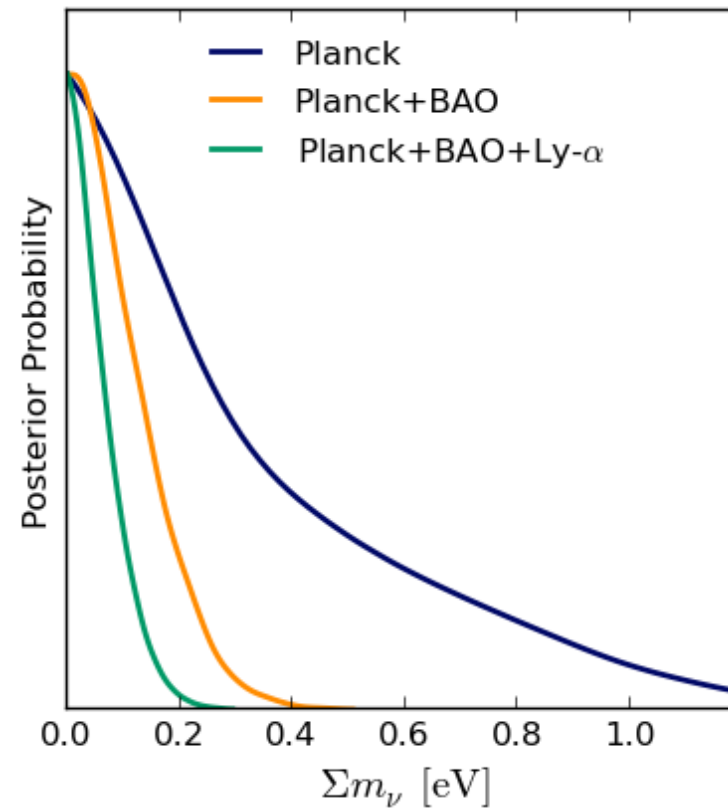
$$\Sigma m_\nu < 0.93 \text{ eV}(2\sigma)$$

CONSTRAINTS on NEUTRINO MASSES FROM Planck+BAO: II



$$\Sigma m_\nu < 0.24 \text{ eV} (2\sigma)$$

CONSTRAINTS on NEUTRINO MASSES FROM Planck+BAO+old Lya: III

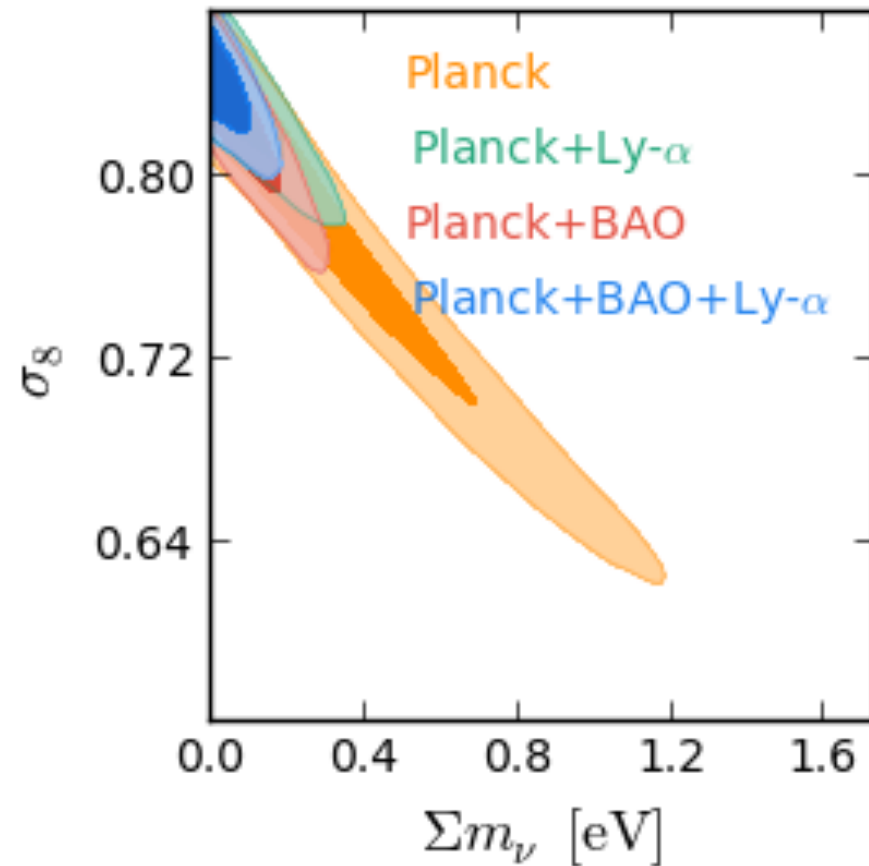


$$\Sigma m_\nu < 0.14 \text{ eV} (2\sigma)$$

CONSTRAINTS on NEUTRINO MASSES FROM Planck+BAO+old Lya: IV

2 σ upper limits

Planck:	$M_\nu < 0.93 \text{ eV}$
Planck+Lya:	$M_\nu < 0.27 \text{ eV}$
Planck+BAO:	$M_\nu < 0.24 \text{ eV}$
Planck+BAO+Ly α :	$M_\nu < 0.14 \text{ eV}$

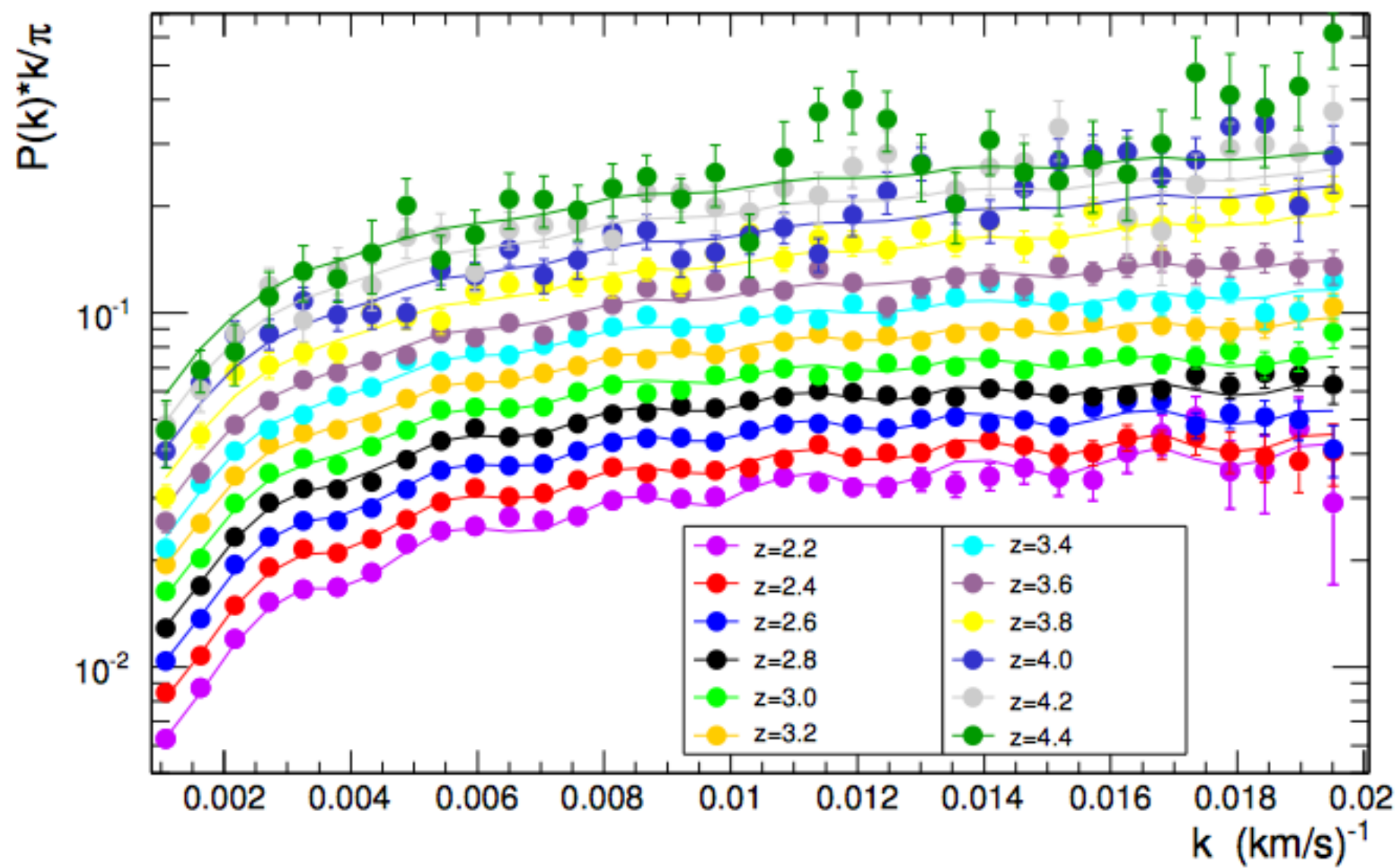


2 eV
29 eV
59 eV
9 eV

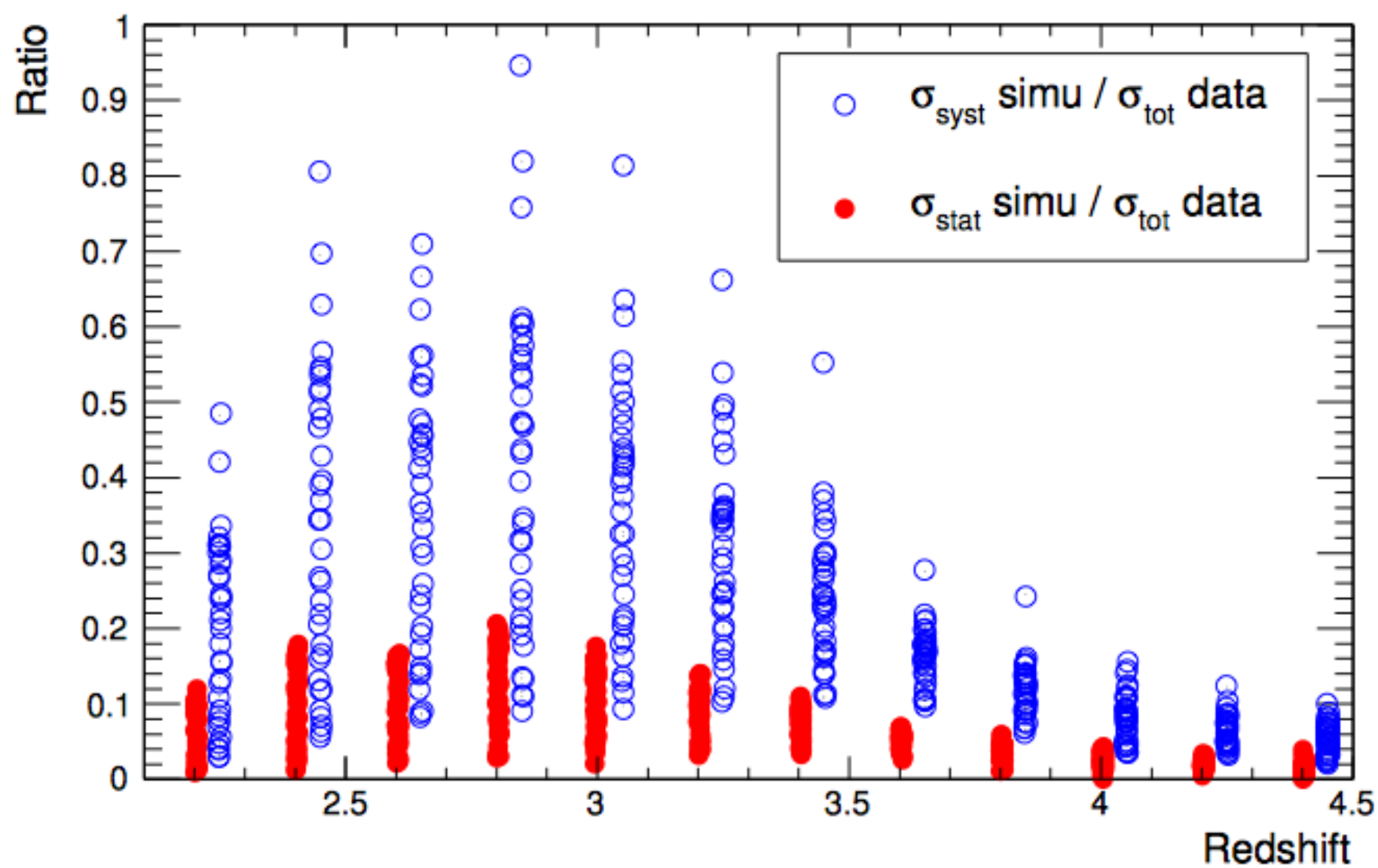
Constraint on neutrino masses from SDSS-III/BOSS $\text{Ly}\alpha$ forest and other cosmological probes

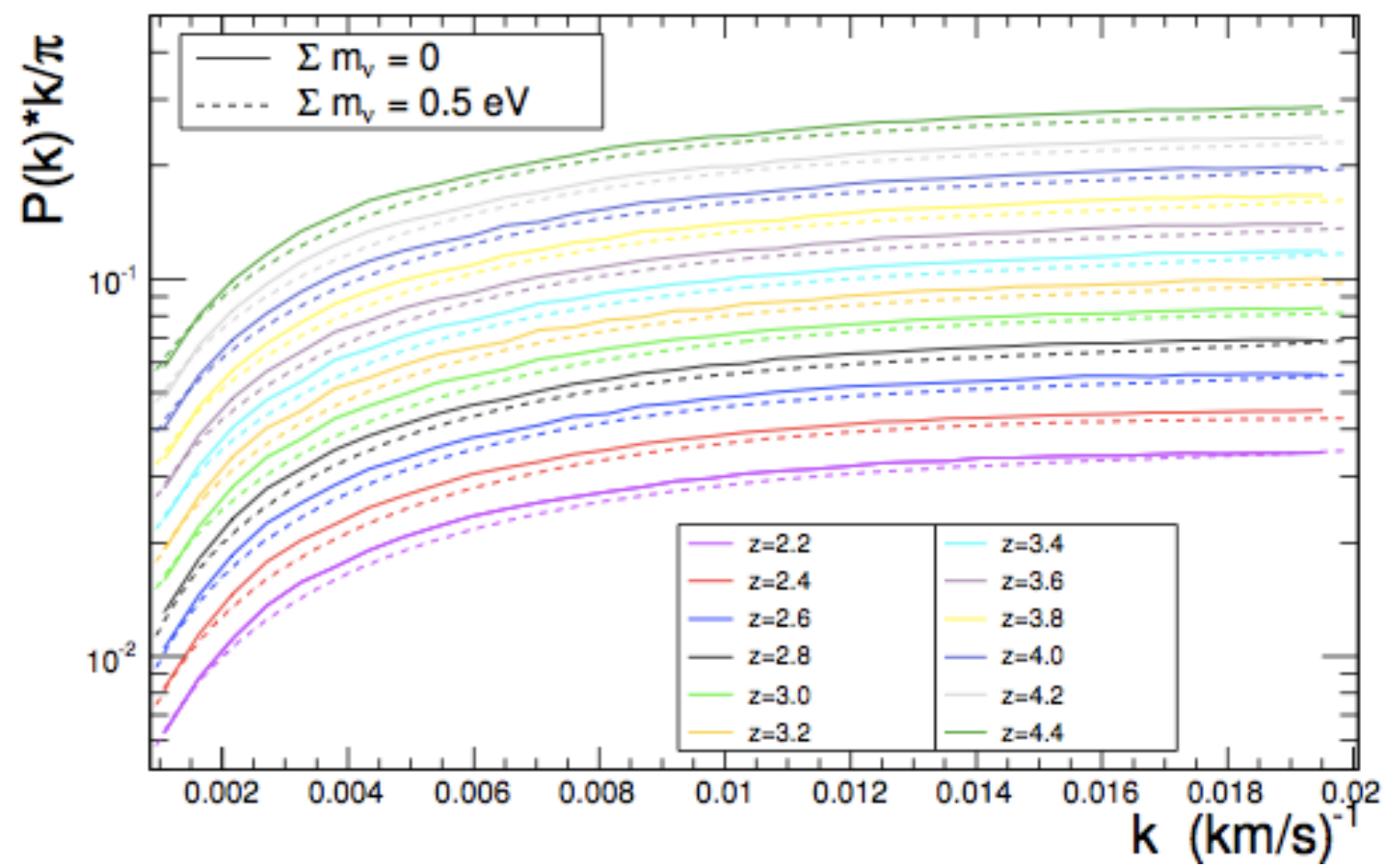
Nathalie Palanque-Delabrouille,^{a,b} Christophe Yèche,^a Julien Lesgourgues,^{c,d,e} Graziano Rossi,^{a,f} Arnaud Borde,^a Matteo Viel,^{g,h} Eric Aubourg,ⁱ David Kirkby,^j Jean-Marc LeGoff,^a James Rich,^a Natalie Roe,^b Nicholas P. Ross,^k Donald P. Schneider,^{l,m} David Weinbergⁿ

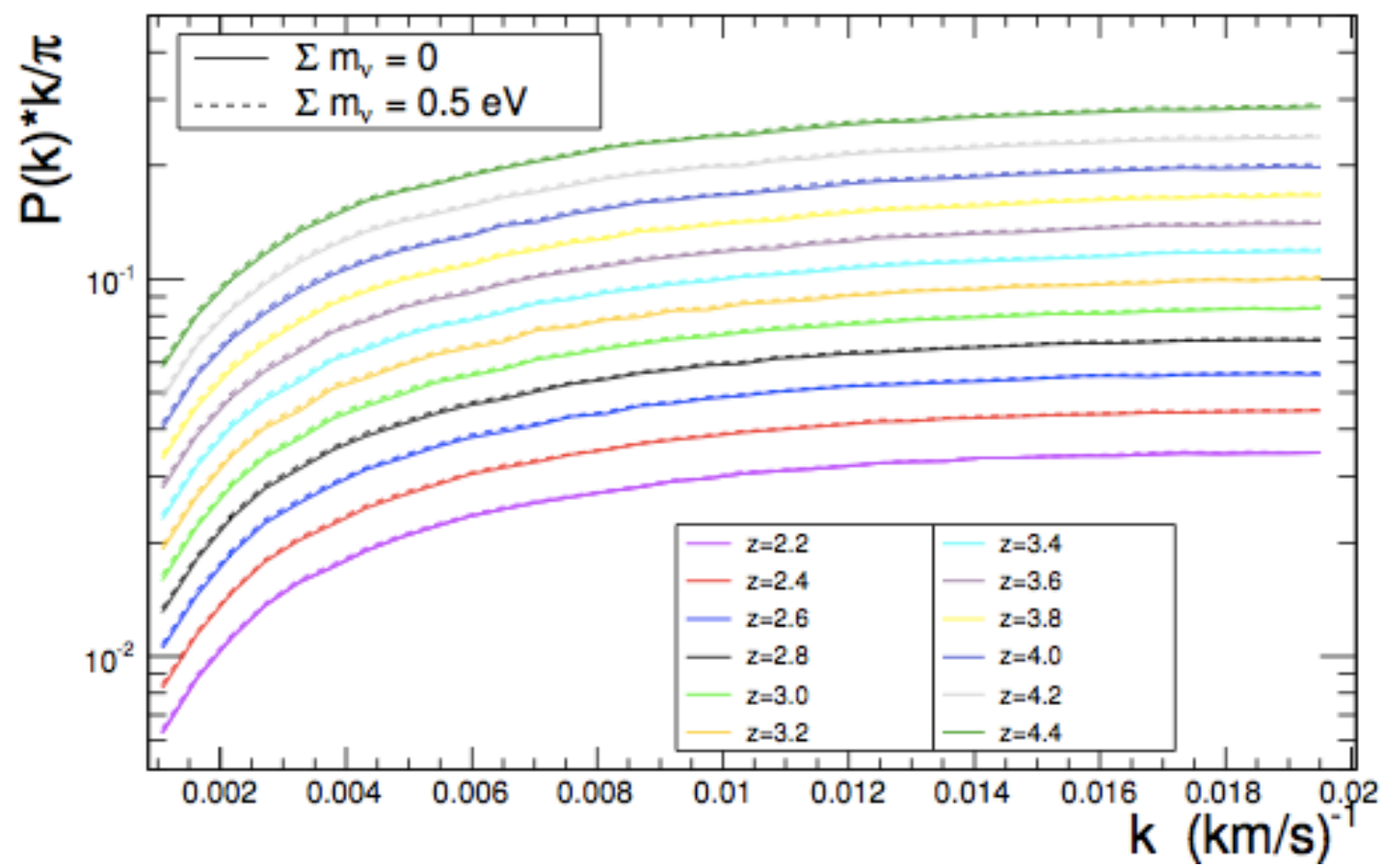
JCAP in press

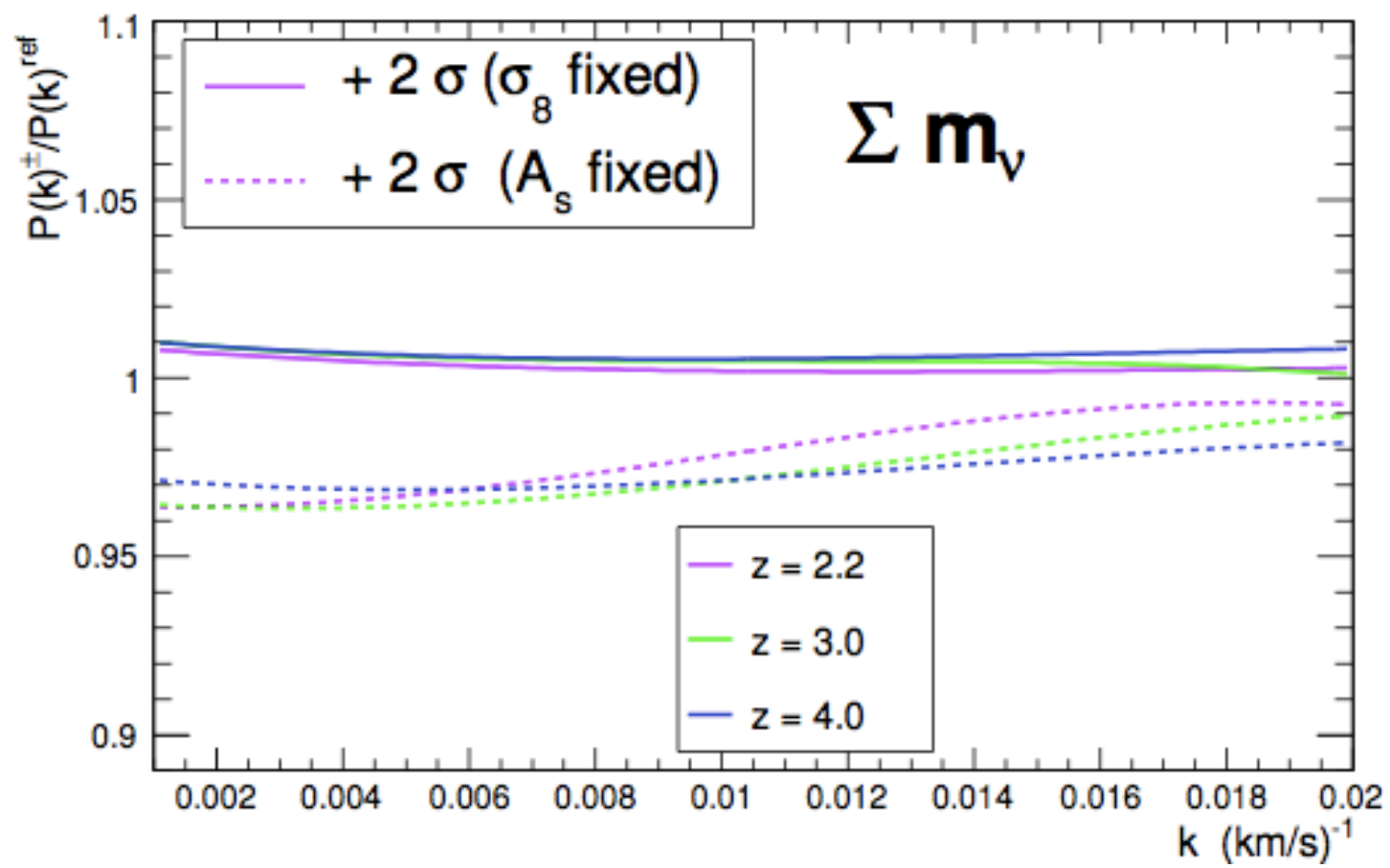


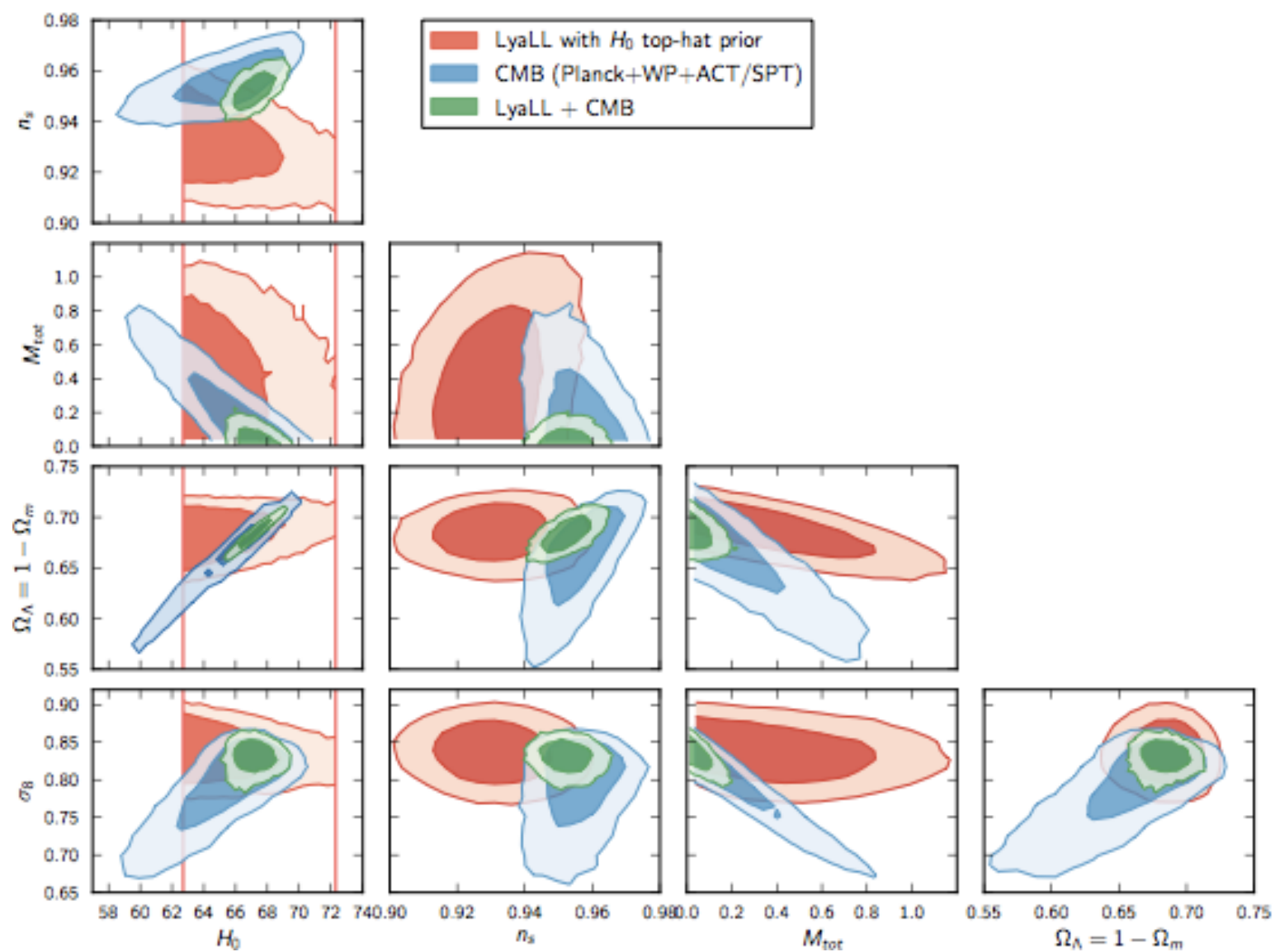
Parameter	Central value	Range
n_s	0.96	± 0.05
σ_8	0.83	± 0.05
Ω_m	0.31	± 0.05
H_0	67.5	± 5
$T_0(z = 3)$	14000	± 7000
$\gamma(z = 3)_{..}$	1.3	± 0.3
A^τ	0.0025	± 0.0020
η^τ	3.7	± 0.4
$\sum m_\nu$ (eV)	0.0	0.4, 0.8

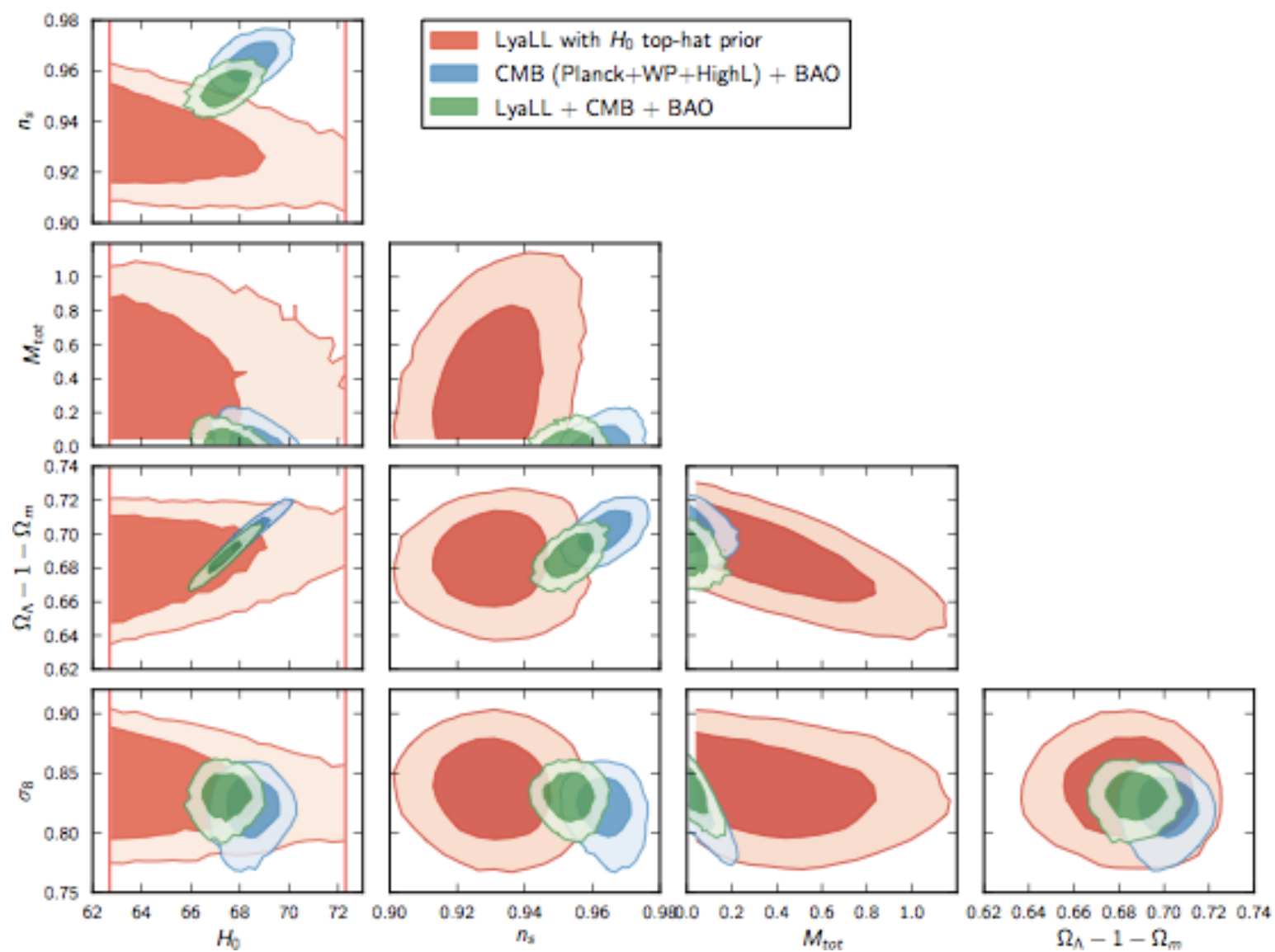




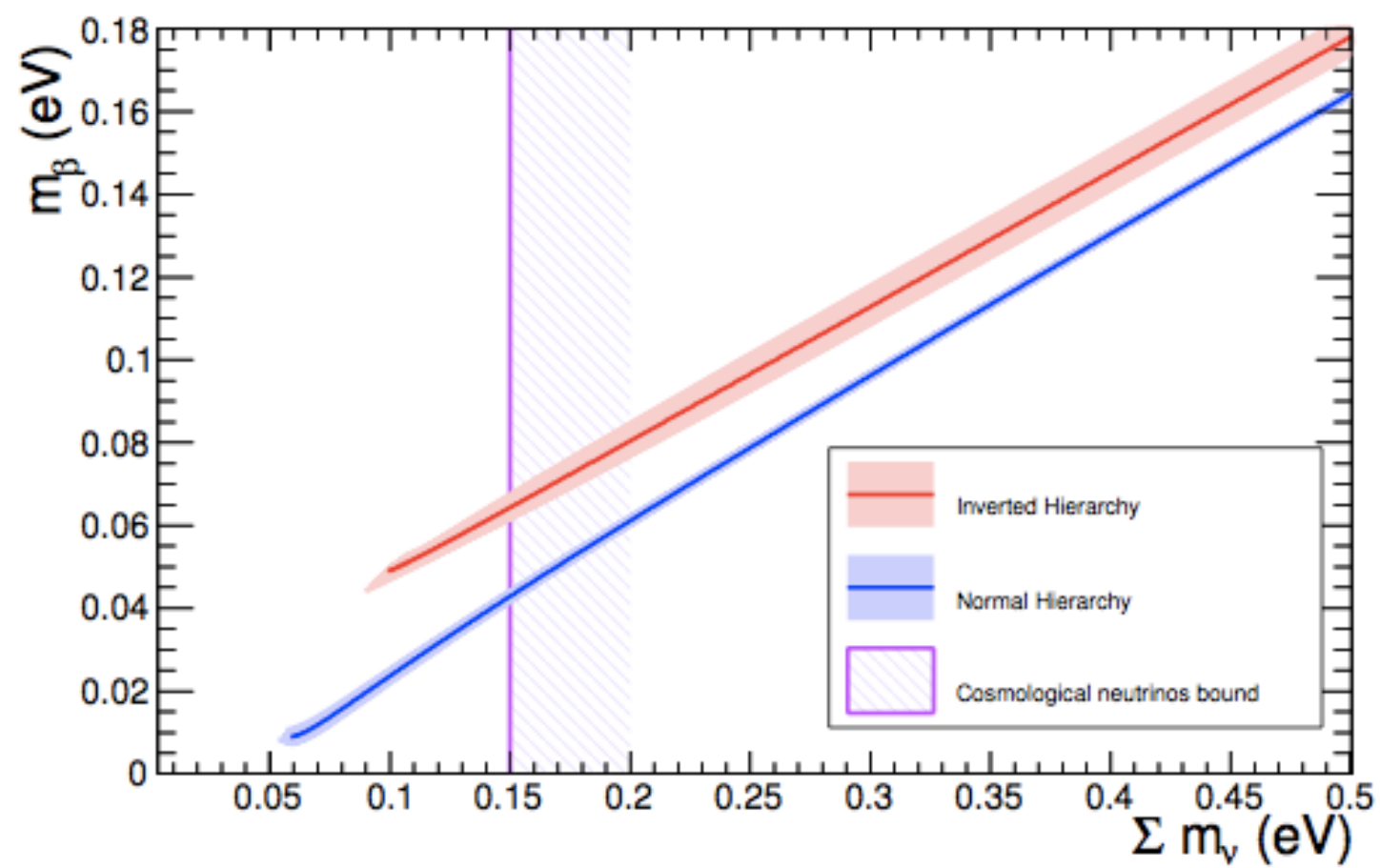


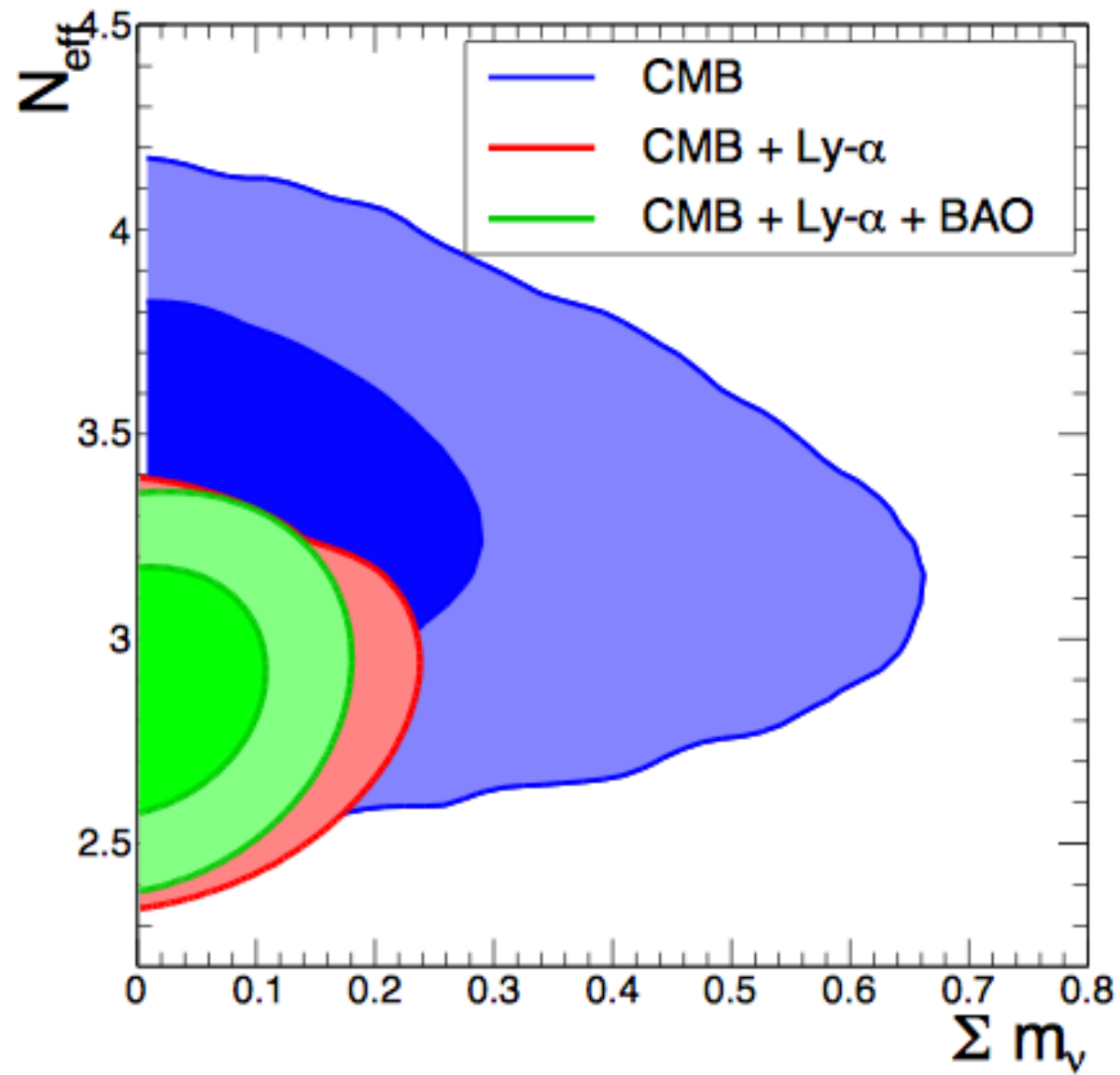






Parameter	$\text{Ly}\alpha + H_0^{\text{tophat}}$ ($62.5 \leq H_0 < 72.5$)	$\text{Ly}\alpha + \text{CMB}$	$\text{Ly}\alpha + \text{CMB}$ + BAO	$\text{Ly}\alpha + \text{CMB}(A_L)$
$10^9 A_s$	$3.2^{+0.5}_{-0.7}$	$2.20^{+0.05}_{-0.06}$	$2.20^{+0.05}_{-0.06}$	$2.18^{+0.05}_{-0.06}$
$10^2 \omega_b$	(fixed to 2.22)	2.20 ± 0.02	2.20 ± 0.02	2.22 ± 0.03
ω_{cdm}	$0.110^{+0.008}_{-0.013}$	$0.1200^{+0.0019}_{-0.0018}$	$0.1196^{+0.0015}_{-0.0014}$	0.1191 ± 0.002
τ_{reio}	(irrelevant)	$0.091^{+0.012}_{-0.013}$	$0.091^{+0.011}_{-0.013}$	$0.0871^{+0.012}_{-0.013}$
n_s	0.931 ± 0.012	0.953 ± 0.005	0.953 ± 0.005	$0.955^{+0.005}_{-0.006}$
H_0	< 70.9 (95%)	$67.2^{+0.8}_{-0.9}$	67.4 ± 0.7	$67.5^{+1.0}_{-1.1}$
$\sum m_\nu$ (eV)	< 0.98 (95%)	< 0.16 (95%)	< 0.14 (95%)	< 0.21 (95%)
A_L	(fixed to 1)	(fixed to 1)	(fixed to 1)	1.12 ± 0.10
σ_8	0.84 ± 0.03	$0.830^{+0.017}_{-0.013}$	$0.830^{+0.016}_{-0.012}$	$0.818^{+0.021}_{-0.014}$
Ω_m	$0.316^{+0.018}_{-0.021}$	0.316 ± 0.012	0.313 ± 0.009	0.312 ± 0.013





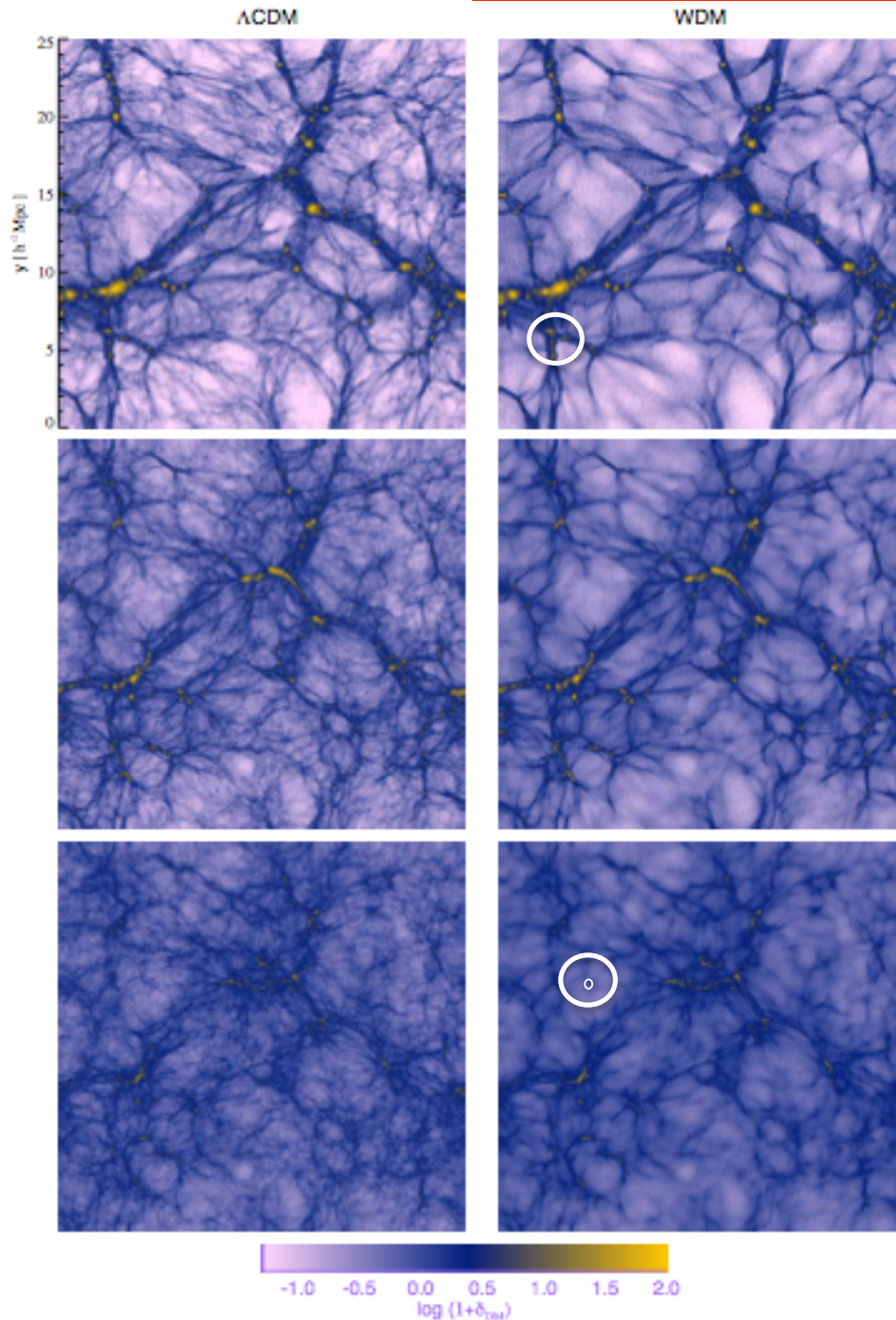
Rossi et al. arXiv 1412.6763

$$N_{\text{eff}} = 2.88 \pm 0.20$$

THE COLDNESS OF COLD DARK MATTER

Viel, Becker, Bolton, Haehnelt, 2013, PRD, 88, 043502

THE COSMIC WEB in WDM/LCDM scenarios



$$z=0 \quad \frac{T_x}{T_\nu} = \left(\frac{10.75}{g_*(T_D)} \right)^{1/3} < 1$$

$$k_{\text{FS}} = \frac{2\pi}{\lambda_{\text{FS}}} \sim 5 \text{ Mpc}^{-1} \left(\frac{m_x}{1 \text{ keV}} \right) \left(\frac{T_\nu}{T_x} \right)$$

$$\omega_x = \Omega_x h^2 = \beta \left(\frac{m_x}{94 \text{ eV}} \right)$$

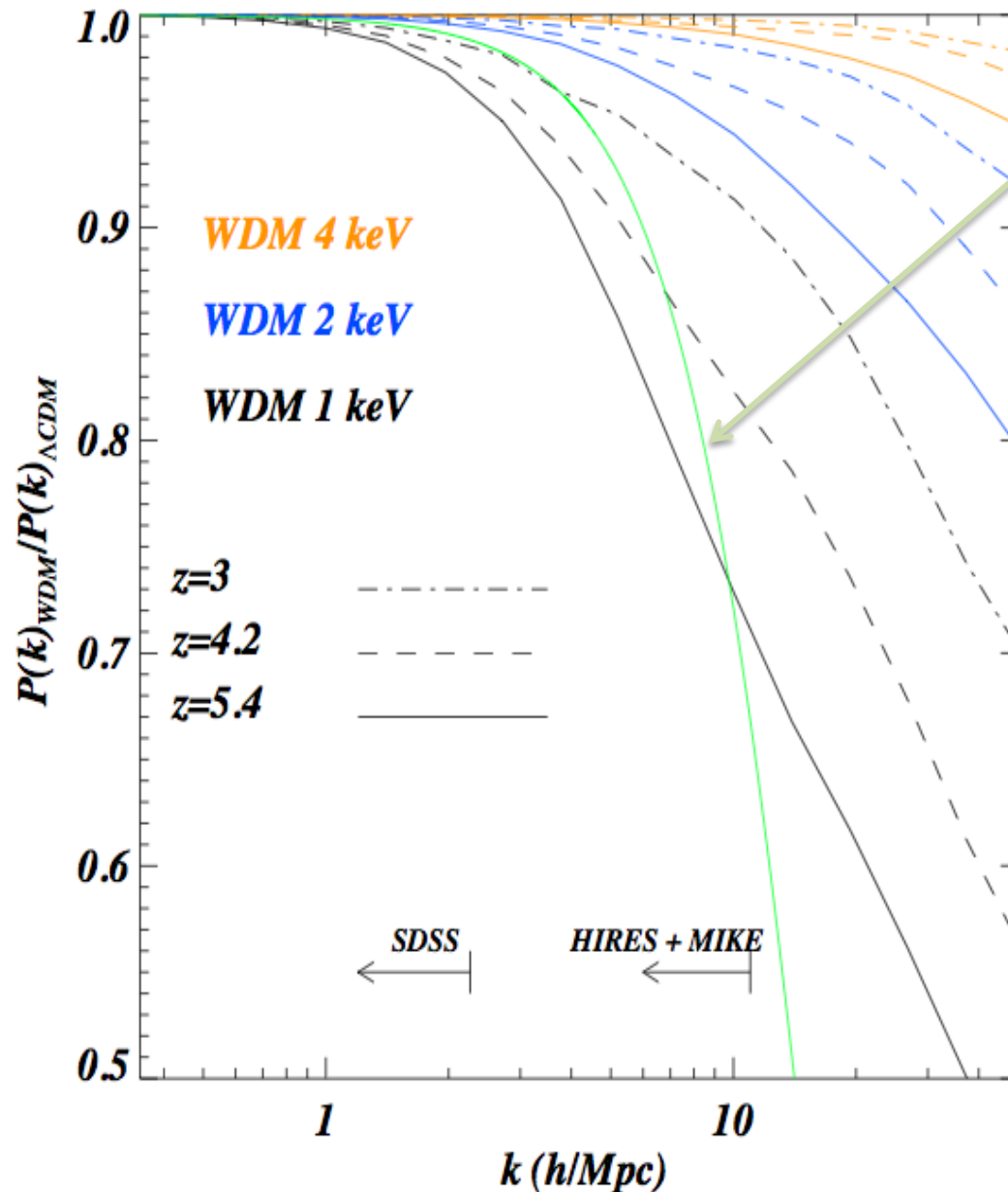
$$\beta = (T_x/T_\nu)^3$$

$$z=2$$

$$k_{\text{FS}} \sim 15.6 \frac{h}{\text{Mpc}} \left(\frac{m_{\text{WDM}}}{1 \text{ keV}} \right)^{4/3} \left(\frac{0.12}{\Omega_{\text{DM}} h^2} \right)^{1/3}$$

$$z=5$$

THE WARM DARK MATTER CUTOFF IN THE MATTER DISTRIBUTION



Linear cutoff for WDM 2 keV

Linear cutoff is redshift independent

Fit to the non-linear cut-off

$$T_{\text{nl}}^2(k) \equiv P_{\text{WDM}}(k)/P_{\Lambda\text{CDM}}(k) = (1 + (\alpha k)^{\nu l})^{-s/\nu},$$

$$\alpha(m_{\text{WDM}}, z) = 0.0476 \left(\frac{1\text{keV}}{m_{\text{WDM}}} \right)^{1.85} \left(\frac{1+z}{2} \right)^{1.3},$$

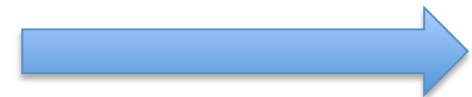
$\nu = 3, l = 0.6$ and $s = 0.4$.

Viel, Markovic, Baldi & Weller 2013

IMPLICATIONS FOR STRUCTURE FORMATION

- | | |
|---|---|
| - Strong and weak lensing | Markovic et al. 13/Faadely & Keeton 12 |
| - Galaxy formation | Menci et al 13, Kang et al. 13 |
| - Reionization/First Stars | Gao & Theuns 07 |
| - Dark Matter Haloes (mass functions) | Pacucci et al. 13 |
| - Luminous matter properties | Polisensky & Ricotti 11, Lovell et al. 09 |
| - Gamma-Ray Bursts | De Souza et al. 13 |
| - HI in the local Universe | Zavala et al. 09 |
| - Phase space density constraints | Shi et al. 13 |
| - Radiative decays in the high-z universe | Boyarsky et al. 13 |

+ **Lyman $-\alpha$**



HISTORY OF WDM LYMAN- α BOUNDS

Narayanan et al. 00 : $m > 0.75$ keV

Nbody sims + 8 Keck spectra
Marginalization over nuisance not done

Viel et al. 05 : $m > 0.55$ keV (2σ)

Hydro sims + 30 UVES/VLT spectra
Effective bias method of Croft et al. 02

Seljak et al. 06 : $m > 2.5$ keV (2σ)

Hydro Particle Mesh method + SDSS
grid of simulation for likelihood

Viel et al. 06 : $m > 2$ keV (2σ)

Fully hydro+SDSS
Not full grid of sims. but Taylor expans.

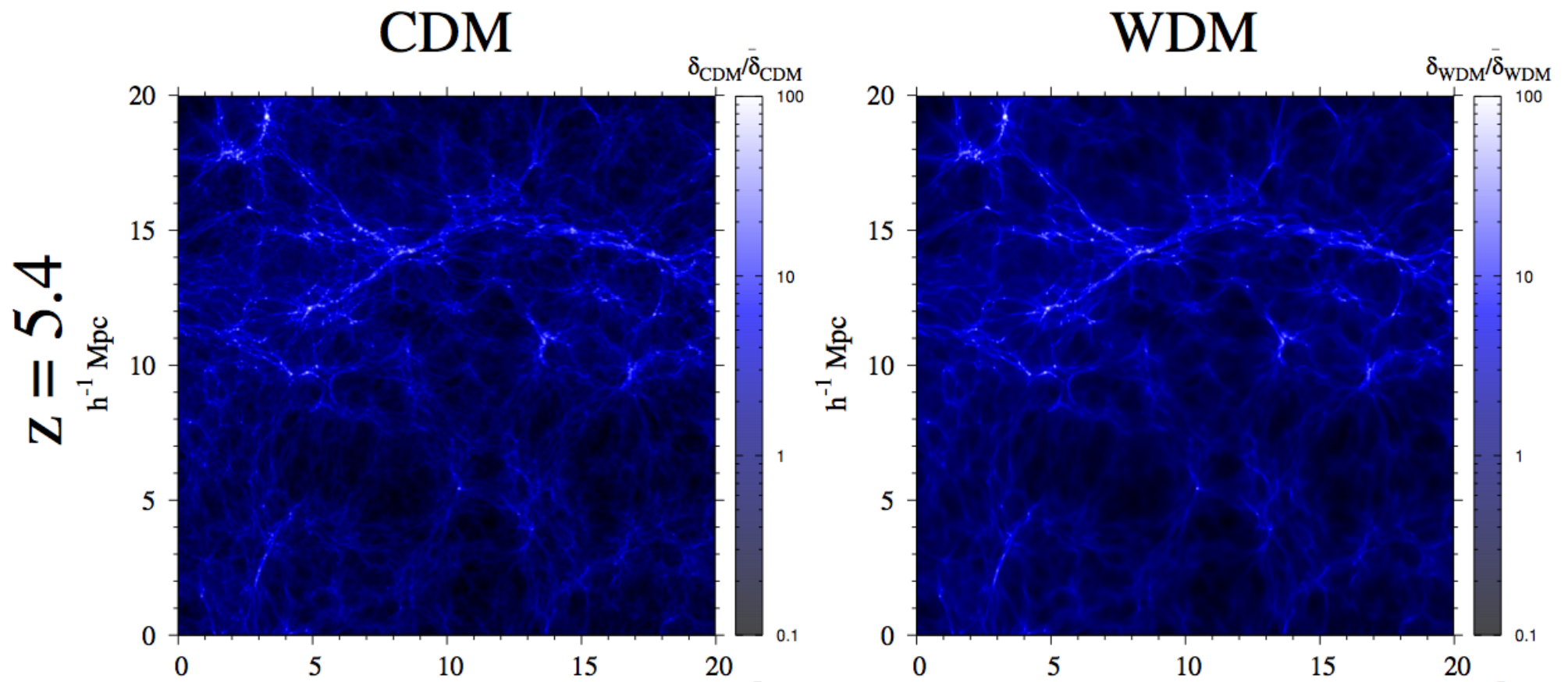
Viel et al. 08 : $m > 4.5$ keV (2σ)

SDSS+HIRES (55 QSOs spectra)
Full hydro sims (Taylor expansion of the flux)

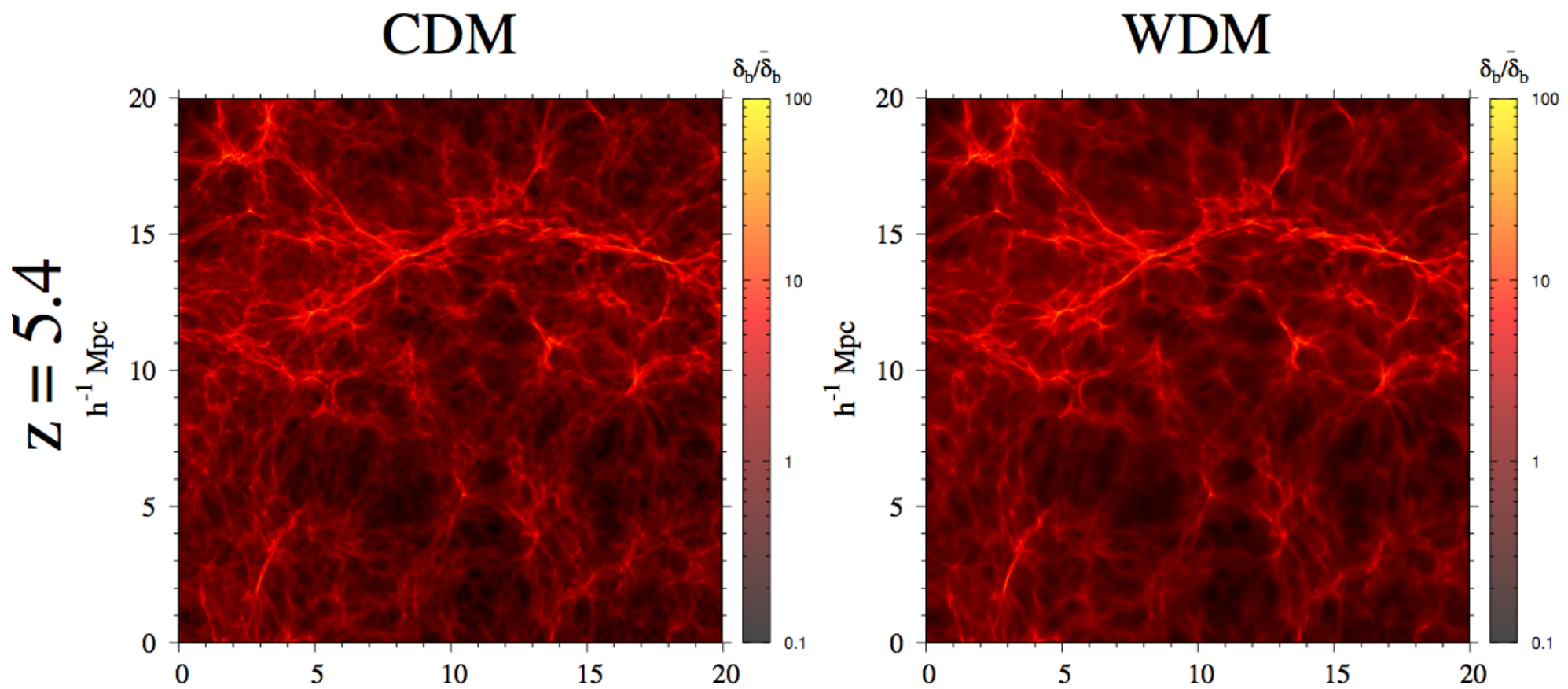
Boyarsky et al. 09 : $m > 2.2$ keV (2σ)

SDSS (frequentist+bayesian analysis)
emphasis on mixed ColdWarmDM models

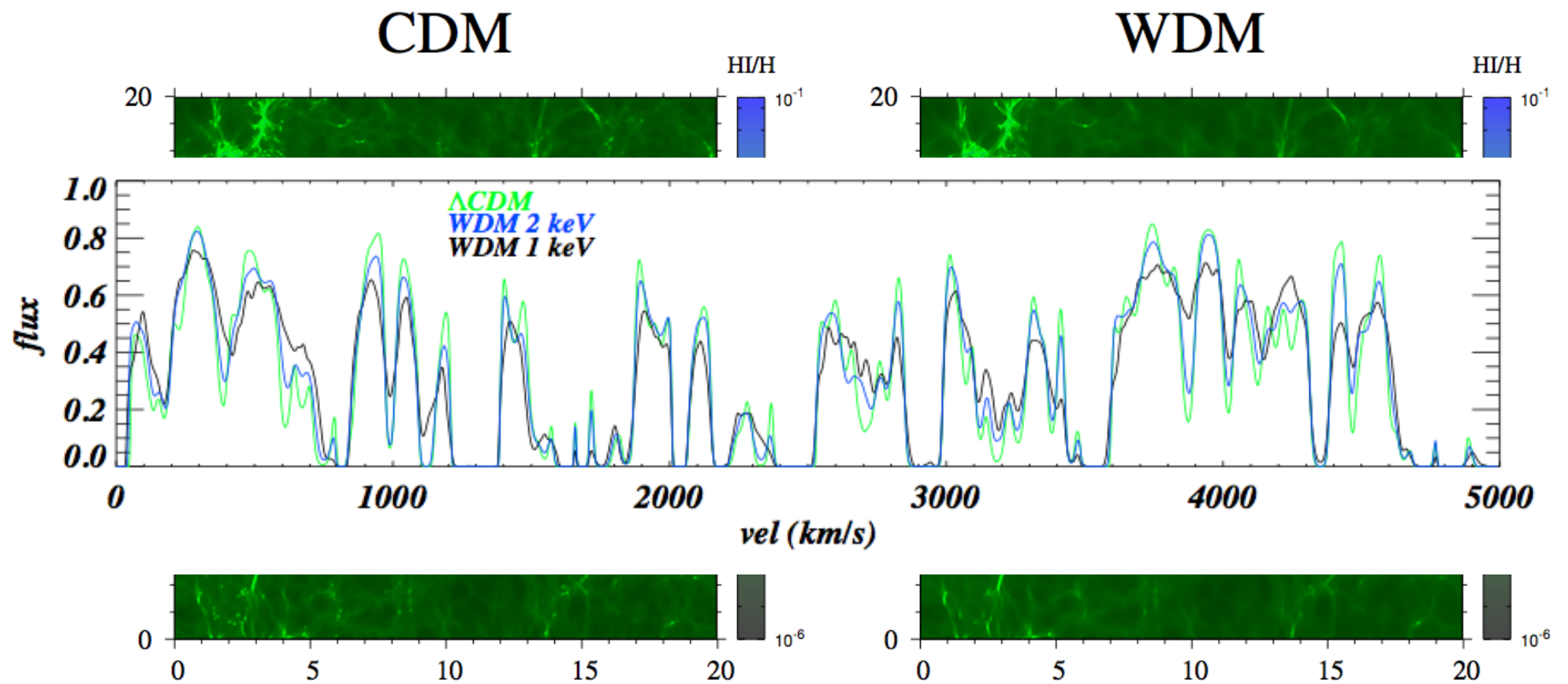
DARK MATTER DISTRIBUTION



GAS DISTRIBUTION



HI DISTRIBUTION



“Warm Dark Matter as a solution to the small scale crisis: new constraints from high redshift Lyman- α forest data” MV+ arXiv:1306.2314

DATA: 25 high resolution QSO spectra at $4.48 < z_{\text{em}} < 6.42$
from MIKE and HIRES spectrographs. Becker+ 2011

SIMULATIONS: Gadget-III runs: 20 and 60 Mpc/h and $(512^3, 786^3, 896^3)$

Cosmology parameters: σ_8 , n_s , Ω_m , H_0 , m_{WDM}

Astrophysical parameters: z_{reio} , UV fluctuations, T_0 , γ , $\langle F \rangle$

Nuisance: resolution, S/N, metals

METHOD: Monte Carlo Markov Chains likelihood estimator
+ **very conservative assumptions** for the continuum
fitting and error bars on the data

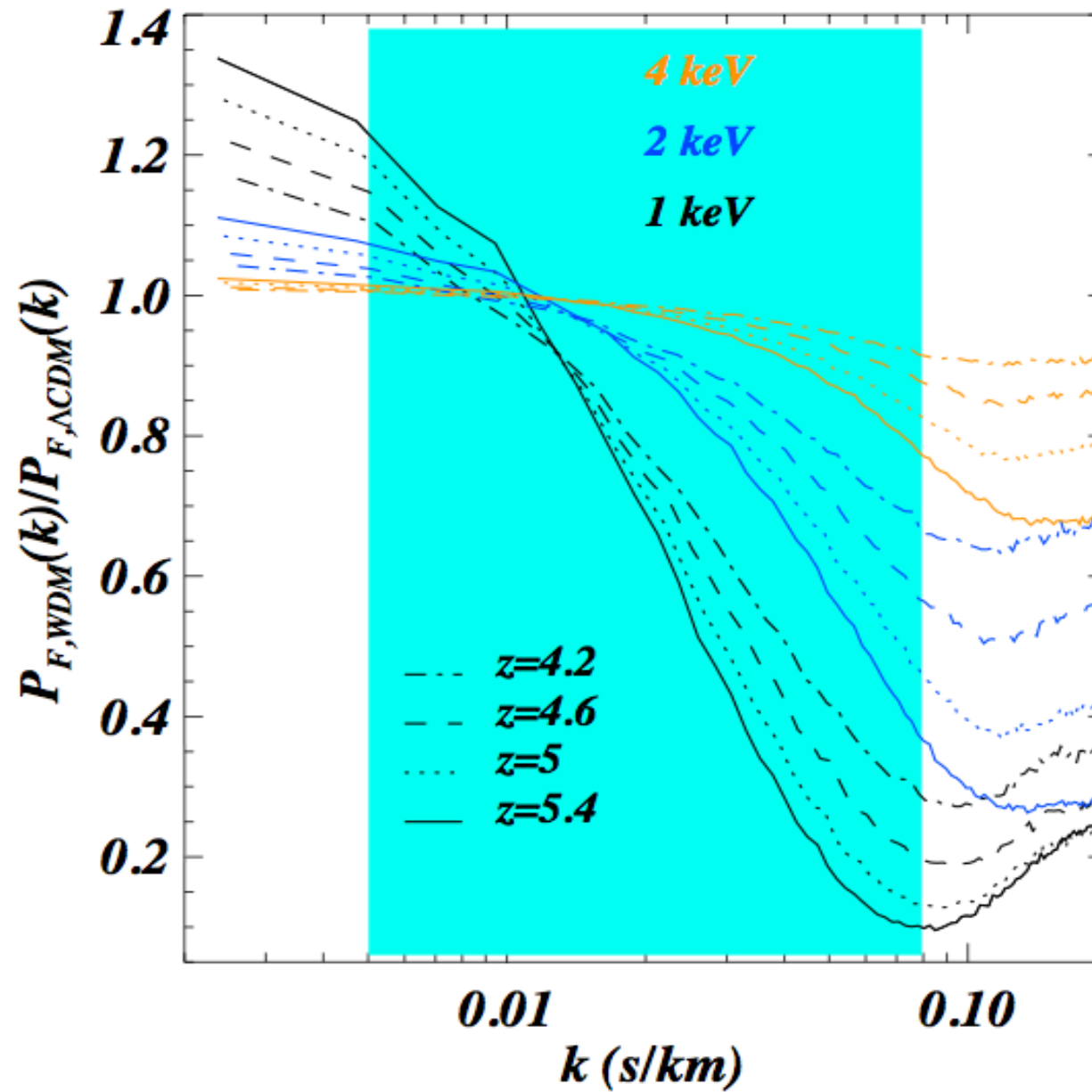
Parameter space: m_{WDM} , T_0 , γ , $\langle F \rangle$ explored fully

Parameter space: : σ_8 , n_s , Ω_m , H_0 , UV explored with second order
Taylor expansion of the flux power

$$P_F(k, z; \mathbf{p}) = P_F(k, z; \mathbf{p}^0) + \sum_i^N \left. \frac{\partial P_F(k, z; \mathbf{p}_i)}{\partial p_i} \right|_{\mathbf{p}=\mathbf{p}^0} (p_i - p_i^0) + \text{second order}$$

THE HIGH REDSHIFT WDM CUTOFF

$$\delta_F = F/\langle F \rangle - 1$$



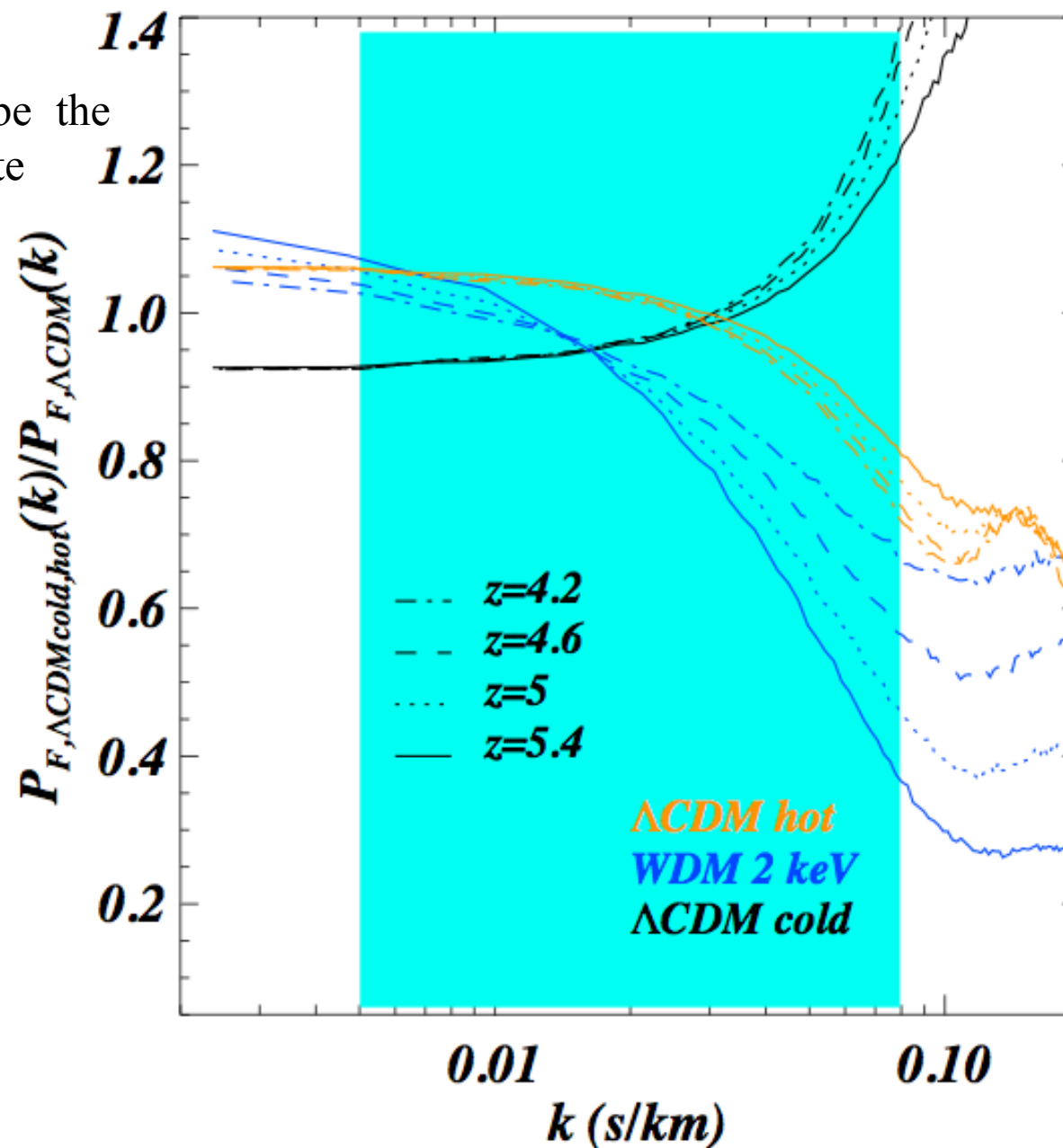
THE TEMPERATURE: T_0

$$T = T_0(1 + \delta)^{\gamma-1}$$

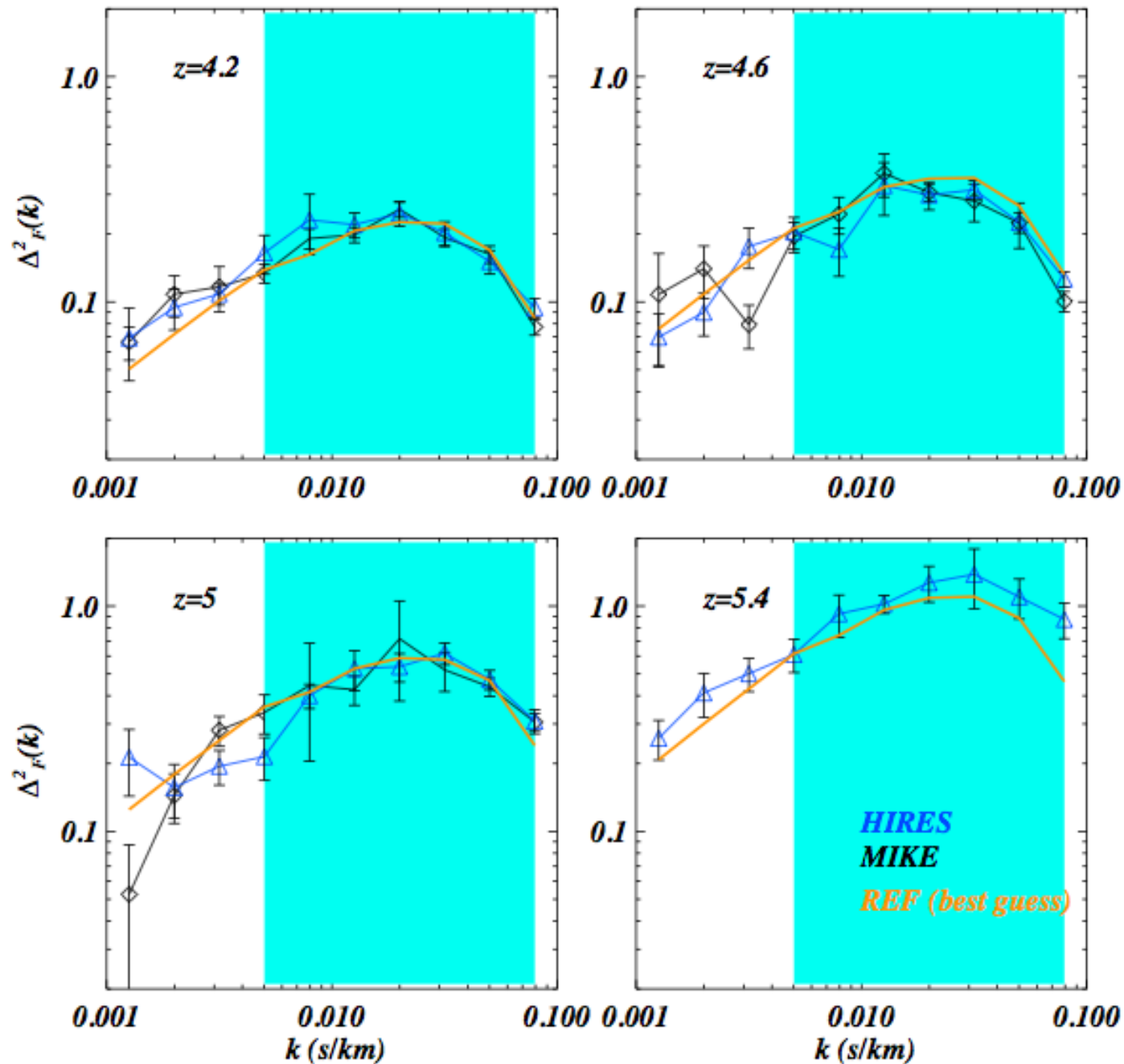
T_0 and γ describe the
IGM thermal state

Hot + 3000 K
Cold – 3000 K

REF has 8300 K
at $z=4.6$

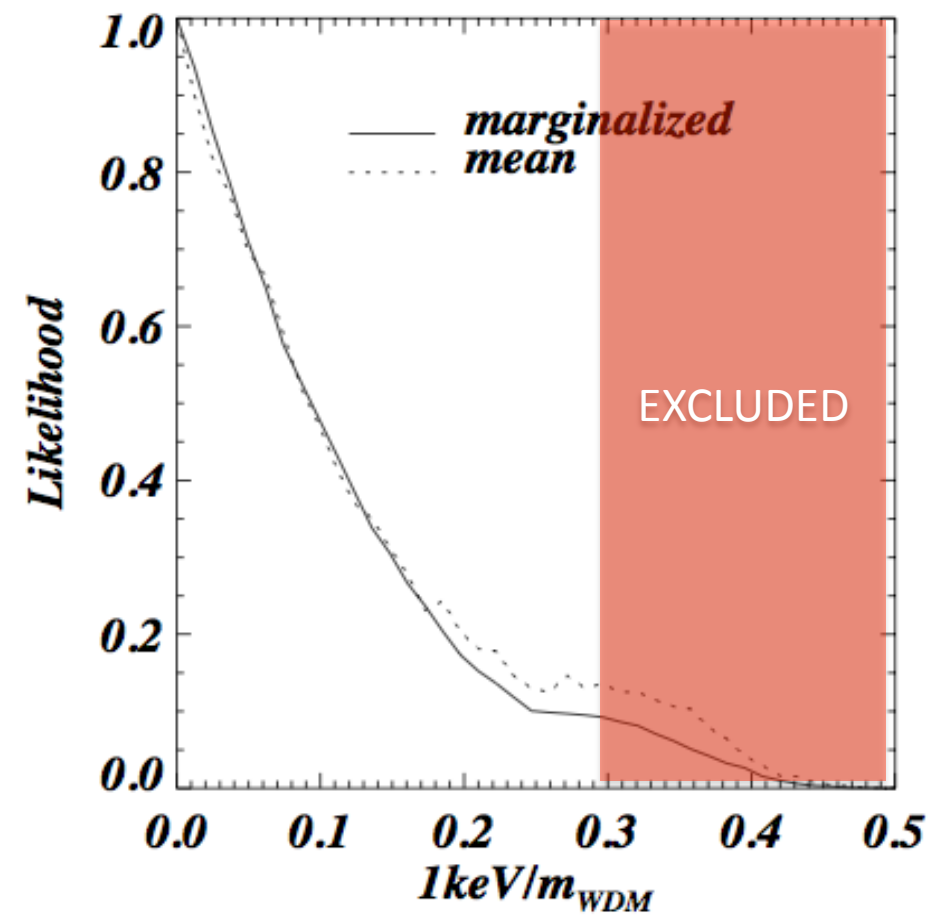


THE BEST GUESS MODEL



This is the starting point of the MCMC likelihood estimation cosmology close to Planck values

RESULTS FOR WDM MASS

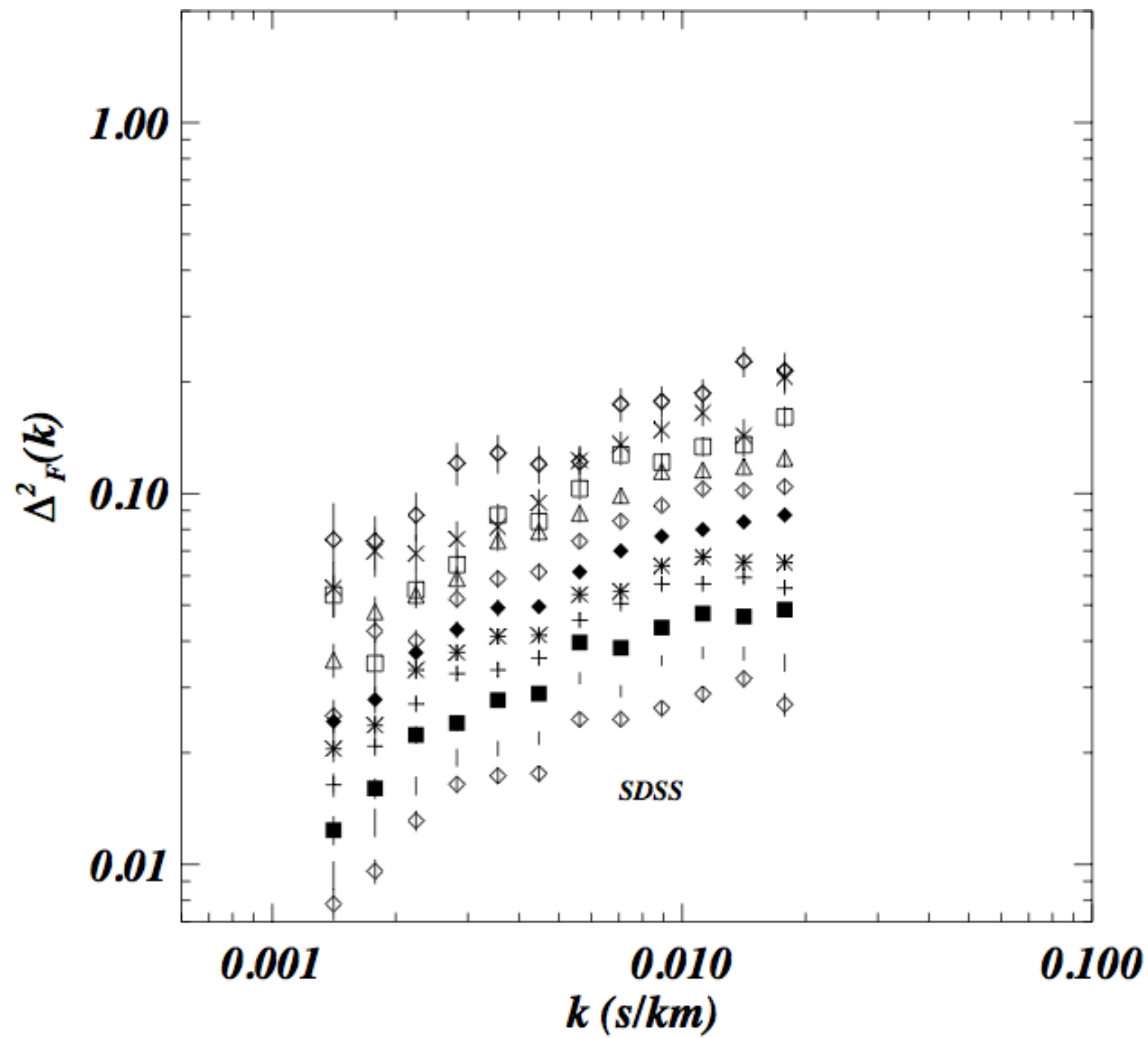


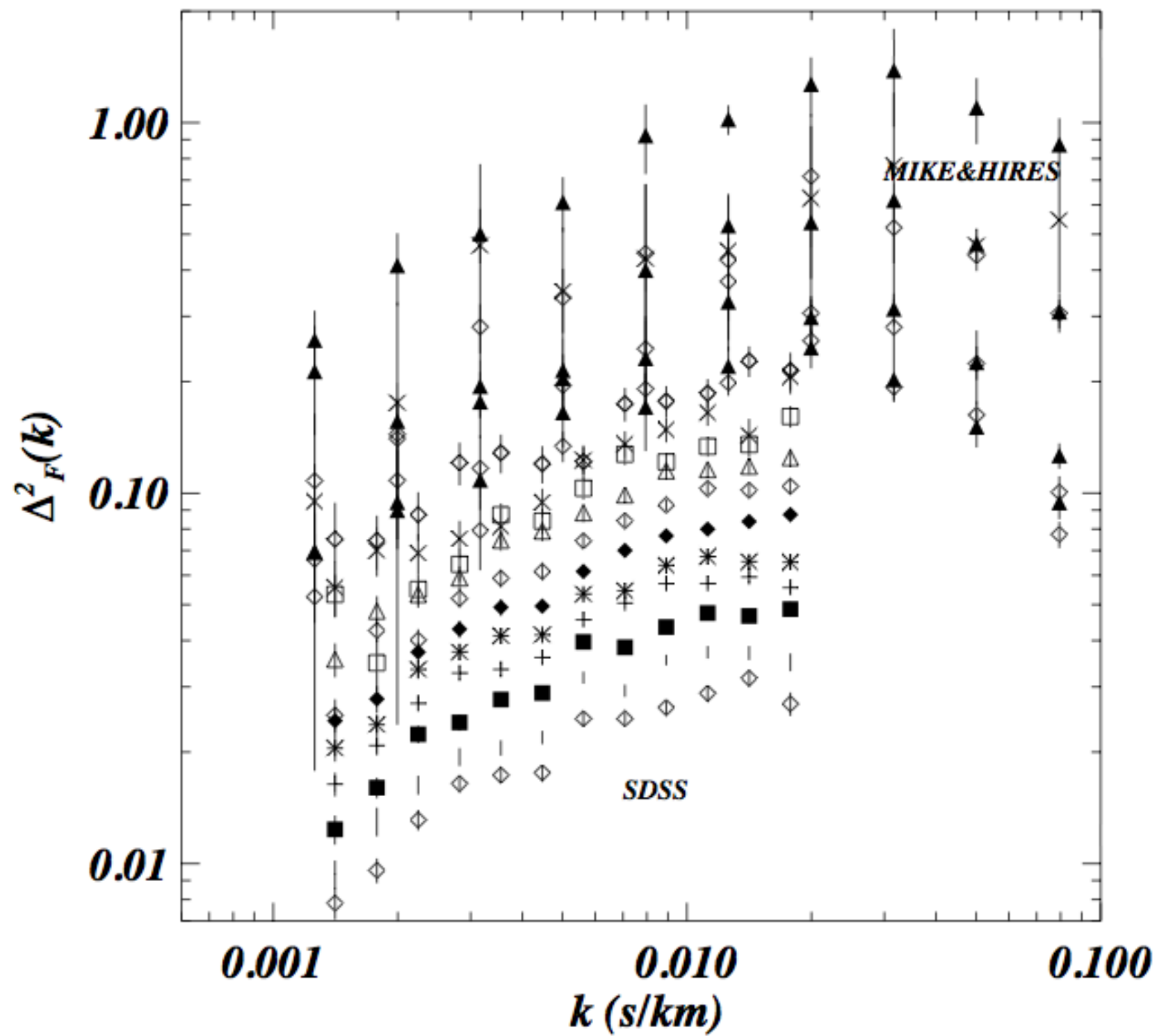
$m > 3.3 \text{ keV} (2\sigma)$

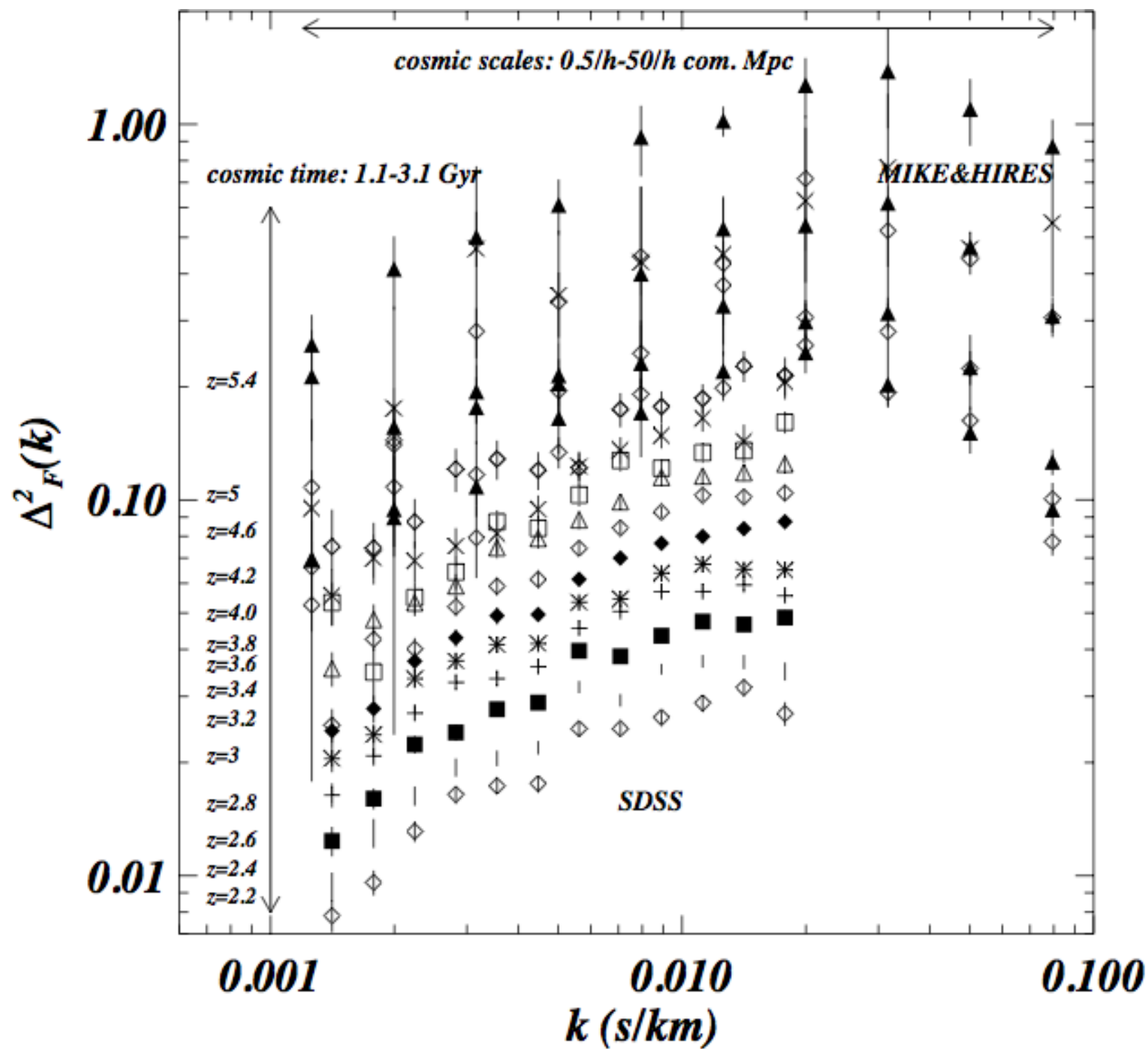
SDSS + MIKE + HIRES CONSTRAINTS

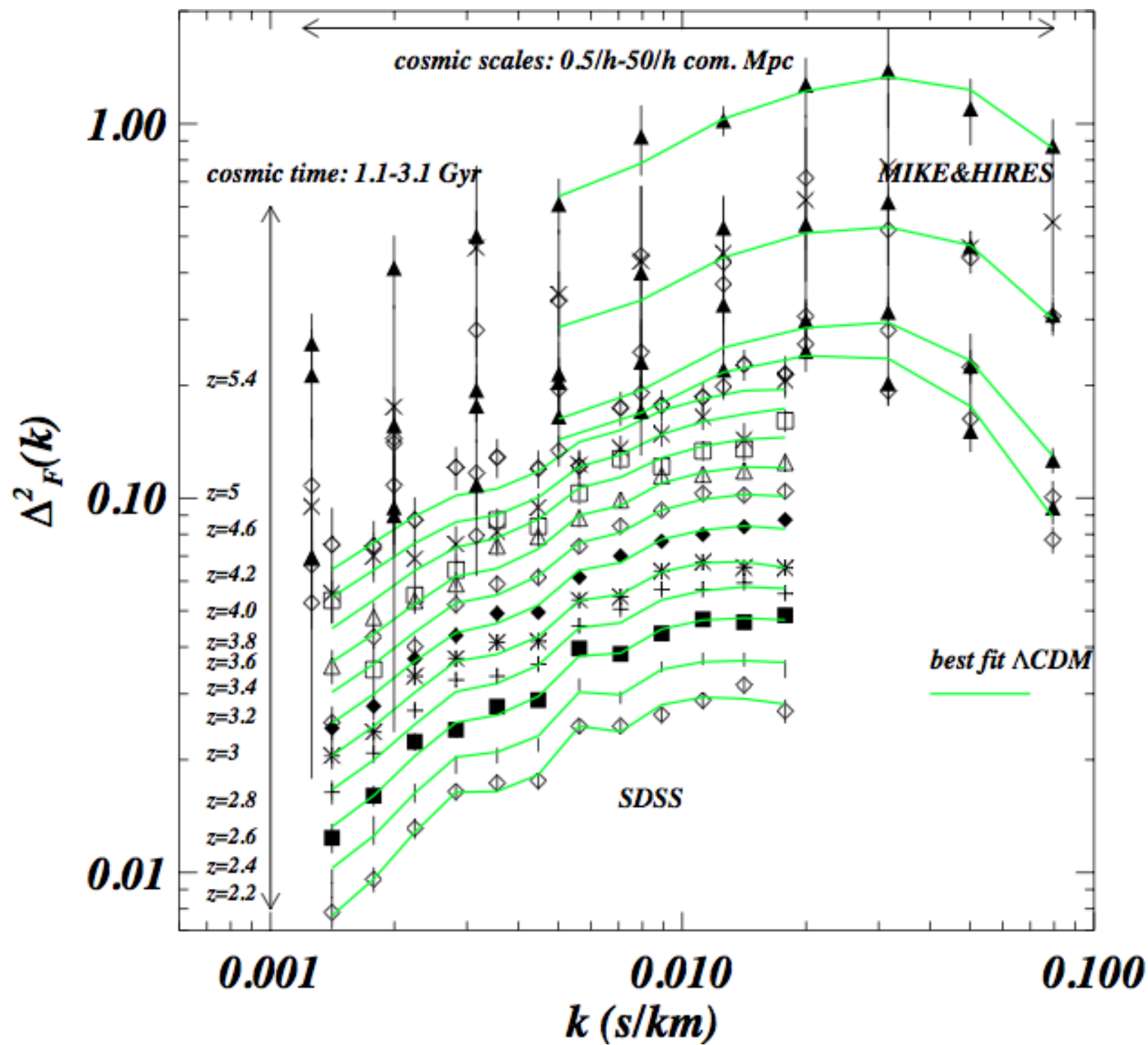
Joint likelihood analysis

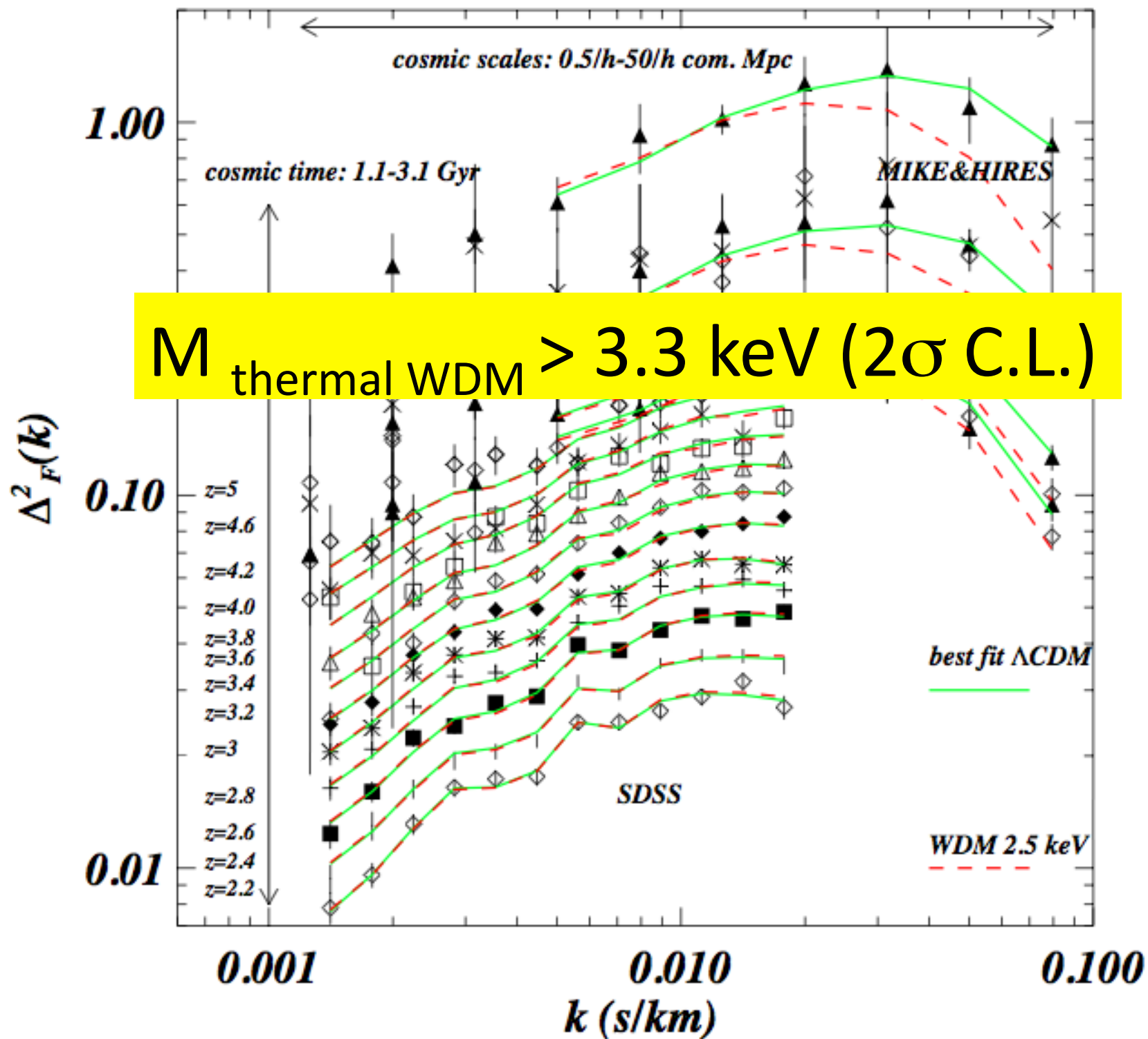
SDSS data from McDonald05,06 not BOSS











CONCLUSIONS – GEOMETRY and NEUTRINOS

Constraints on the geometry of the Universe via BAO measurements of Ly α and cross-correlations. Small tension with Planck.

Galaxy clustering data tend to give < 0.3 eV
CMB + BAO < 0.2 eV

1D Lyman- α flux power provides the tightest constraints (< 0.14 eV using old SDSS) on total neutrino mass. This was improved recently by using new SDSS/BOSS data with new methods and new simulations. The result is

< 0.14 eV

CONCLUSIONS – NEUTRINO COSMOLOGY FUTURE

Neutrino non-linearities modelled in the matter power spectrum, correlation function, density distribution of haloes, peculiar velocities, redshift space distortions. NEW REGIME!

Forecasting for Euclid survey: 14 meV error is doable but need to model the power spectrum to higher precision (possibly subpercent) and with physical input on the scale dependence of the effect.
Very conservative 20-30 meV

CONCLUSIONS – WARM DARK MATTER

High redshift Lyman- α disfavours thermal relic models with masses that are typically chosen to solve the small-scale crisis of Λ CDM

Models with 1 keV are ruled out at 9σ

2 keV are ruled out at 4σ

2.5 keV are ruled out at 3σ

3.3 keV are ruled out at 2σ

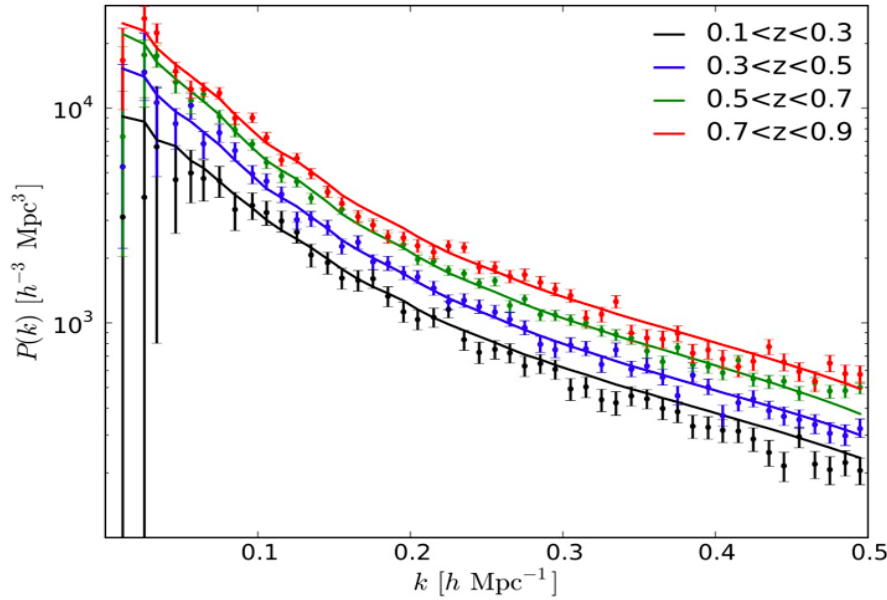


1) free-streaming scale is $2 \times 10^8 M_{\odot}/h$

2) at scales $k=10 h/\text{Mpc}$ you cannot suppress more than 10% compared to Λ CDM

Of course they remain viable candidate for the Dark Matter (especially sterile neutrinos) but there are OBSERVATIONAL challenges

TIGHTEST LIMITS PUBLISHED SO FAR



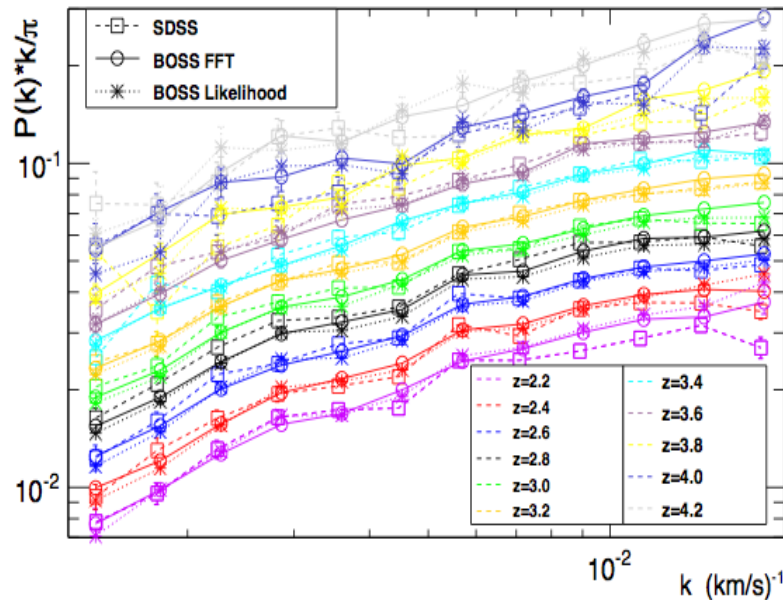
WiggleZ survey + Planck + HST + BAO

$$\Sigma m_\nu < 0.18 \text{ eV (} 2\sigma \text{ C.L.)}$$

Riemer-Sorensen et al. 13

Beutler et al. 14

$$\Sigma m_\nu = 0.34 \pm 0.14 \text{ eV,}$$



Intergalactic Medium data + CMB

$$\Sigma m_\nu < 0.17 \text{ eV (} 2\sigma \text{ C.L.)}$$

Seljak et al. 06

Viel, Haehnelt & Springel 2010

IGM alone $\Sigma m_\nu < 0.9 \text{ eV (} 2\sigma \text{ C.L.)}$

RESULTS FOR TEMPERATURE

$$\gamma^A(z) = \gamma^A[(1+z)/5.5]^{\gamma_A^S} \quad T_0^A(z) = T_0^A[(1+z)/5.5]^{T_0^S}$$

